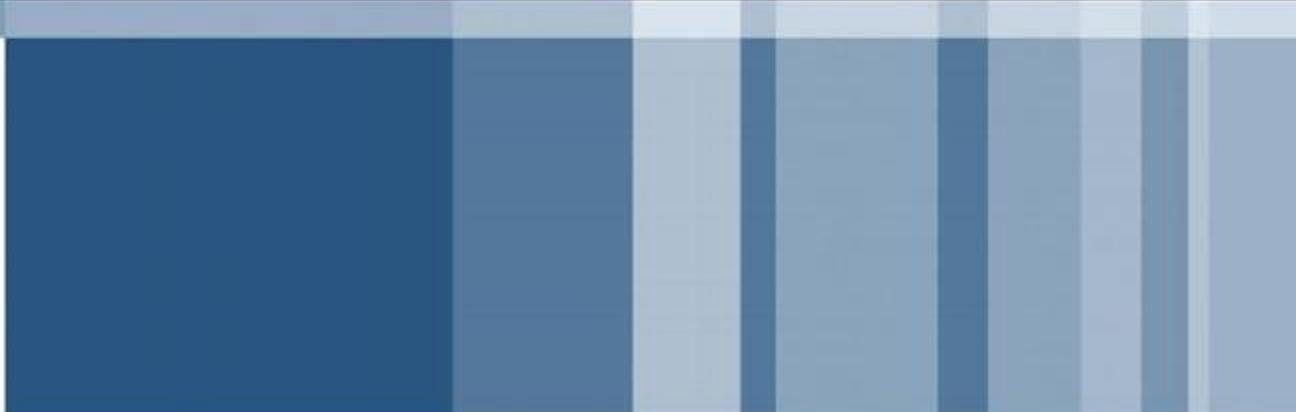




Department of Chemistry, Materials, and Chemical Engineering
Politecnico di Milano (Italy)



POLITECNICO
DI MILANO



Alberto Cuoci

Numerical simulation of NO_x formation in turbulent
flames through the Kinetic Post-Processing (KPP)
technique

Université Libre de Bruxelles

March 5th, 2014 – Bruxelles (Belgium)

1. The CRECK Modeling Group @ Politecnico di Milano
2. Introduction
3. The Kinetic Post Processing (KPP) Technique for NOx
 - ✓ Kinetic mechanisms for CFD applications
 - ✓ Reactor networks from CFD
 - ✓ Effects of temperature fluctuations on NOx formation
 - ✓ Solution of reactor networks
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 - ✓ Lab-scale flames
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5. Extension to other pollutants
6. Conclusions

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The CRECK Modeling Group

People

Full Professors



Eliseo Ranzi



**Tiziano
Faravelli**

Assistant Professors



**Alessio
Frassoldati**



Alberto Cuoci

PhD Students



Mattia Bissoli



Matteo Pelucchi



Chiara Saggese



**Alessandro
Stagni**



**Giancarlo
Gentile**



Paulo De Biagi

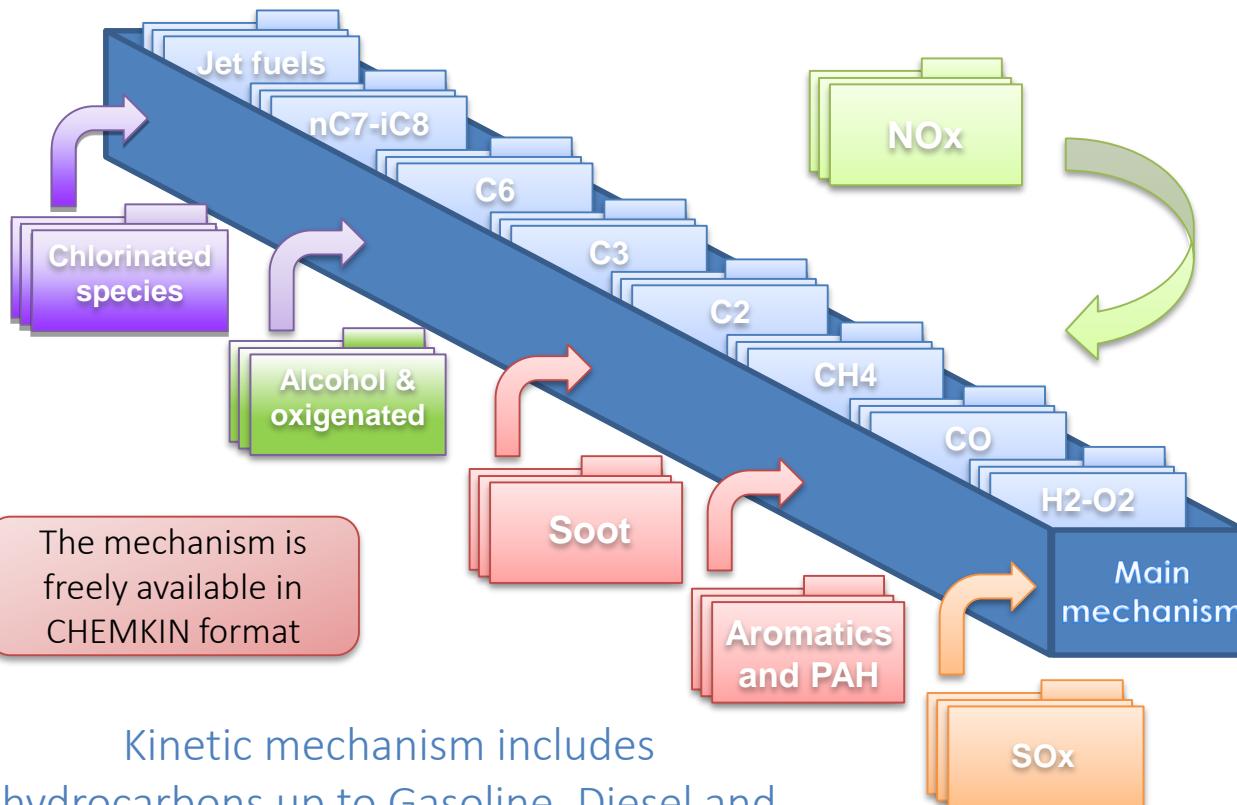
Permanent Staff



Dipartimento di Chimica, Materiali e
Ingegneria Chimica "Giulio Natta"
Politecnico di Milano

<http://creckmodeling.chem.polimi.it/>

Detailed kinetic mechanism

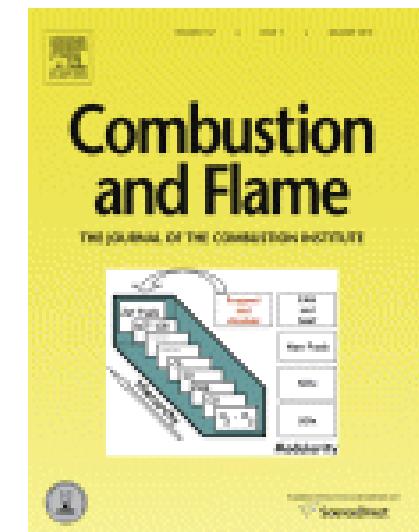


Kinetic mechanism includes hydrocarbons up to Gasoline, Diesel and jet fuels, as well as several pollutants

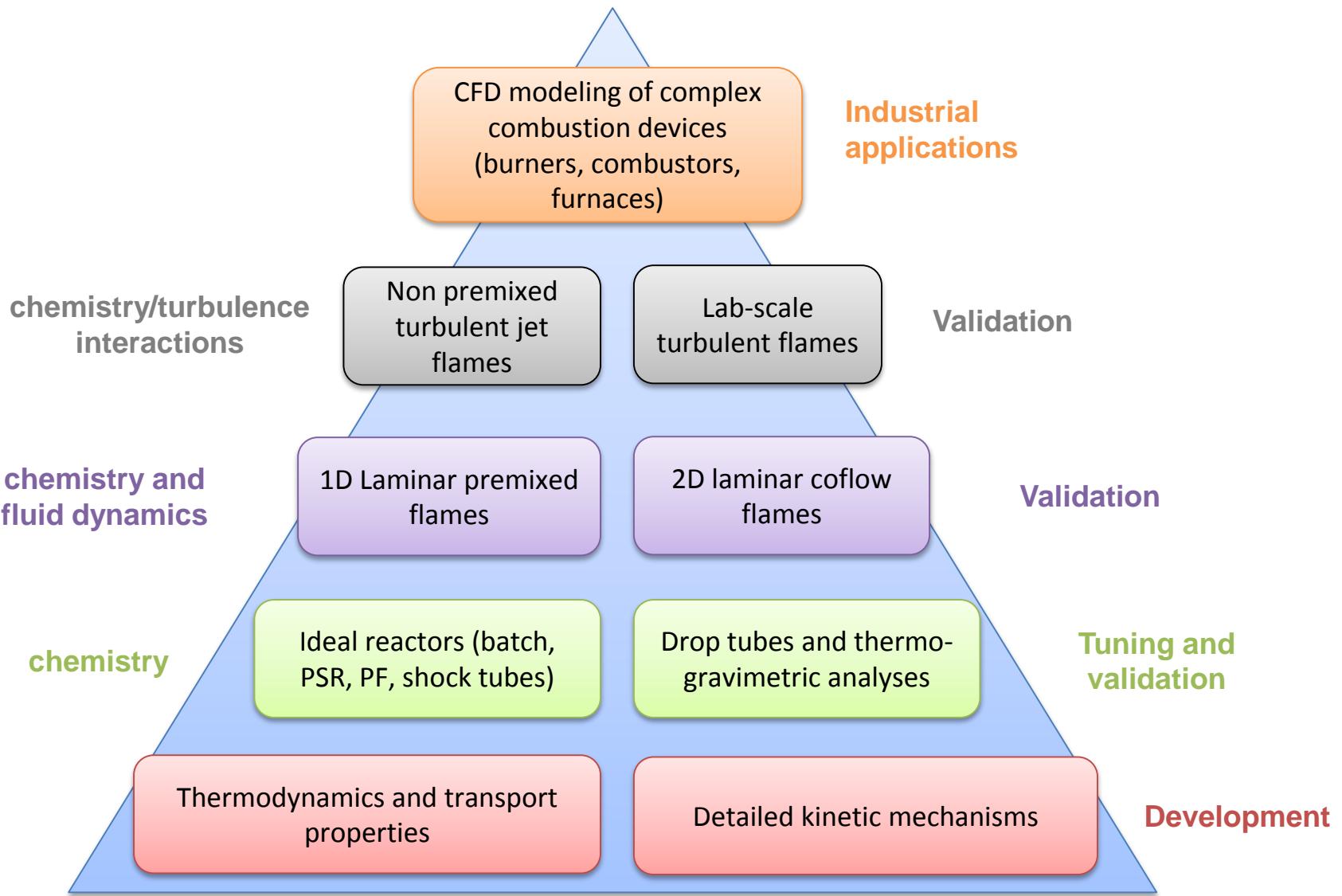
A. Frassoldati, A. Cuoci, Faravelli T., Niemann U., Ranzi E., Seiser K., Seshadri K., Combustion and Flame 157(1), 2-16 (2010)

Ranzi, E., Frassoldati, A., Grana, R., Cuoci, A., Faravelli, T., Kelley, A.P., Law, C.K, Progress in Energy and Combustion Science, 38 (4), pp. 468-501 (2012)

- Hierarchy
 - Modularity
 - Generality
- ~ 500 species
- ~ 15,000 reactions



From molecules to furnaces



The CRECK Modeling Group on the web

HOME RESEARCH PEOPLE KINETIC SCHEMES PUBLICATIONS COLLABORATIONS COURSES WORK WITH US

CRECK Modeling

Chemical Reaction Engineering and Chemical Kinetics

Environmental Targets for 2020*

Reduce noise by 50%
The ECAC targets represent a double-digit reduction in the environmental impact of air transport.
Reduce fuel consumption and CO₂ emissions by 50%
Advisory Council for Aerospace Research in Europe. Targets are valid to year 2020.

CFD Modeling of combustors for aero-engines
The emissions of pollutant species (CO, NO_x, unburned hydrocarbons, etc.) from combustors used for aero-engines are estimated through a post-processing technique based on very detailed kinetic mechanisms.

You are here: Home

RECENT PUBLICATIONS

- Cuoci A. et al., Experimental and detailed kinetic modeling study of PAH formation in laminar co-flow methane diffusion...
- Saggese C. et al., A lumped approach to the kinetic modeling of pyrolysis and combustion of biodiesel fuels, Procedia...
- Ranzi E. et al., Hierarchical and comparative kinetic modeling of laminar flame speeds of hydrocarbon and oxygenated f...

AVAILABLE MASTER THESIS

- Simplified kinetics of solid fuels for CFD
Abstract: The larger availability and lower cost of coal, in respect to other...
- Next generation engines (HCCI)
Abstract: The increasing attention for the environmental issues has been...
- Laminar coflow flames doped with alcohols
Abstract: Since the late 1970s, oxyfuels have been used in gasoline...

Welcome to CRECK Modeling

The Chemical Reaction Engineering and Chemical Kinetics group has a consolidated experience of the development of detailed and semi-detailed kinetic mechanisms of the pyrolysis, oxidation and combustion of gas, liquid and solids. The group is lead by Prof. Eliseo Ranzi and Prof. Tiziano Faravelli and includes 3 professors, 2 assistant professors and 4 PhD students.

NEW! TRAINING SCHOOL

The COST CM0901 Training School on Modeling Combustion Kinetics will be hosted by Politecnico di Milano and it will take place from July 8th to 12th, 2013 in Milano (Italy).

[Read more...](#)

PEOPLE

- Eliseo Ranzi
- Tiziano Faravelli
- Alessio Frassoldati

Comprehensive Kinetic Schemes

Detailed kinetic schemes constitute a very useful tool for the proper understanding of combustion processes and the characterization of typical phenomena like ignition delays and induction times, flame structure and pollutant formation.

Design, simulation, optimization and control of industrial burners, gas turbines, boilers, incinerators and gasifier are typical application as well as the design of internal combustion engines and the formulation of new fuels.

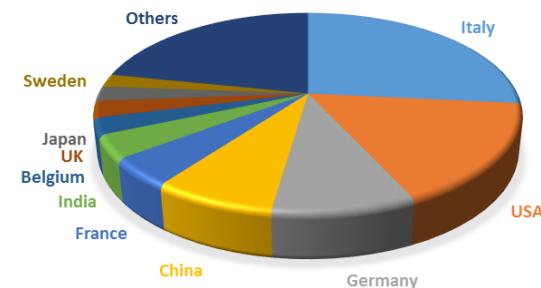
4,287 Visitors 5 MAY 2013 - 25 MAY 2013
[Click to see](#)

The kinetic schemes can be freely downloaded in CHEMKIN format from our web site:

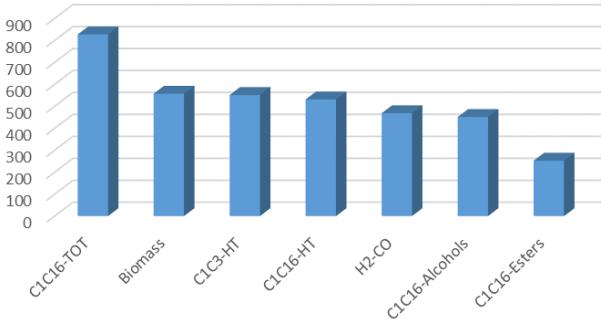
<http://creckmodeling.chem.polimi.it/>

Statistics since January 2013

Unique visitors: 9,600
Visits: 12,000 (~28 per day)
Visits from 97 countries



The kinetic schemes were downloaded more than 3,600 times since Jan 2013



Academic and Industrial Collaborations

8



● Academic

● Industrial

Academic collaborations (I)

Rensselaer Polytechnic Institute
M. Oehlschlaeger
Decalin ignition

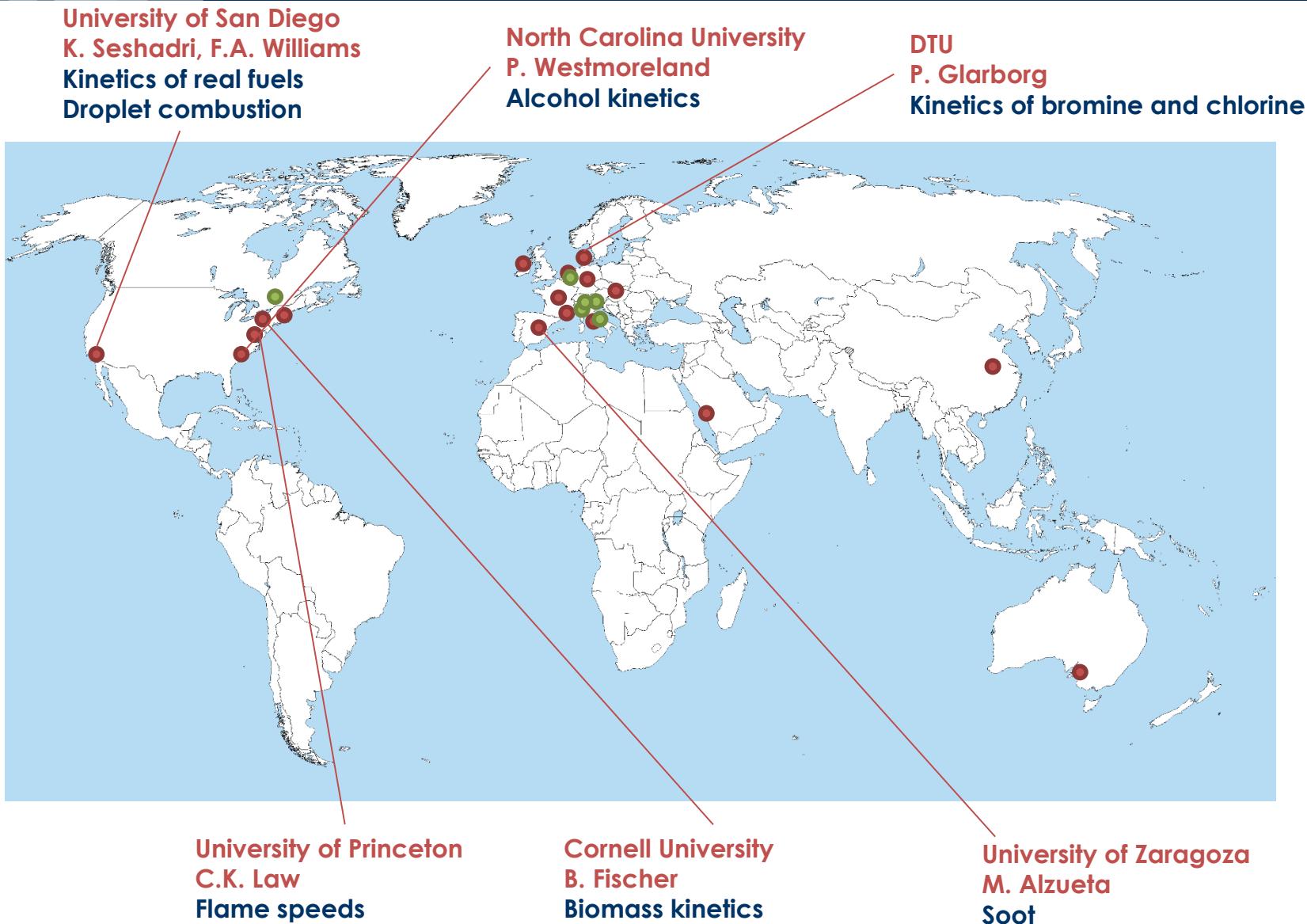
University of Galway
H. Curran
Oxygenated fuels

Université Libre de Bruxelles
A. Parente
Reduction of kinetic mechanisms



Academic collaborations (II)

10



Academic collaborations (III)

University of Bielefeld
K. Kohse-Höinghaus
Alcohols kinetics

University of Ostrava
V. Nevrly
Pulsating flames

University of Hefei
F. Qi
Laminar, coflow flames



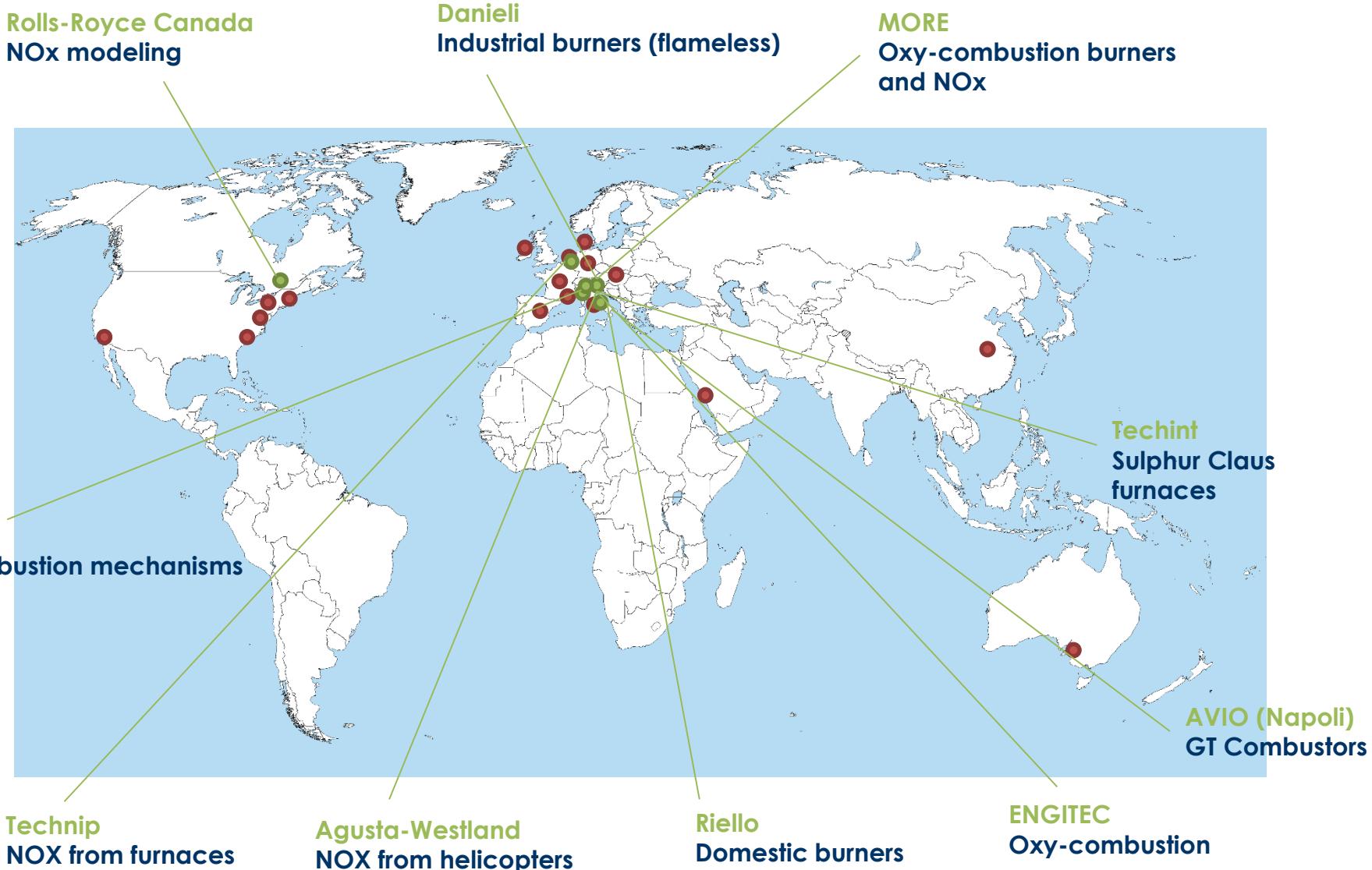
University of Nancy
F. Battin-Leclerc
Kinetics of large methyl-esters

KAUST University
M. Sarathy
PRIME Project

University of Adelaide
P. Medwell
MILD combustion

Industrial collaborations

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Reduction of pollutant emissions (I)

14

Increasingly stringent regulations for pollutant emissions in furnaces, power plants, gas turbines, burners etc.

Pollutant	Health Effect
CO – Carbon Monoxide	<ul style="list-style-type: none">Cardiovascular effects, especially in those persons with heart conditions
HC – Unburned Hydrocarbons (a primary component of Volatile Organic Compounds, or VOC)	<ul style="list-style-type: none">Eye and respiratory tract infectionHeadachesDizzinessVisual disordersMemory impairment
NO_x – Nitrogen Oxides PM – Particulate Matter (smoke is a primary component of PM.)	<ul style="list-style-type: none">Lung irritationLower resistance to respiratory infections <ul style="list-style-type: none">Premature mortalityAggravation of respiratory and cardiovascular diseaseChanges in lung functionIncreased respiratory symptomsChanges to lung tissues and structureAltered respiratory defence mechanisms



Environmental Targets for 2020*

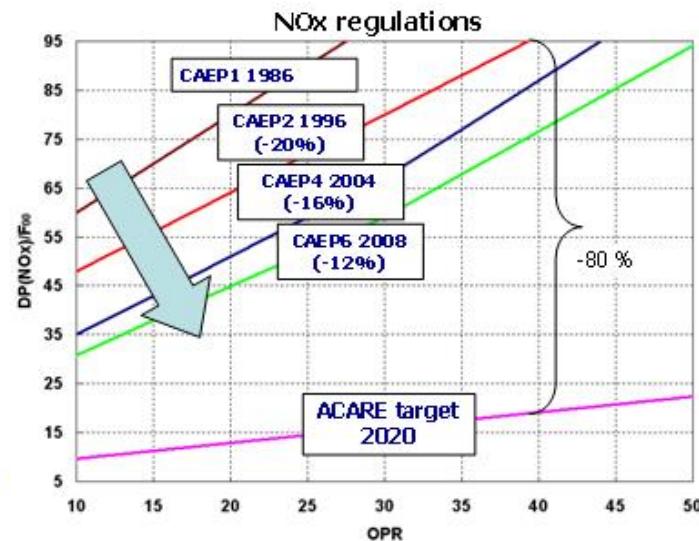
Reduce noise by 50%



The ACARE targets represent a doubling of the historical rate of improvement...

Reduce fuel consumption and CO₂ emissions by 50%

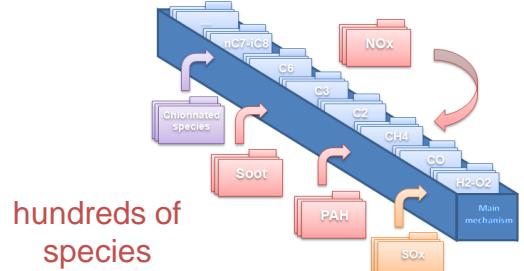
Reduce NOx emissions by 80%



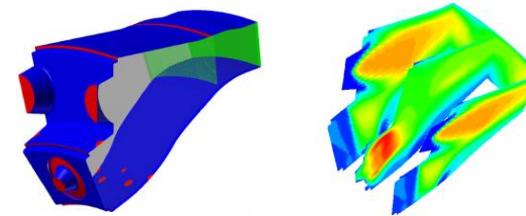
Advisory Council for Aeronautics Research in Europe.
Targets are relative to year 2000

Combustion is a complex process that involves hundreds of species and thousands of chemical reactions.

Detailed kinetic schemes



CFD simulations



millions of computational cells



Jet fuels and surrogate mixtures

need of modeling synergistic effects between the different components



Oxyfuel combustion

need of including radical species (O, H, OH, etc.)

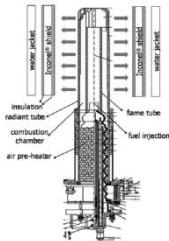
Biofuels

bioalcohols, biodiesel, green diesel, bioethers



Flameless combustion

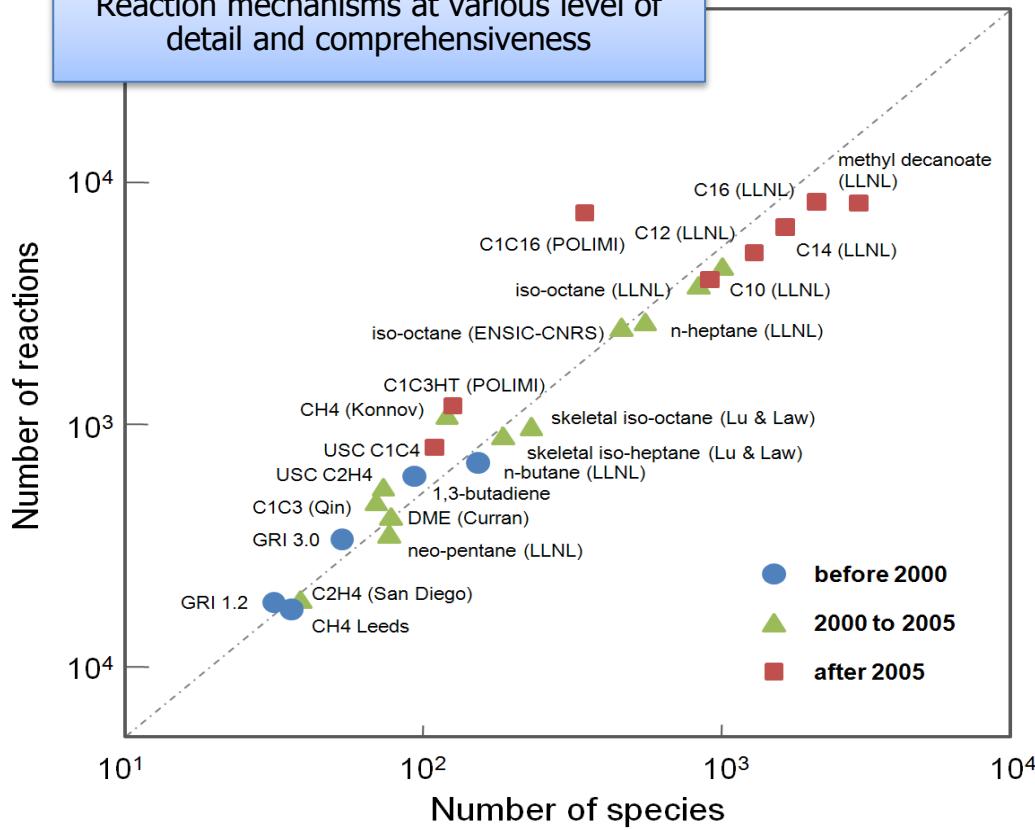
(low Damkholer number, slow chemistry)



Detailed kinetic mechanisms

17

Reaction mechanisms at various level of detail and comprehensiveness



Adapted from:

T.F. Lu, C.K. Law, *Prog. Energy Comb. Sci.*, 35 (2009)

increasing effort to incorporate **more complex reaction mechanisms** in simulation of combustion processes and this has led to the development of reaction mechanisms with different levels of detail and comprehensiveness

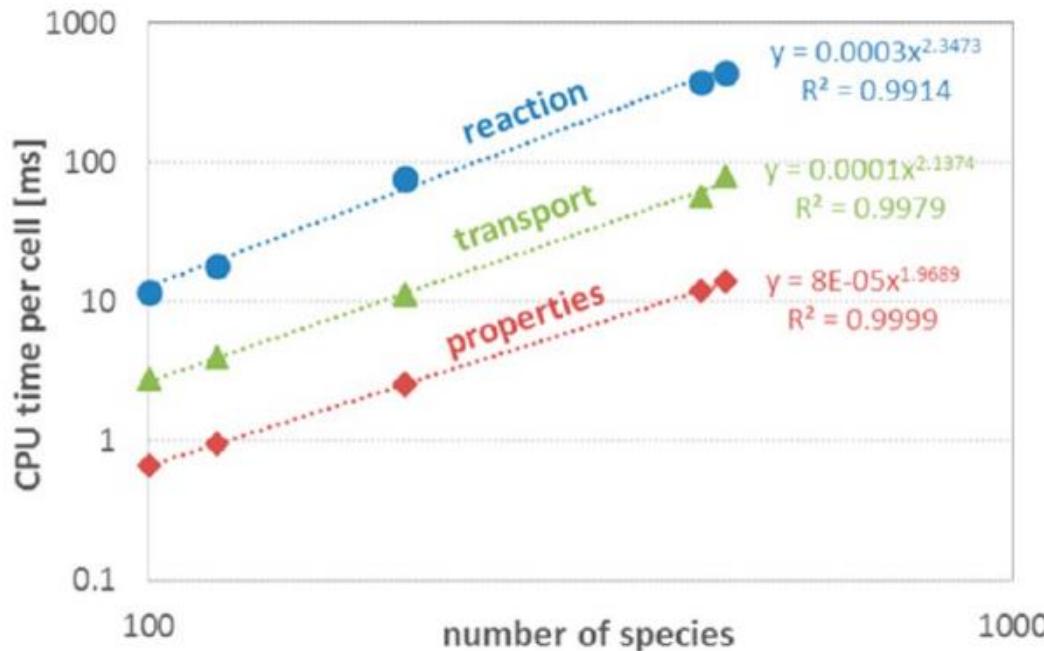
computational cost associated with such mechanisms is usually very high



need of **computational tools** to make computationally efficient the management of large kinetic schemes and easy their **integration** in new and/or existing numerical codes

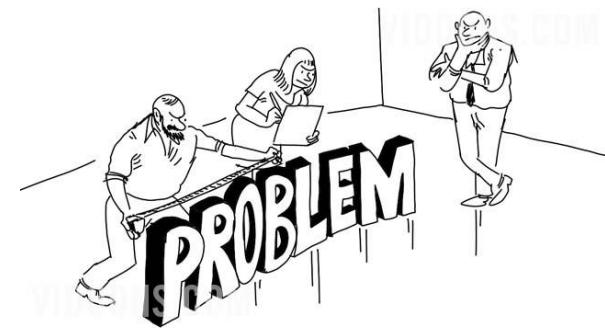
Computational cost of kinetics

18



Simulation of laminar, coflow flames fed with ethylene
(2D, structured grid, in-house code)

$$C \approx N^{2.5}$$



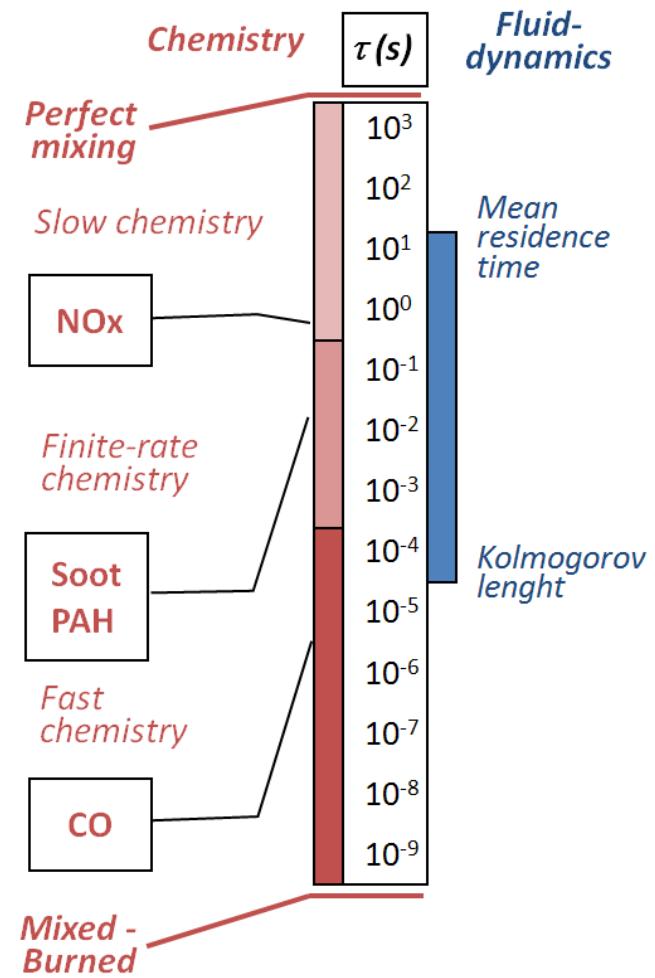
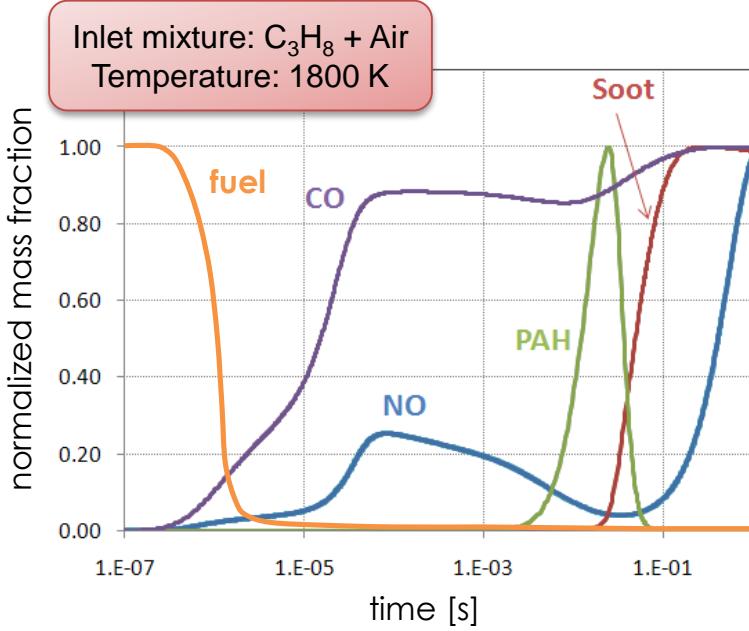
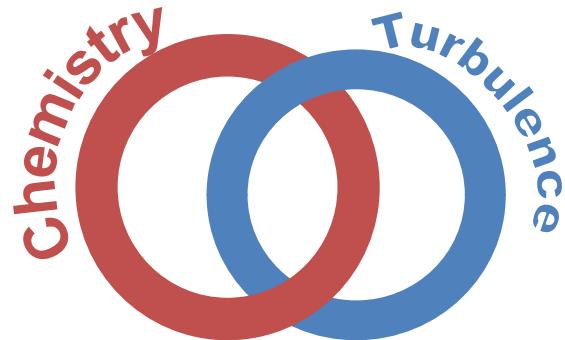
Usually the computational cost of multi-dimensional CFD simulations increases **more than quadratically** with respect to the number of species

Cuoci, A. Frassoldati, T. Faravelli, E. Ranzi, "Numerical Modeling of Laminar Flames with Detailed Kinetics Based on the Operator-Splitting Method", Energy & Fuels, 27 (12), p. 7730-7753 (2013), DOI: 10.1021/ef4016334

Coupling between turbulence and chemistry

19

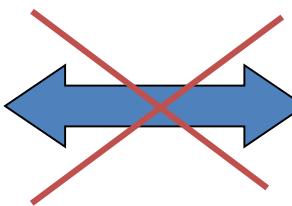
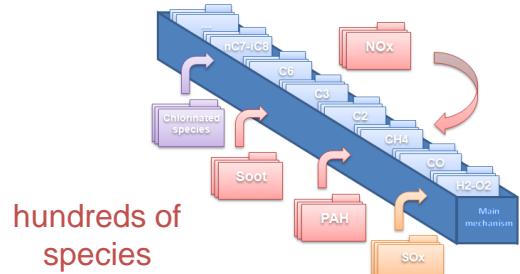
Strong coupling between chemistry and turbulence in combustion processes



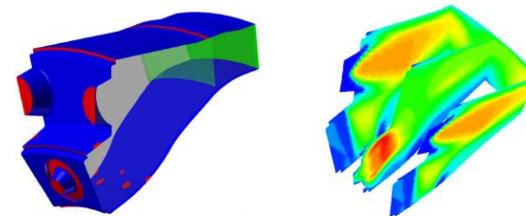
Adapted from:
R. Fox, "Computational models for turbulent reacting flows", Cambridge University Press (2002)

Combustion is a complex process that involves hundreds of species and thousands of chemical reactions.

Detailed kinetic schemes



CFD simulations



Jet fuels and surrogate mixtures

need of modeling synergistic effects between the different components



Oxyfuel combustion

need of including radical species (O, H, OH, etc.)

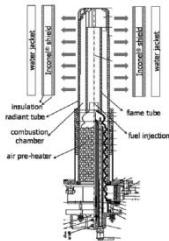
Biofuels

bioalcohols, biodiesel, green diesel, bioethers



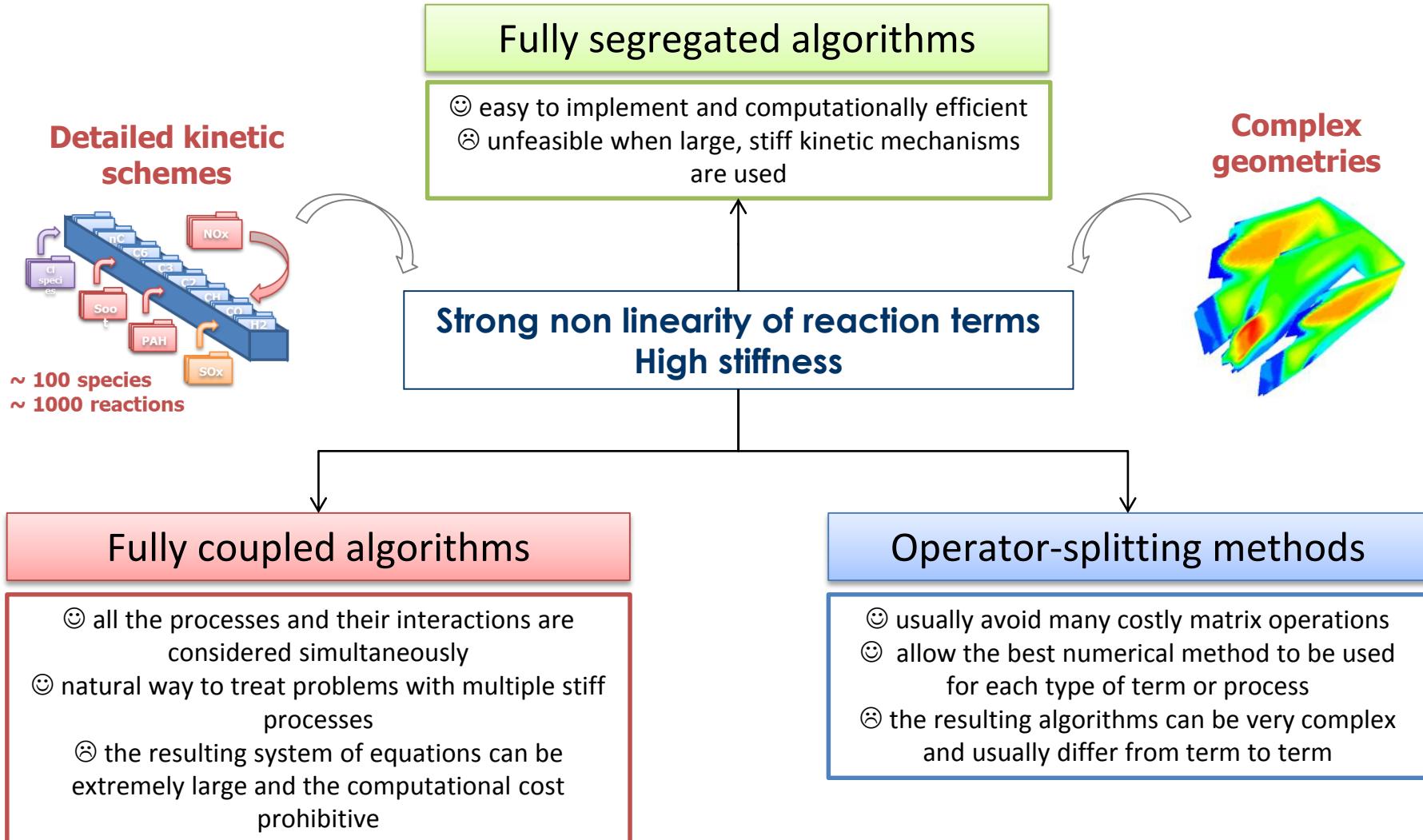
Flameless combustion

(low Damkholer number, slow chemistry)



Segregated vs Coupled Algorithms

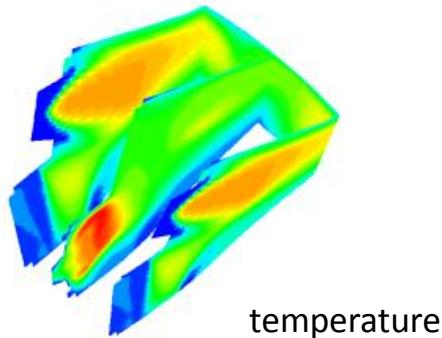
21



The Kinetic Post Processing technique

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CFD simulation

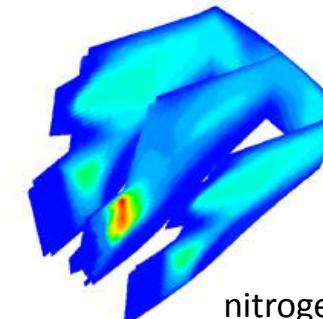


temperature

a steady state CFD simulation of the combustion device is performed using a **global kinetic mechanism**, which allows for the correct prediction of **thermal and flow fields**, but which cannot give us information on pollutant species

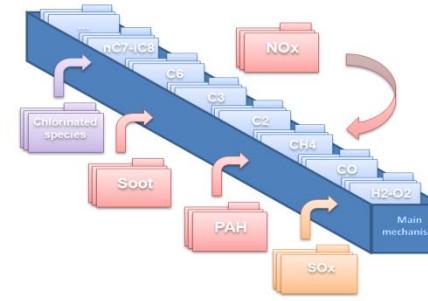
pollutant species usually affect only marginally the main combustion process and consequently do not influence the overall temperature and flow field

Post-Processing



nitrogen oxides
“slow” pollutant species

Detailed chemistry

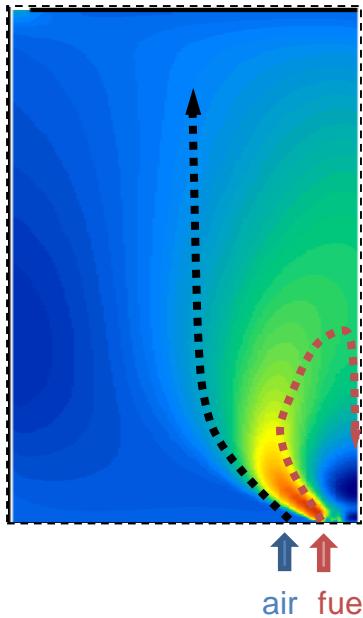


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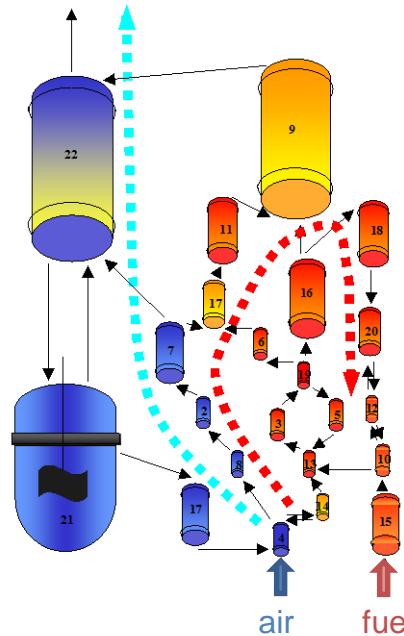
The Kinetic Post Processing technique

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1. CFD Simulation



2. Clustering and network construction



- ✓ The **clustering** reduces the overall dimensions of the problem
- ✓ According to the clustering, a complex **reactor network** is constructed

3. Interactions with the turbulence

- ✓ In each reactor a **fixed temperature** is assumed
- ✓ These temperature is **corrected** to take into account the effects of turbulent fluctuations on the mean reaction rates

4. Network solution

- ✓ A very **detailed kinetic scheme** is used
- ✓ High number of non linear equations
 - example: $100 \text{ species} \times 50,000 \text{ reactors} = 5,000,000 \text{ eqs}$
- ✓ Specifically conceived numerical method

Ehrhardt et al. (1998)

were **the first** to propose and apply the post-processing technique. A simplified network of ideal PSRs or plugflow reactors. The proposed zone model was restricted only to flows without recycling zones and with downstream convection much larger than upstream diffusion.

Falcitelli et al. (2002)

a **general algorithm to construct the reactor network**, and application to practical industrial systems, such as glass melting furnaces and pilot- and full-scale boilers.

Skjøt-Rasmussen et al. (2003)

retained **all of the individual cells** in the computational domain, which were treated as PSRs, with fixed temperature and mass flow rates, as predicted by the CFD simulation. The reactors were modeled using DKM and the effects of turbulent fluctuations were accounted for.

Fichet et al. (2010)

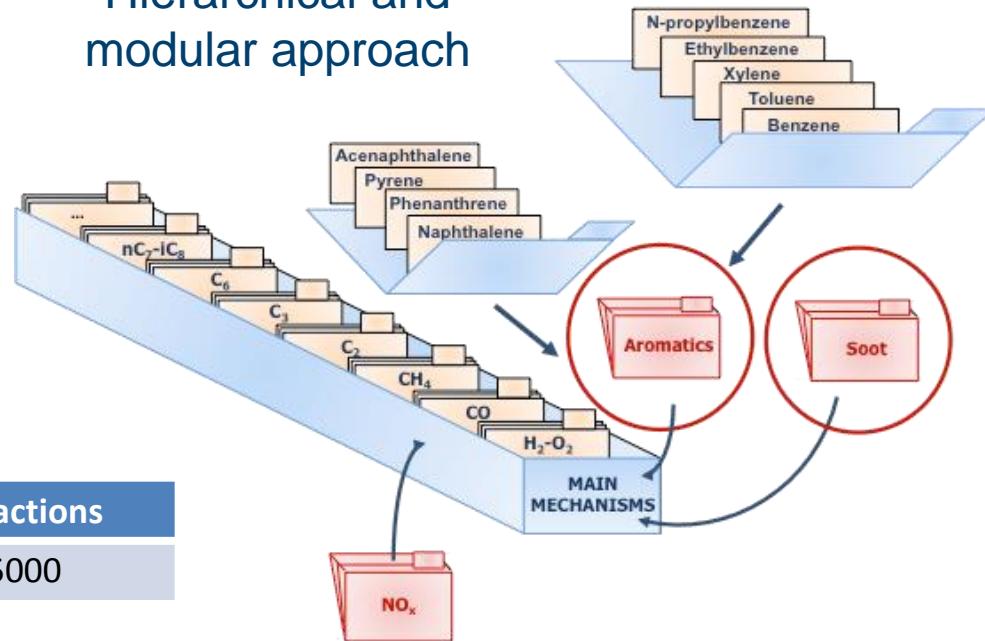
post-processing a gas turbine flame fed with natural gas. Attention was devoted to the **splitting criteria** to minimize the number of equivalent reactors the reactor **temperature was not assumed fixed** from CFD results, but the energy balance was solved during the post-processing phase.

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- ✓ Detailed mechanisms for hydrocarbon combustion may include thousands of species
- ✓ Lumping methodology is able to significantly reduce its number
- ✓ A further reduction is needed for their use in multidimensional models

Mechanism	# Species	# Reactions
Polimi_C1C16	500	15000

Hierarchical and modular approach



Detailed kinetics



Skeletal schemes



Global schemes



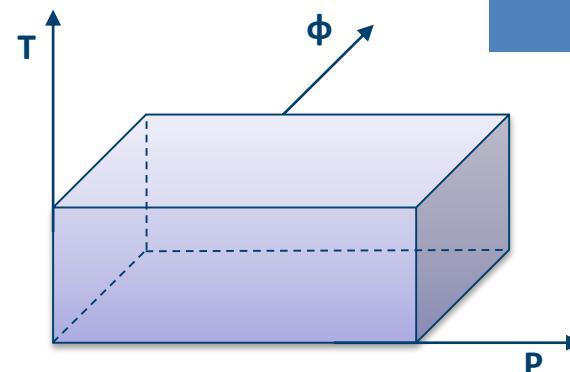
1.

Selection of testing conditions:

- ✓ Temperature: 700 – 2000 K
- ✓ Pressure: 1 – 50 atm
- ✓ Equivalence Ratios: 0.5 – 2

2.

- ✓ Progressive reduction of detailed kinetics.
- ✓ Analysis of Reacting fluxes in sample PFRs reactors



3.

Validation of reduced kinetics through comparison with experimental data and detailed mechanism:

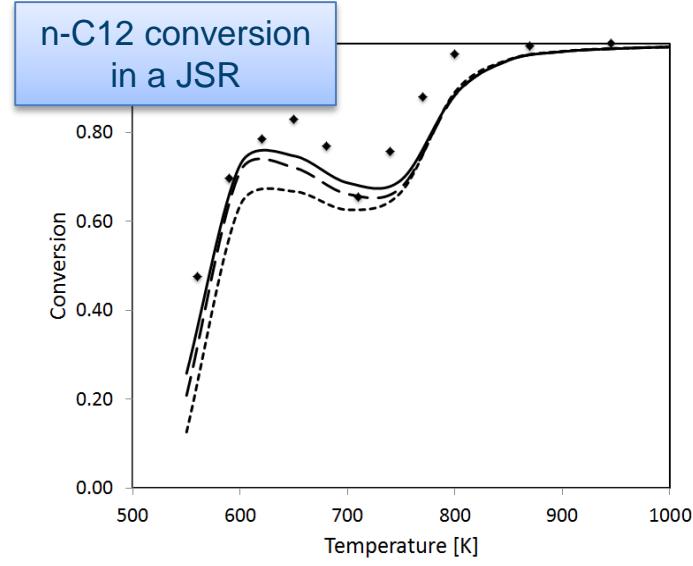
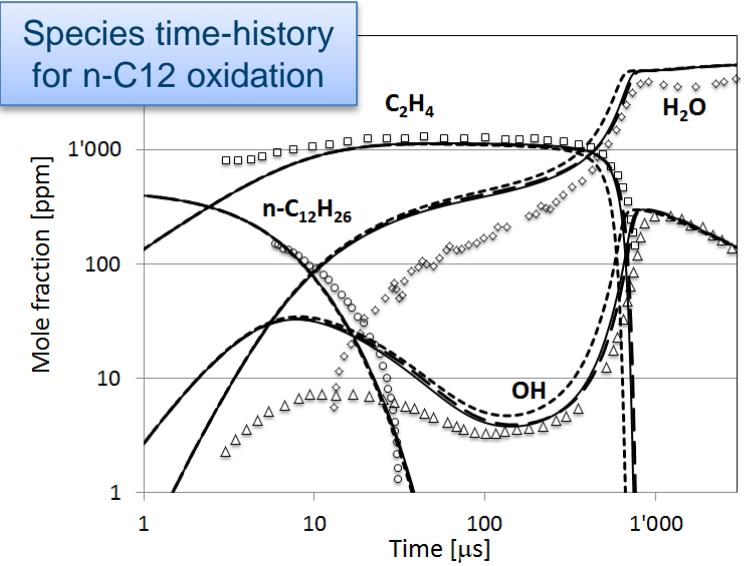
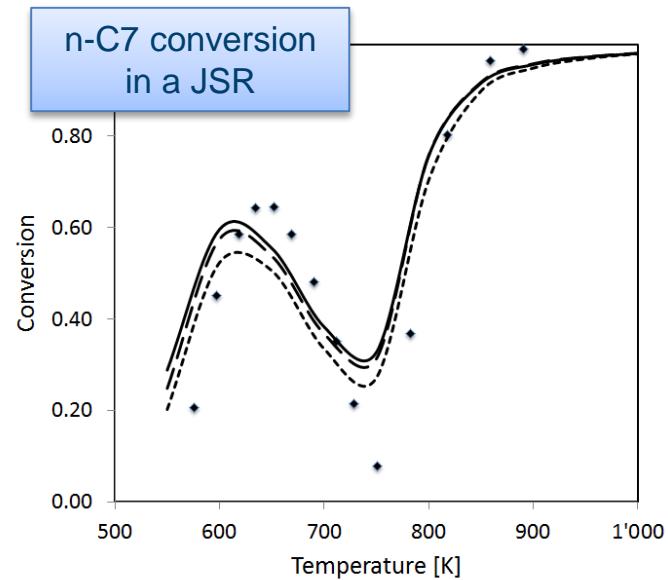
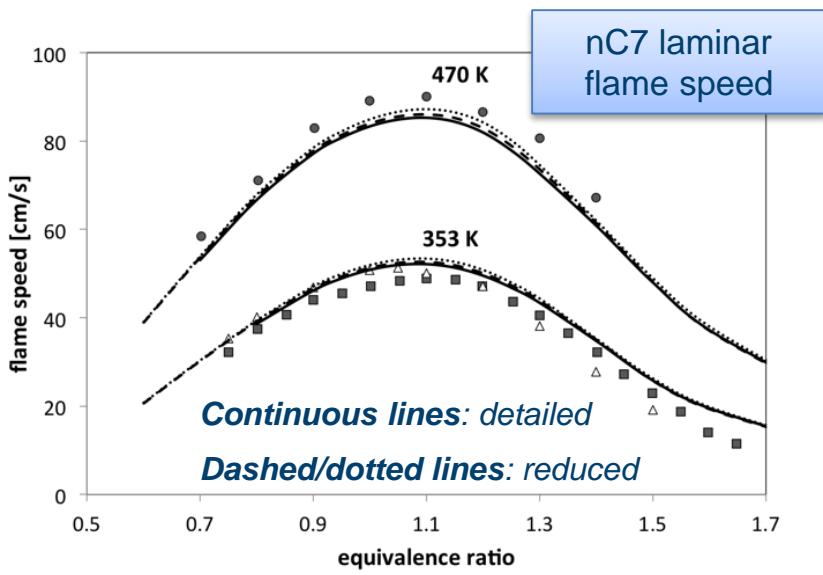
- Shock Tube Reactor
- Laminar Flame Speed
- Perfectly Stirred reactors

4.

Application to multi-dimensional codes

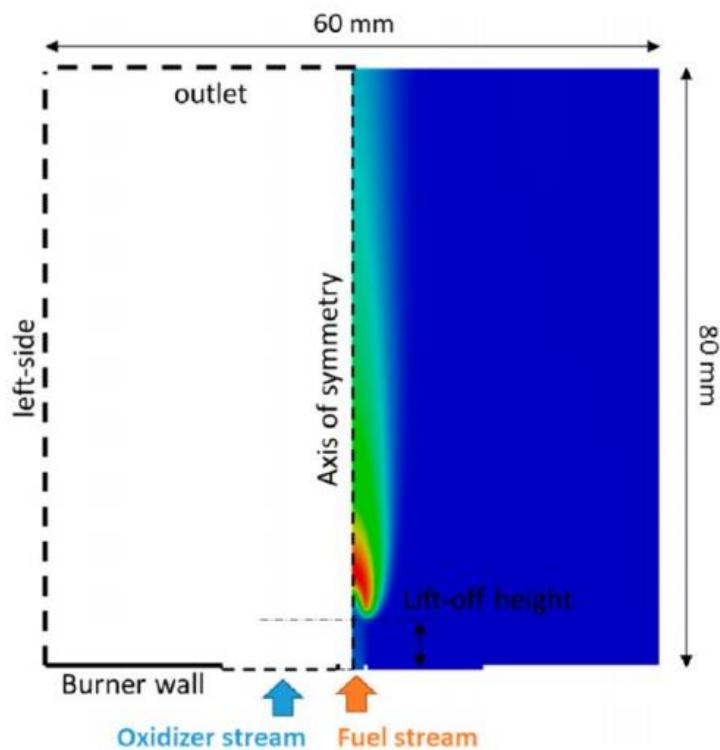
Stagni A., Cuoci A., Frassoldati A., Faravelli T., Ranzi E.,
Industrial & Engineering Chemistry Research, Accepted, In
press (2014), DOI: 10.1021/ie403272f

Reduced kinetic schemes



Validation in coflow flames

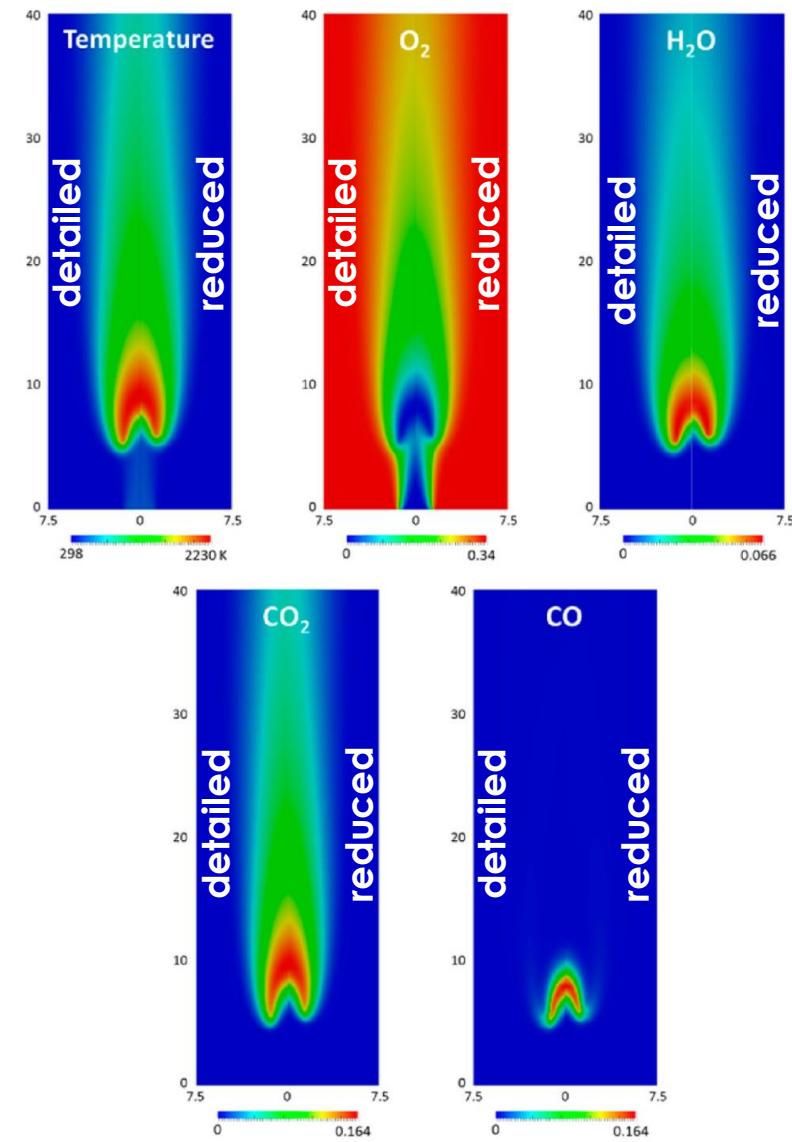
30



Fuel: 3.67% NC7 96.33% N₂ (vol.) @ 470K

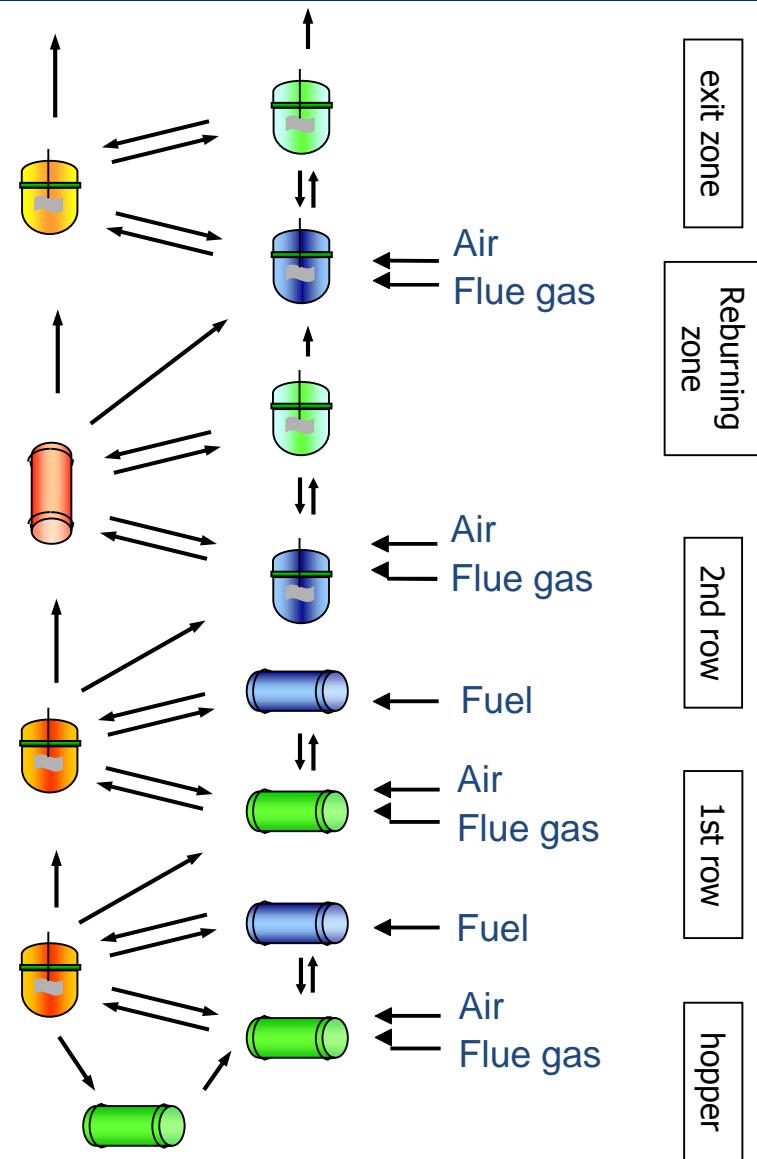
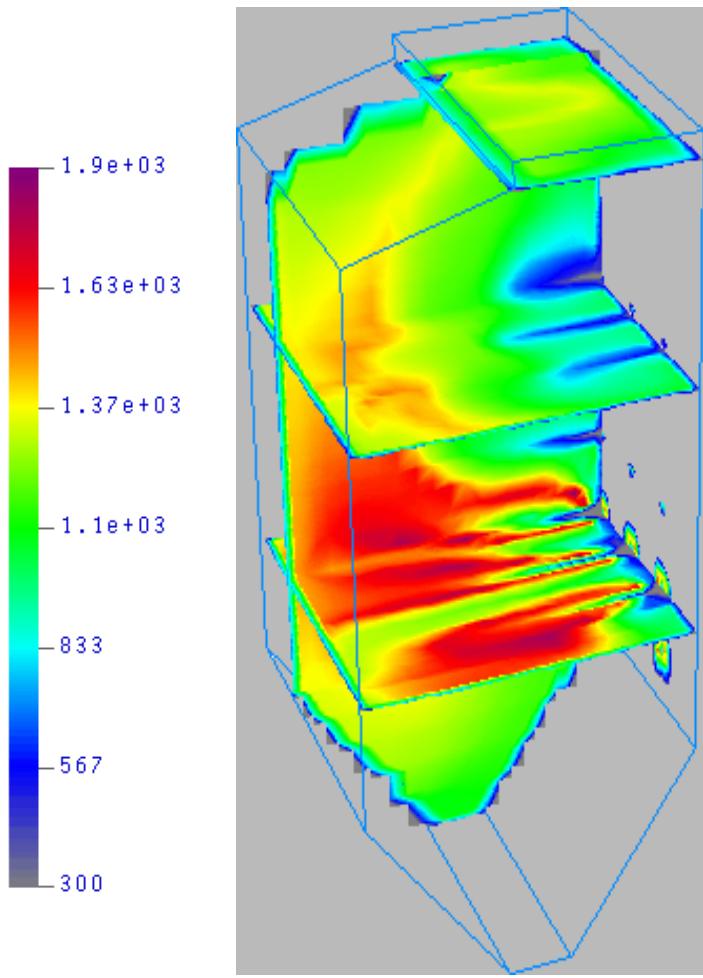
Oxidizer: 31% O₂ 69% N₂ (vol.) @ 300K

Velocities: 79 cm/s (F) and 68.7 cm/s (O)

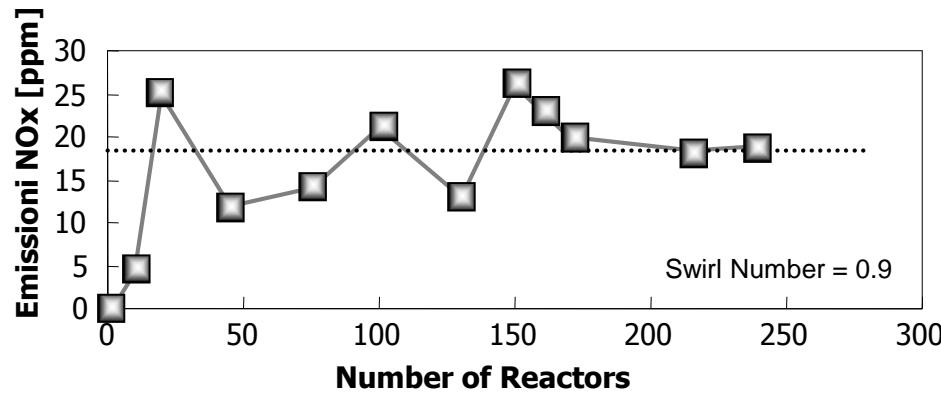
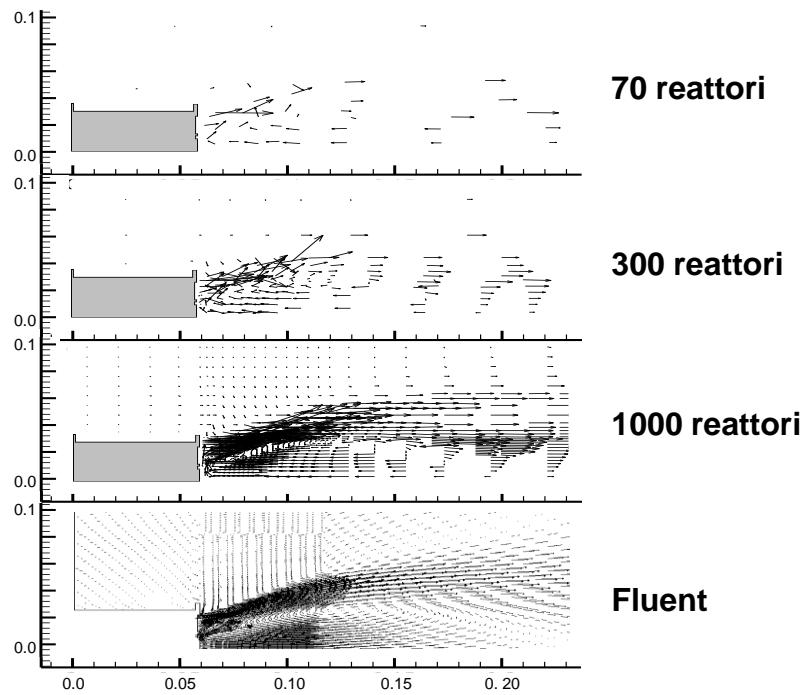
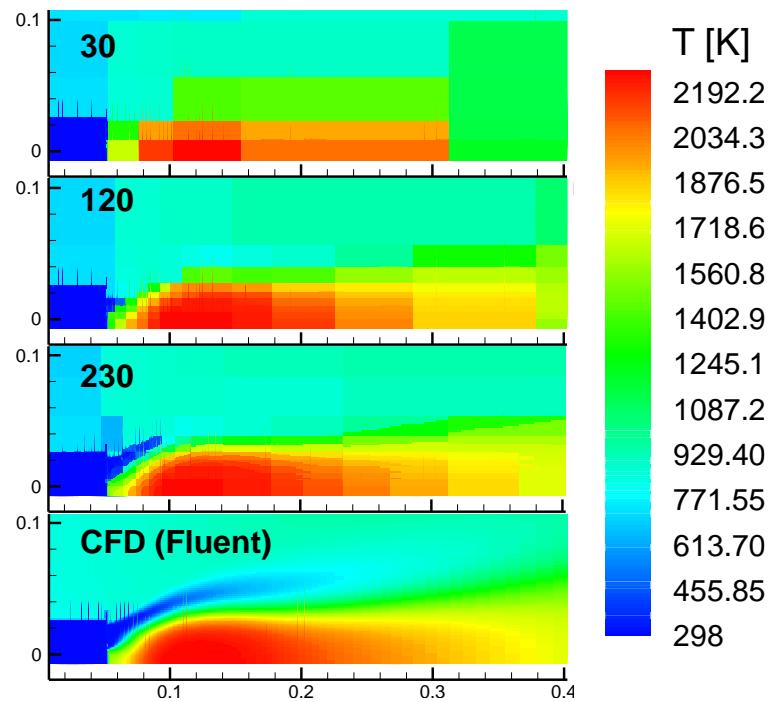


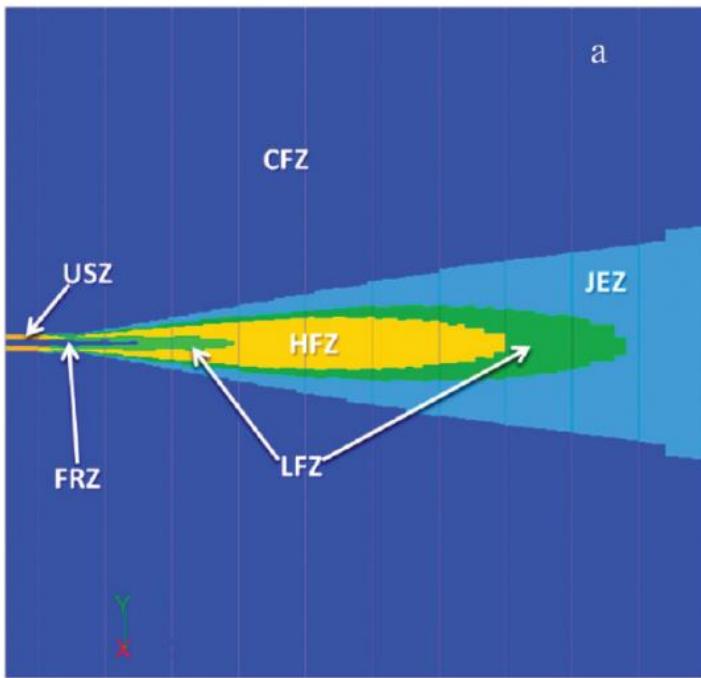
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Industrial furnace (Cassano d'Adda, 75 MW)



The clustering procedure (II)





upstream zone (USZ):

region between the furthest upstream part of the domain and the outlets of the jet and pilot

fuel-rich zone (FRZ):

where initial mixing and fuel decomposition occurs

low- and high-temperature flame zones (LFZ and HFZ):
where heat release rates are highest (i.e., the flame brush)

jet expansion zone (JEZ):

the region of combustion products at elevated temperatures

co-flow zone (CFZ):

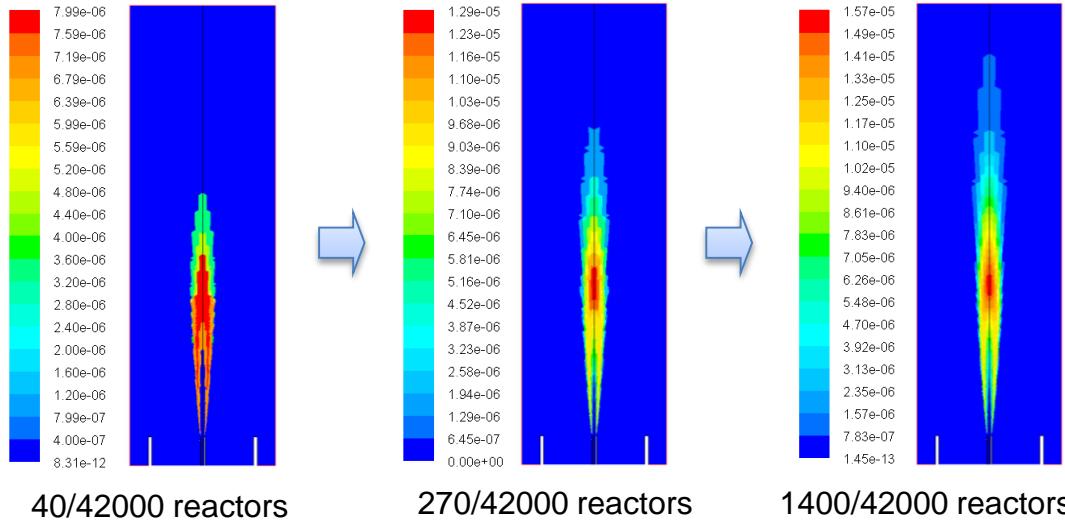
region of low-temperature, slow-moving air

Consider neighboring computational cells, whose z coordinates, temperatures, and mixture fractions place them within the limits of the same zone. If the differences in properties between the cells are less than those defined for their assigned zone (Δf , ΔT , and Δz), they are considered to be the same reactor in the CRN.

Monaghan, R.F.D., et al., *Detailed multi-dimensional study of pollutant formation in a methane diffusion flame* (2012) Energy and Fuels, 26 (3), pp. 1598-1611, DOI: 10.1021/ef201853k

zone	zone limits	reactor criteria
upstream zone (USZ)	$z < 0 \text{ m}$	n/a
fuel-rich zone (FRZ)	$z > 0 \text{ m}, 0.9 < f < 1.0$	$\Delta f = 0.01, \Delta z = 0.01 \text{ m}$
low-temperature flame zone (LFZ)	$z > 0 \text{ m}, 0.1 < f < 0.9, T < 1400 \text{ K}$	$\Delta T = 100 \text{ K}$
high-temperature flame zone (HFZ)	$z > 0 \text{ m}, 0.1 < f < 0.9, T > 1400 \text{ K}$	$\Delta T = 100 \text{ K} (T < 1800 \text{ K}), \Delta T = 50 \text{ K} (1800 \text{ K} < T < 2000 \text{ K}), \Delta T = 2 \text{ K} (T > 2000 \text{ K})$
jet expansion zone (JEZ)	$z > 0 \text{ m}, 0.01 < f < 0.1$	$\Delta T = 100 \text{ K}$
co-flow zone (CFZ)	$z > 0 \text{ m}, 0 < f < 0.01$	$\Delta z = 0.2 \text{ m}$

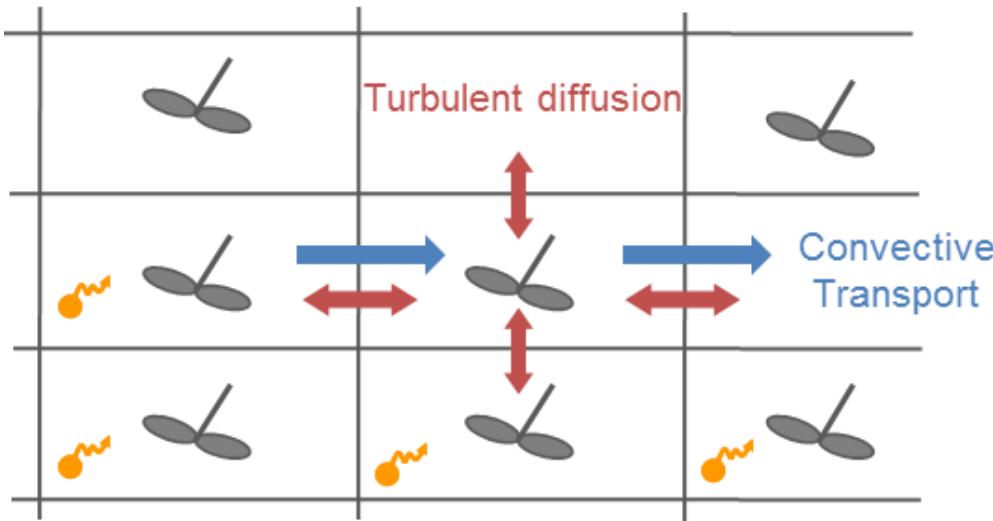
NO mass fraction fields



- ✓ In the first guesses, coarse meshes with a high level of clustering are adopted
- ✓ The calculations are then iteratively performed using a progressively increased number of cells up to convergence, i.e. without further grid sensitivity
- ✓ The NOx-Postprocessor typically reduces the number of the original grid-cells with a factor of ~10

The mass balance equations

36



Diffusion flux due to concentration gradients and velocity fluctuations of the turbulent flow

$$\vec{J}_i = -\frac{\mu_t}{Sc_t} \cdot \nabla \omega_i$$

$$\left[\sum_{n=1}^{Ns} W_n \omega_{i,n}^{out} - W \cdot \omega_i^{out} \right] + \sum_{n=1}^{Ns} J_{i,n} S_n + V^* \tilde{\Omega}_i + \Pi_i = 0$$

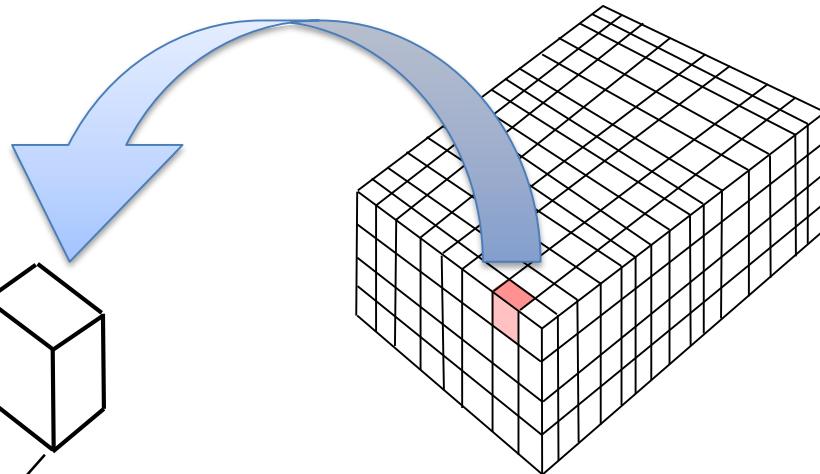
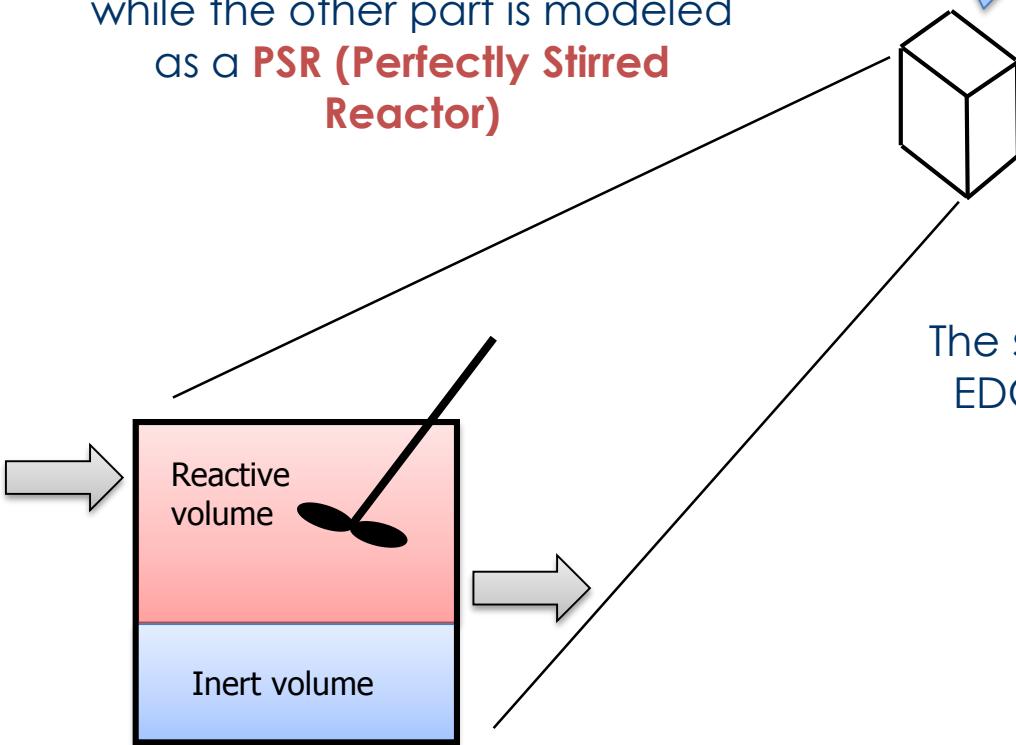
Diffusion
Convection Vaporization
Devolatilization
Chemical reactions

1. The CRECK Modeling Group @ Politecnico di Milano
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Effective volume of reaction

38

To account for the non perfect mixing, each equivalent reactor of the network can be split in two parts: one part is **inert** with respect to chemical reactions, while the other part is modeled as a **PSR (Perfectly Stirred Reactor)**



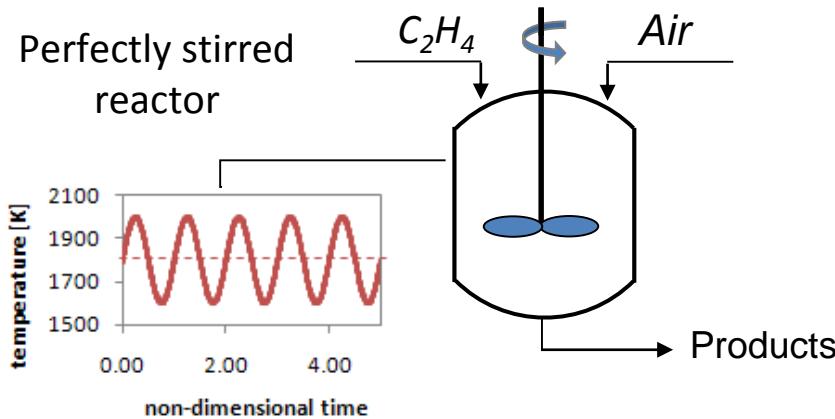
The splitting is estimated according to the EDC (Eddy Dissipation Concept) Model

$$V_{\text{reactor}} = V_{\text{reactive}} + V_{\text{inert}}$$

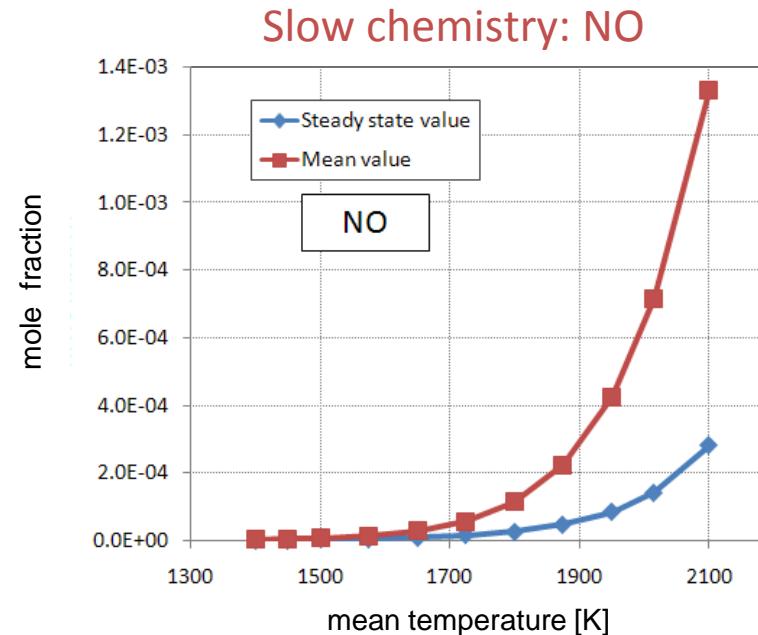
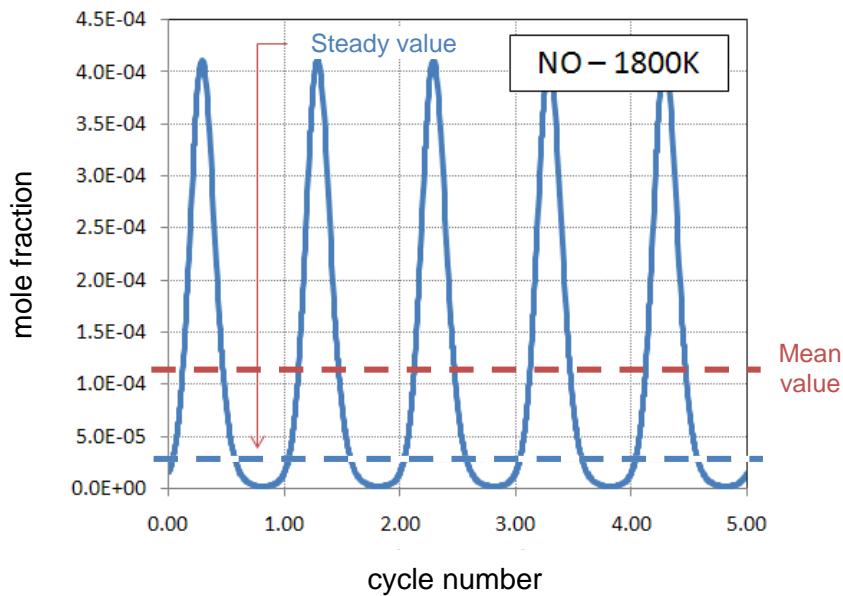
$$\frac{V_{\text{reactive}}}{V_{\text{reactor}}} = 2.13 \left(\frac{\nu \cdot \varepsilon}{k^2} \right)^{3/4}$$

Fluctuations of temperature and NOx

39



The fluctuations of temperature have a strong impact on the formation of NOx because of the high activation energy of the thermal path



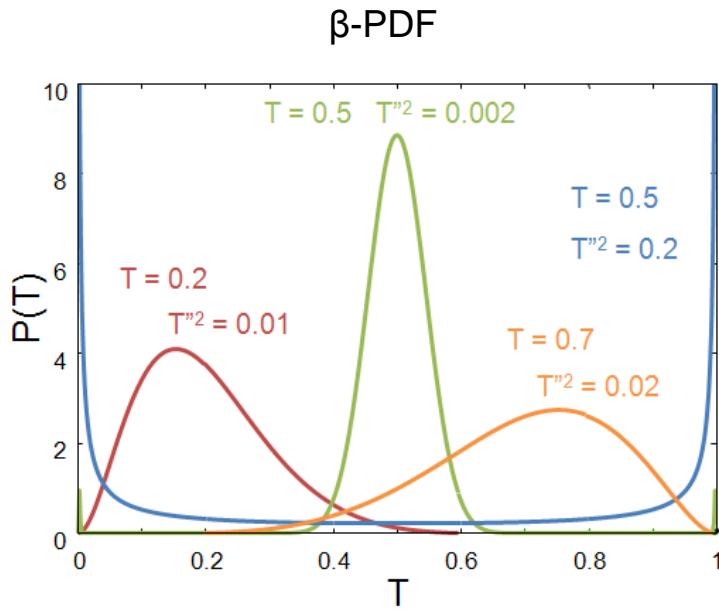
Correction coefficient for reaction rates (I)

40

Rate constant is highly **non linear** function of temperature

$$k(T) = A \cdot T^\beta \cdot \exp\left(-\frac{E_{att}}{RT}\right)$$

Requires the knowledge of the **variance of temperature**

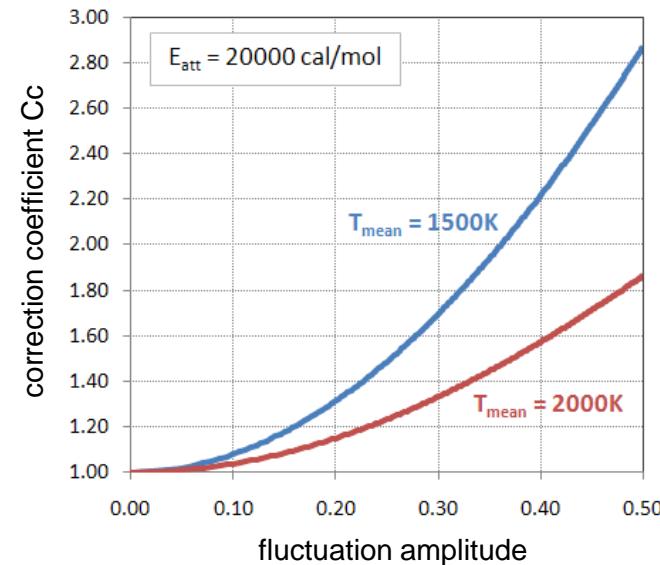


Introduction of a proper **probability distribution function** $p(T)$

$$\tilde{k}(T) = \int_{T_{min}}^{T_{max}} k(T) p(T) dT = C_C k(\tilde{T})$$

Correction coefficient

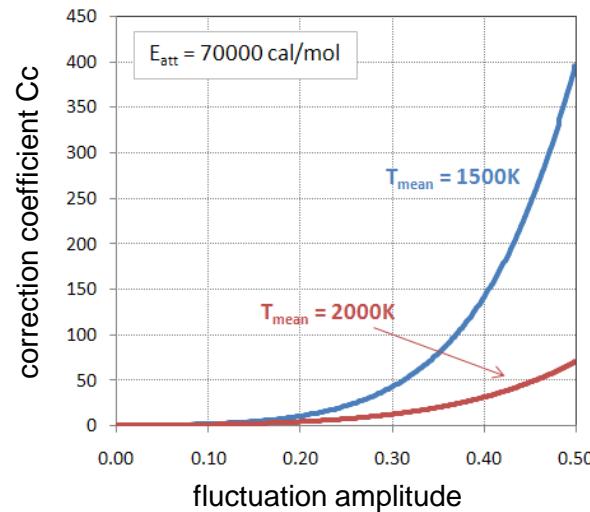
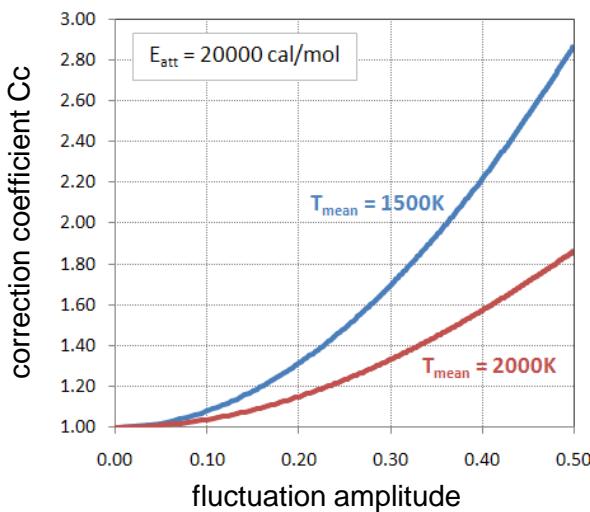
$$C_C = \frac{\int_{T_{min}}^{T_{max}} k(T) p(T) dT}{k(\tilde{T})}$$



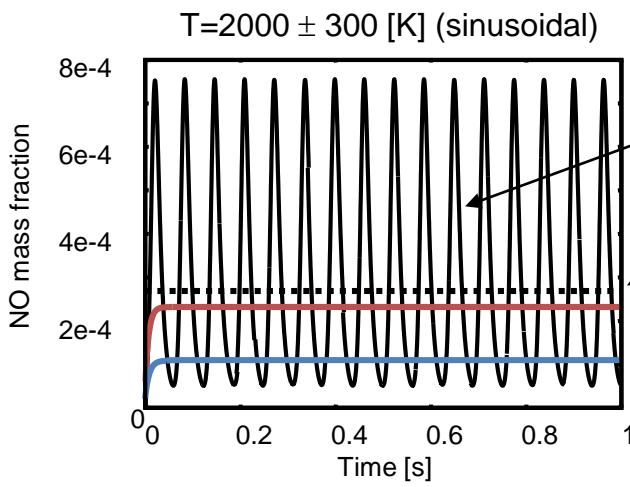
A. Cuoci, A. Frassoldati, G. Buzzi Ferraris, T. Faravelli, E. Ranzi,
International Journal of Hydrogen Energy (32), p. 3486-3500 (2007)

Correction coefficient for reaction rates (II)

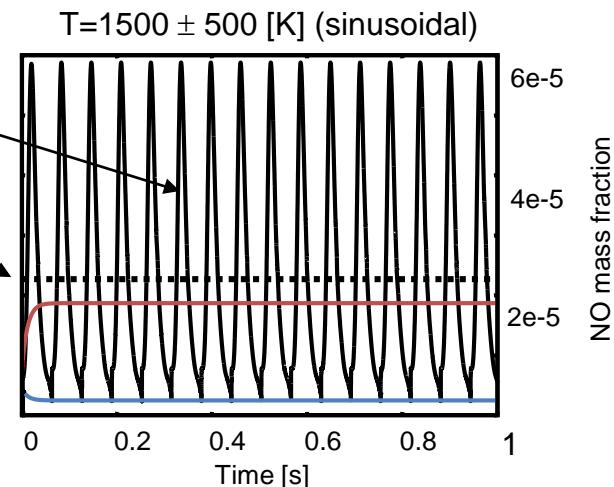
41



The correction Coefficient
is significantly > 1 for high
activation energies
(Thermal NOx)



$\Phi=0.95$ CH₄/Air
oscillating profile
mean value
Corrected: $k=k(T)*C_c$
Uncorrected: $k=k(T)$



The error (<15%) is due to the fluctuations of composition (neglected)

Calculation of correction coefficients

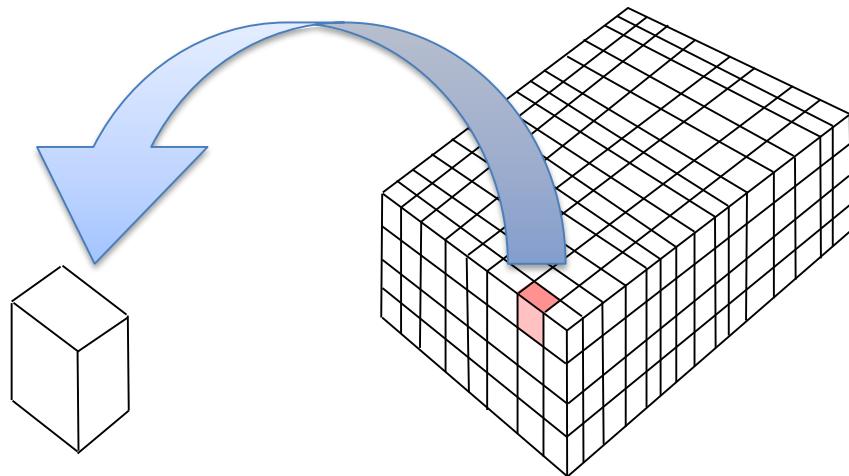
42

The correction coefficient must be calculated for each reaction in each reactor

$$C_C = \frac{\int_{T_{\min}}^{T_{\max}} k(T) p(T) dT}{k(\tilde{T})}$$

Tabulation of Correction Coefficients

Since during the post-processing phase the temperature is fixed in each reactor, the correction can be pre-calculated and stored in memory (i.e. it is always the same, since it is independent of the composition)



Transport equation for the variance of temperature

$$\frac{\partial}{\partial t} \left(\bar{\rho} T''^2 \right) + \nabla \left(\bar{\rho} \tilde{\mathbf{v}} T''^2 \right) = \nabla \left(\frac{\mu_T}{Sc_T} \nabla \tilde{T} \right) + 2 \frac{\mu_T}{Sc_T} \nabla \tilde{T} \nabla \tilde{T} - C_p \frac{\varepsilon}{\kappa} T''^2$$

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HYPOTHESIS

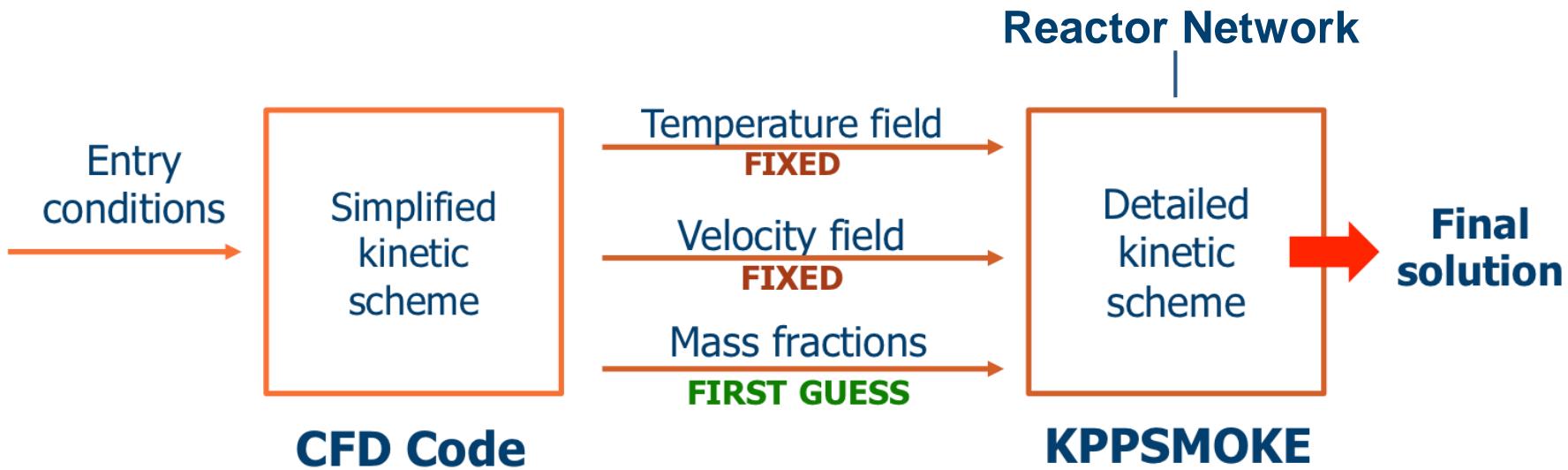
Negligible influence of minor species
on temperature and velocity fields



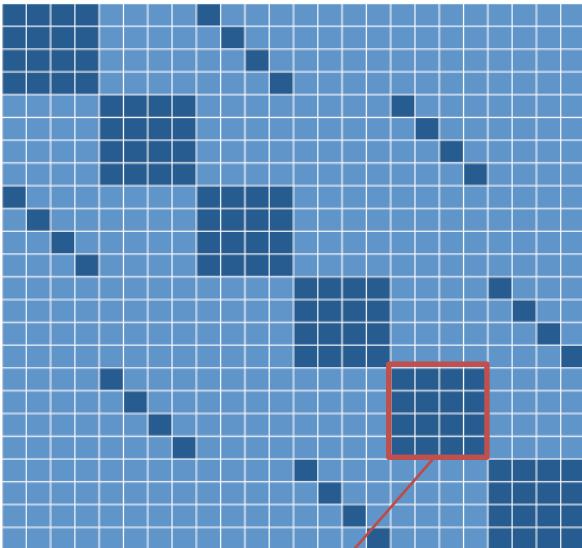
Skeletal kinetics to
assess CFD

Multi-technique
solution strategy

Only mass
balances are solved in CRN



Jacobian sparsity pattern



Single reactor

$$\left(\sum_{k=1}^{N_{AD}} \dot{m}_{k,j} \omega_{k,j,i} - \dot{m}_j \omega_{j,i} \right) + \sum_{k=1}^{N_{AD}} \left(J_{j,k,i} \cdot S_{j,k} \right) + V_j^* \tilde{\Omega}_{j,i} + \Pi_{j,i} = 0$$

↓
Linear

↓
 $J_i = -\frac{m_t}{Sc_t} \cdot \nabla W_i$
Linear

↓
Non Linear
(Power Law)

- Jacobian is **sparse** and **block-unstructured**
- High degree of **accuracy** is sought

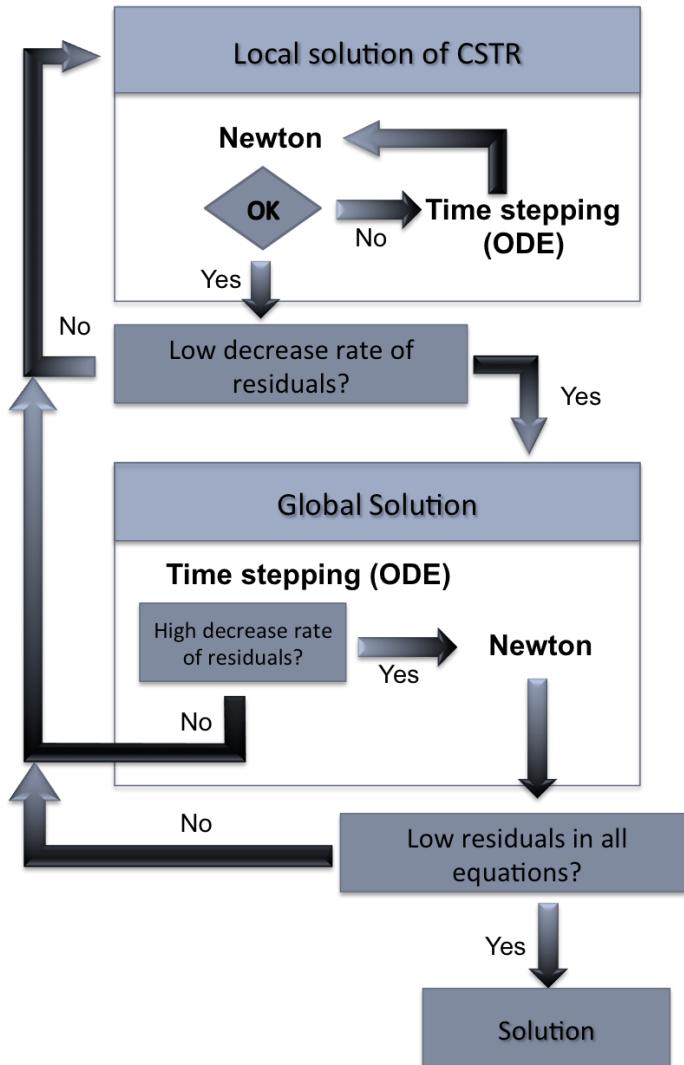
A **fully coupled** resolution is implemented

$$\mathbf{C}(\boldsymbol{\omega}) + \mathbf{R}(\boldsymbol{\omega}) + \mathbf{f} = \mathbf{0}$$

↓ ↓ ↓
Linear Non-Linear External feeds



Numerical procedure



the numerical procedure combines different techniques to obtain the final solution, because the global Newton's method (or modified Newton's methods) can be successfully applied only if the first-guess solution is close to the real solution.

Remember that the first-guess solution (from CFD) could account only for a few species, while the KPP solution for hundreds of species

1. Global Newton's Method
2. Global ODE (Backward Euler)
3. Direct Substitutions (Local solution)
 - a. Local Newton's Method
 - b. Local ODE system (stiff solver)

The individual reactors are solved sequentially to take the whole system closer to the solution. This means that each reactor is solved using a **local Newton's method**.

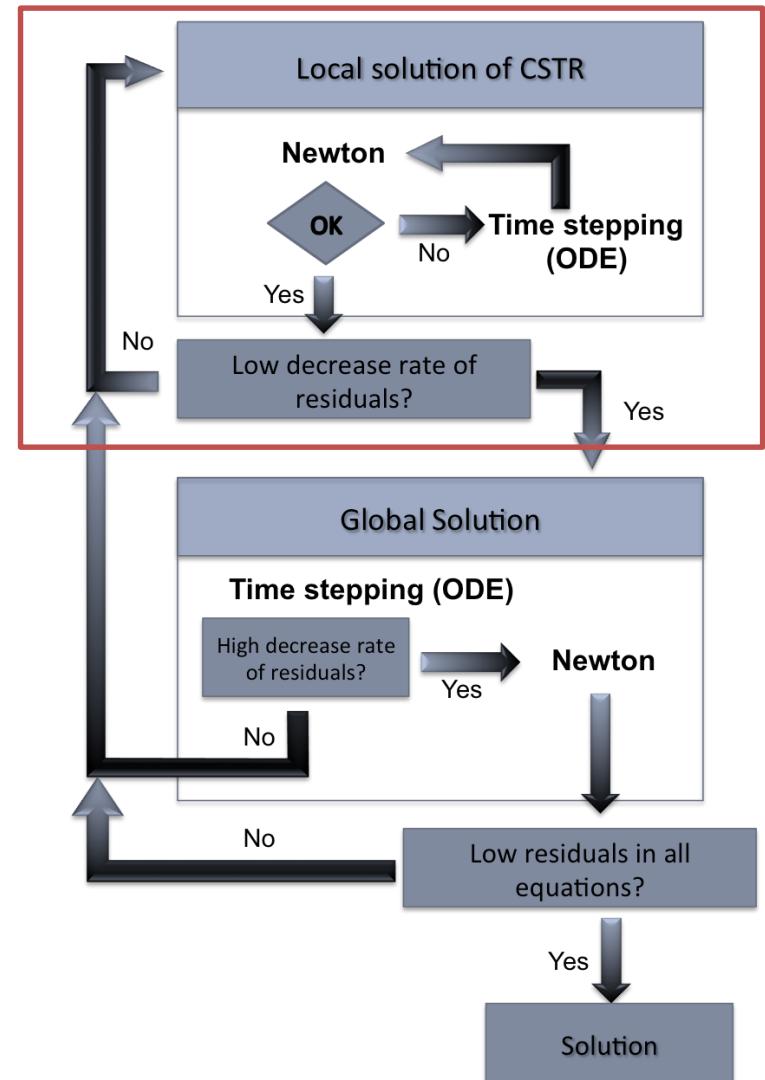
$$[\mathbf{C}_{in}(\omega) + \mathbf{f}]_{old} + \mathbf{C}_{out}(\omega) + \mathbf{R}(\omega) = \mathbf{0}$$

To improve the robustness, especially in the first iteration, a **false transient method** is used to solve the single reactors. The NLS is transformed into a ODE system by adding the unsteady term

$$\mathbf{m} \frac{d\omega}{dt} = [\mathbf{C}_{in}(\omega) + \mathbf{f}]_{old} + \mathbf{C}_{out}(\omega) + \mathbf{R}(\omega)$$

Stiff ODE solvers

CVODE, DVODE, LSODE, RADAU5, BzzMath



the **global Newton's method**, to ensure the accuracy needed to correctly predict chemical species present in very small amounts (ppm or smaller)

$$\mathbf{C}(\boldsymbol{\omega}) + \mathbf{R}(\boldsymbol{\omega}) + \mathbf{f} = \mathbf{0}$$

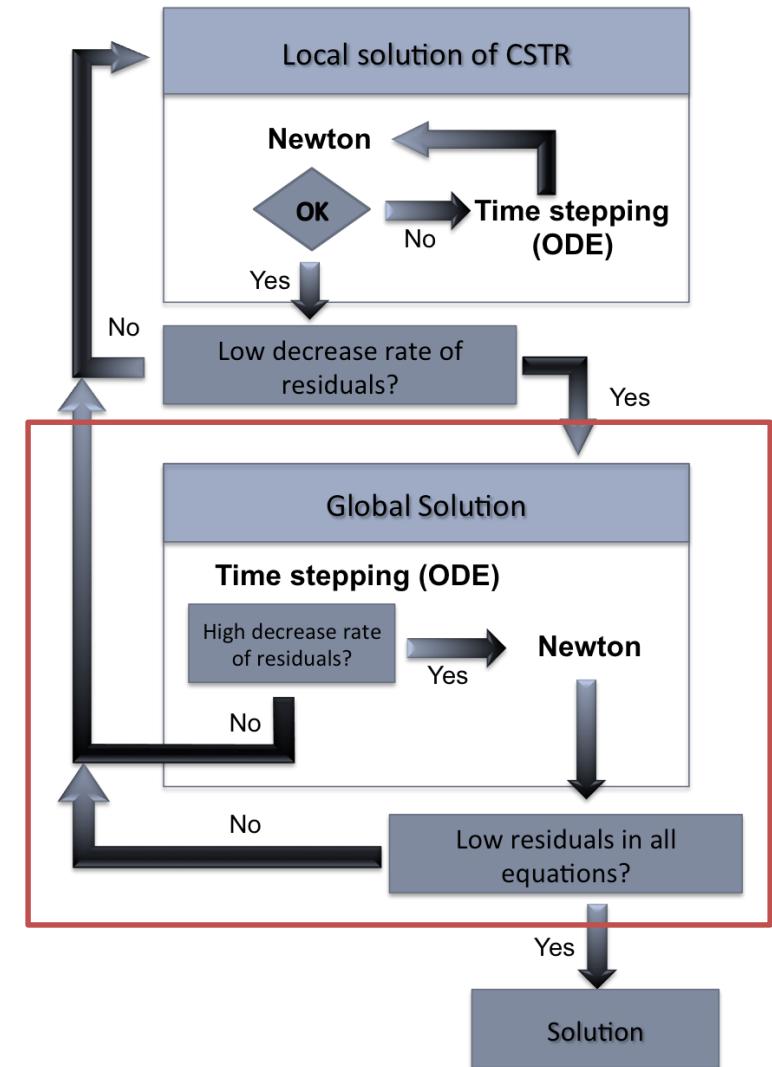
When complex flows are investigated, the sequential approach (i.e., direct substitutions) could not be enough to reduce the residuals of equations to sufficiently small values to successfully apply the global Newton's method. In such a case, a **global time-stepping** procedure must be taken into account.

$$\mathbf{m}_{tot} \frac{\boldsymbol{\omega}^{n+1} - \boldsymbol{\omega}^n}{\Delta t} = \mathbf{C}(\boldsymbol{\omega}^{n+1}) + \mathbf{R}(\boldsymbol{\omega}^{n+1}) + \mathbf{f}$$

Linear System solvers

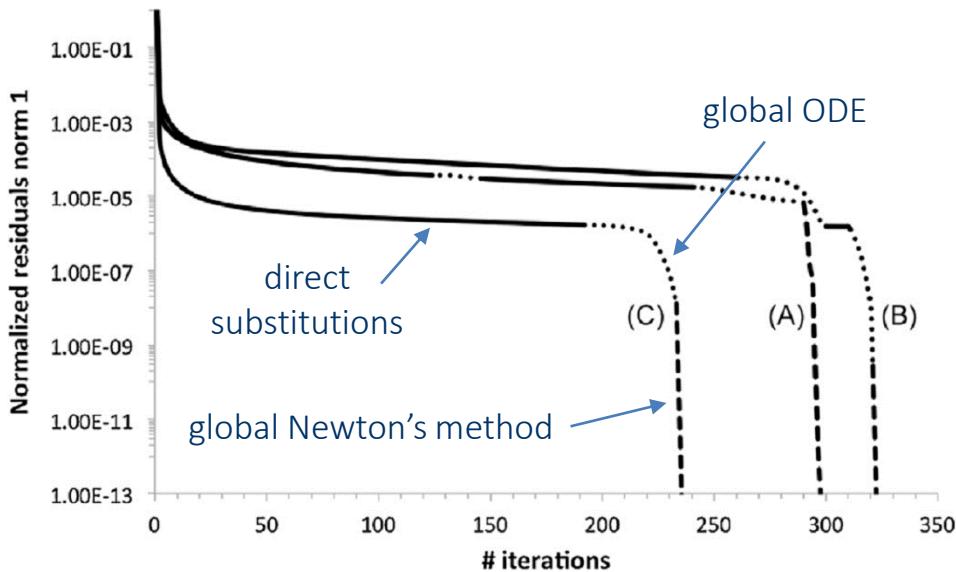
MUMPS 4.10 (Direct Solver)

LIS 1.24 (Iterative Solver)



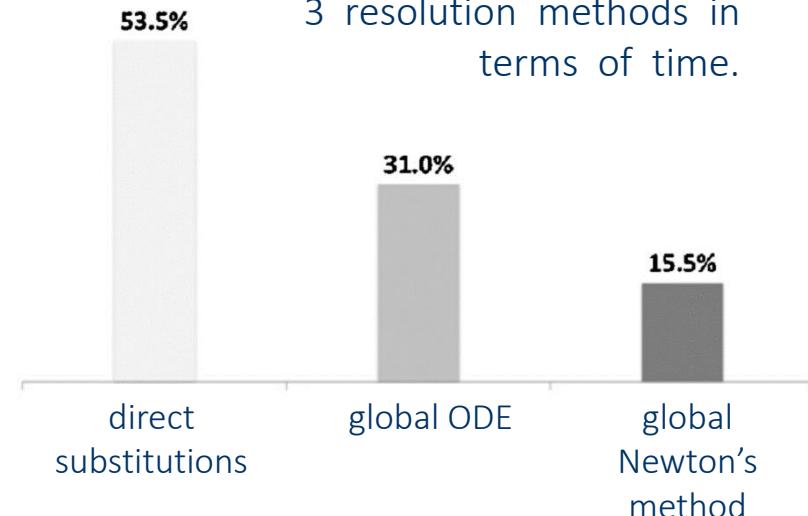
Numerical performances

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Residuals norm 1 trends, normalized with respect to their initial value (set equal to 1)

Relative importance of the 3 resolution methods in terms of time.



- A: a tubular combustor (56,150 reactors, 4.8M equations)
- B: an aircraft combustor (252,885 reactors, 22M equations)
- C: an aircraft combustor (290,764 reactors, 25M equations)

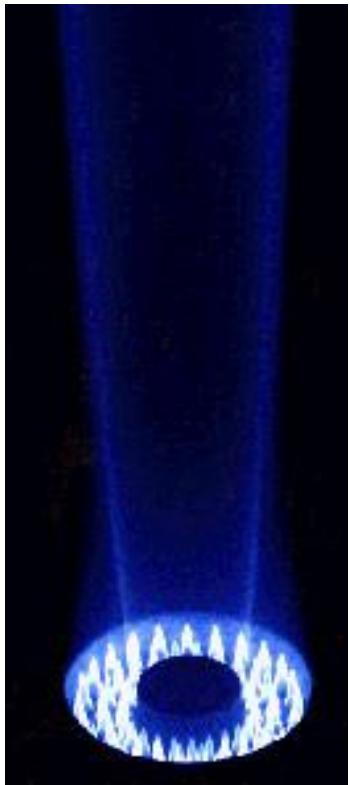
POLIMI NC7 kinetic mechanism
86 species and 1427 reactions

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6. Conclusions



Validation: Sandia Flame D

51



Barlow, R. S. and Frank, J. H., *Proc. Combust. Inst.* 27:1087-1095 (1998)

Nozzle diameter = 7.2mm

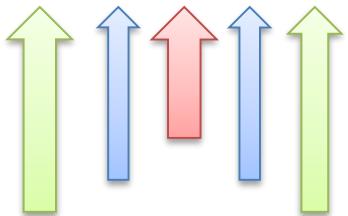
Pilot diameter = 18.2mm

Re = 22,400

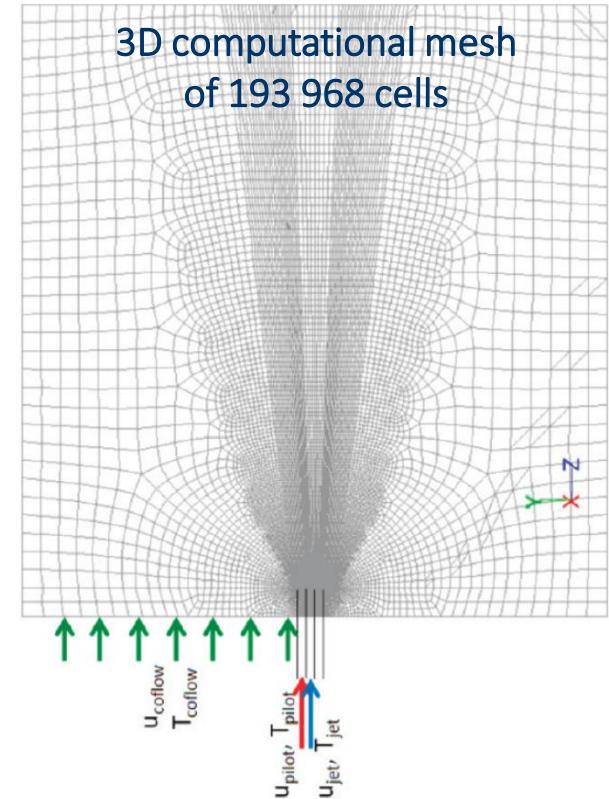
Fuel: 25% CH₄ + 75% Air (vol.)

Pilot: equilibrium composition
of a mixture of CH₄/air
($\Phi=0.77$)

Oxidizer: air



Monaghan, R.F.D., et al., Detailed multi-dimensional study of pollutant formation in a methane diffusion flame (2012) *Energy and Fuels*, 26 (3), pp. 1598-1611, DOI: 10.1021/ef201853k

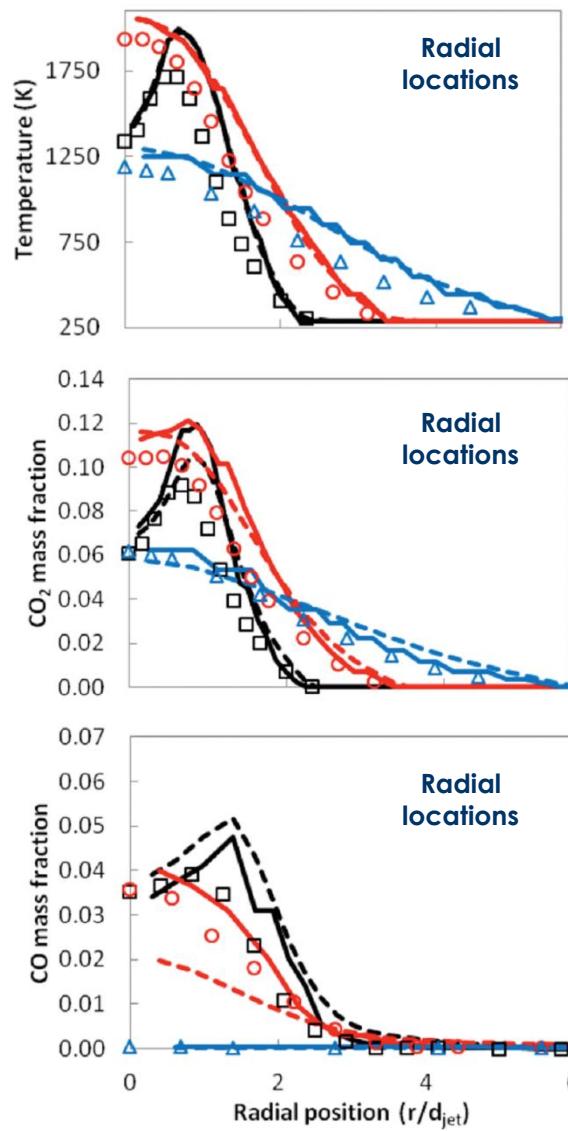
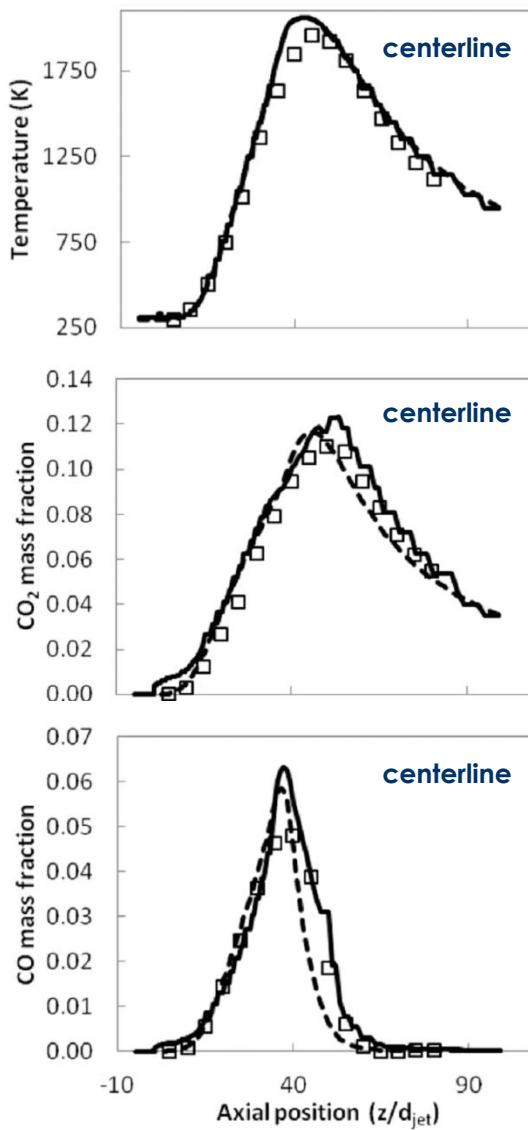


RANS Simulations performed
using the DRM22 kinetic scheme:

- 22 species
- 104 reactions

CFD results vs KPP results

52



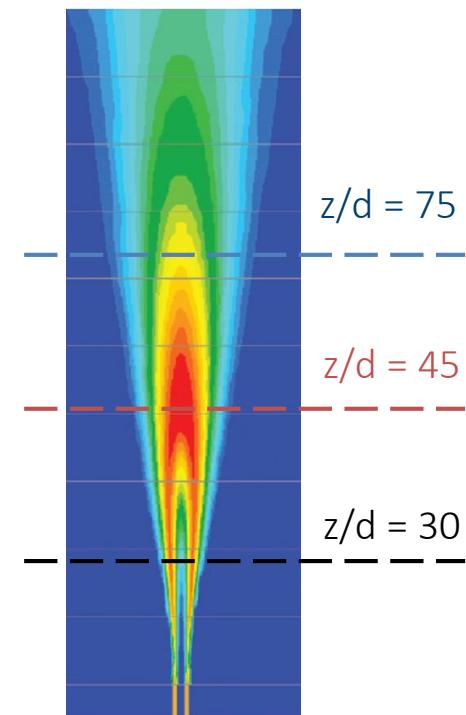
Continuous lines: KPP predictions

Dashed lines: CFD predictions

1114 Reactors

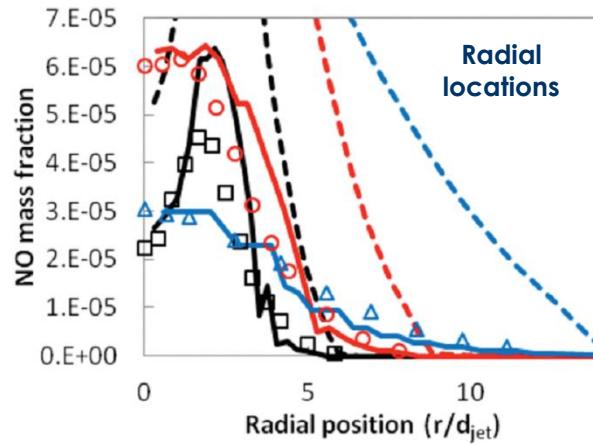
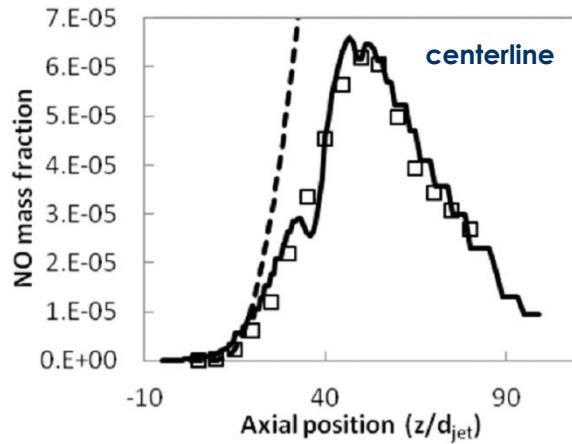
(less than 1% of the original cells)

103 species and 582 reactions



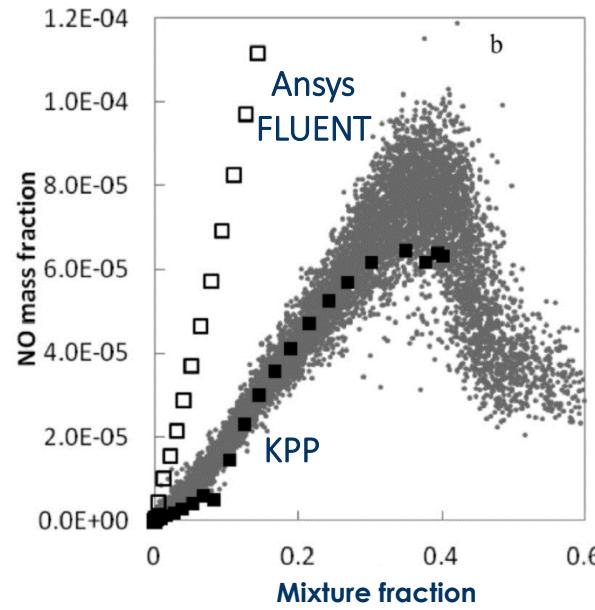
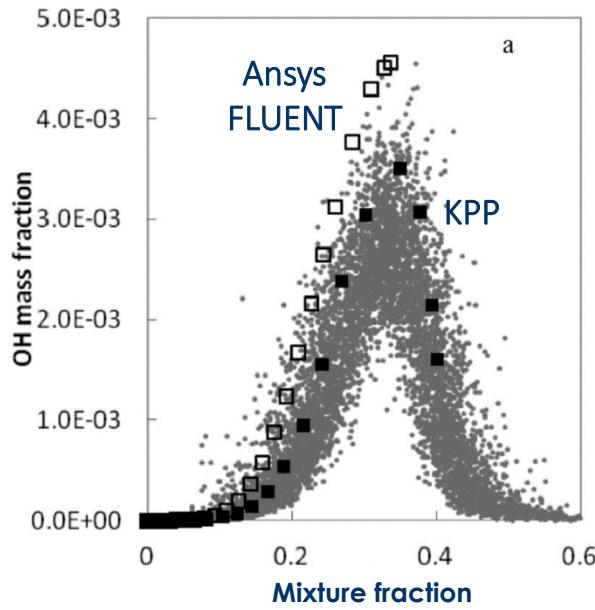
NOx predictions

53



Continuous lines: KPP predictions

Dashed lines: Ansys FLUENT NOX post-processor



The Ansys FLUENT NOx post-processor has the following configuration:

- ✓ thermal, prompt, and N₂O pathways activated
- ✓ instantaneous thermal [O] and [OH] models, quasi-steady N₂O model
- ✓ temperature-only β -PDF turbulence interaction with 10 PDF points
- ✓ temperature variance with a global maximum temperature.

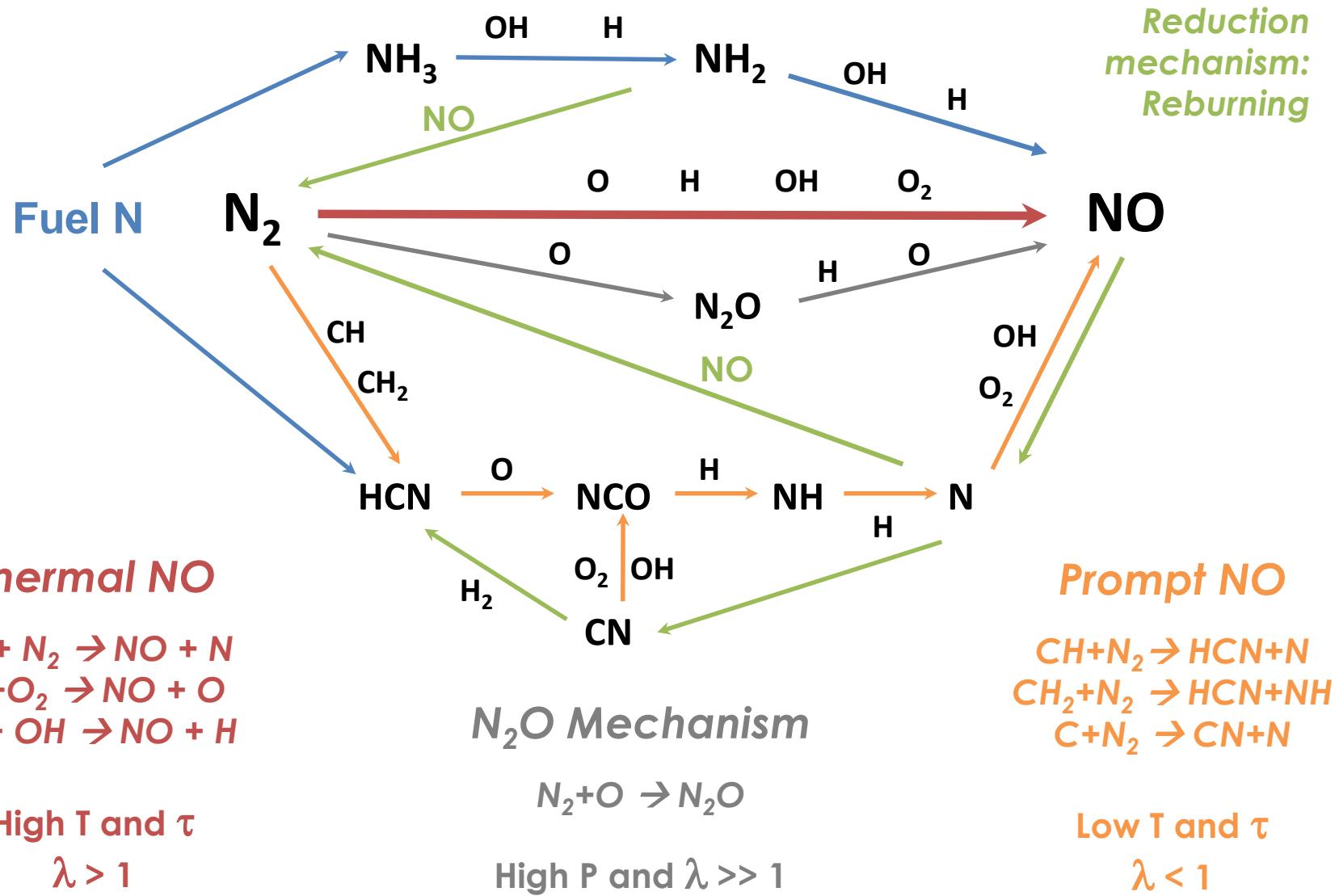


Numerical performances

CRN size	mechanism	time to solution (h:min:s)			improvement factor	NUIG C2
		CHEMKIN PRO	KPP			
108 PSRs	GRI 1.2	0:14:20	0:00:06		143	
108 PSRs	GRI 3.0	0:25:11	0:00:30		50	
108 PSRs	NUIG C2	failed	0:00:39			GRI 3.0
211 PSRs	GRI 1.2	0:23:45	0:00:16		89	53 species
211 PSRs	NUIG C2	failed	0:00:26			325 reactions
255 PSRs	GRI 1.2	1:57:48	0:00:16		442	
255 PSRs	NUIG C2	failed	0:01:28			
372 PSRs	NUIG C2	failed	0:01:48			GRI 1.2
411 PSRs	NUIG C2	failed	0:02:04			32 species
523 PSRs	NUIG C2	failed	0:02:26			279 reactions
617 PSRs	NUIG C2	failed	0:02:38			
722 PSRs	NUIG C2	failed	0:03:20			
809 PSRs	NUIG C2	failed	0:03:50			
1114 PSRs	NUIG C2	failed	0:09:30			

NOx formation pathways (I)

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- Thermal NOx (Zeldovich)



- Direct N₂ oxidation.
 - High temperature required (> 1800 K). **Highly temperature dependent**

- Prompt NOx (Fenimore)



- N≡N bond scission by fuel radicals (CH+N₂=HCN+N).
 - Occurs in flame fronts. Not significantly temperature dependent

- N₂O Pathway



- Through N₂+ O + M → N₂O + M.
 - Relevant under elevated pressures and lean combustion (gas turbines)

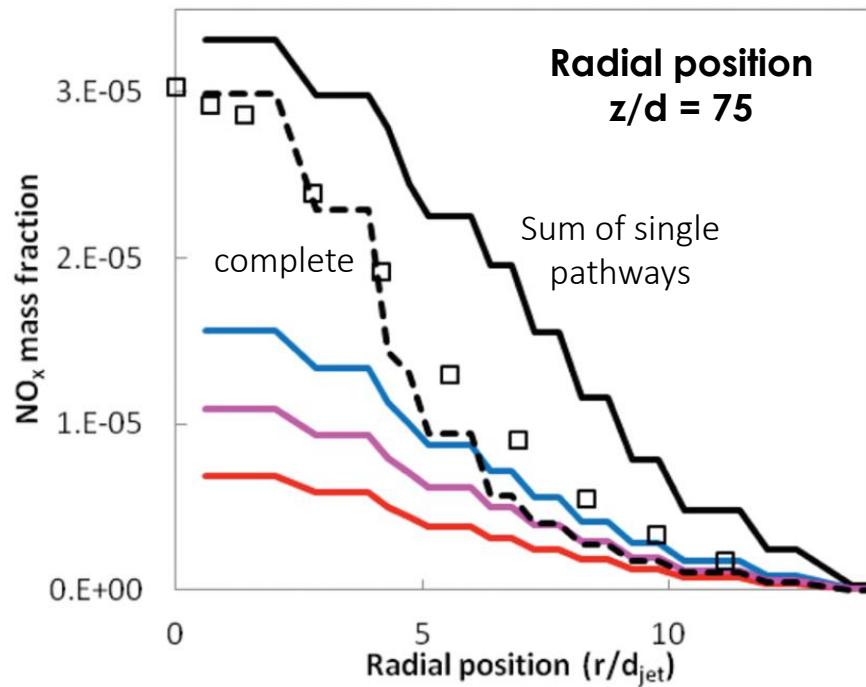
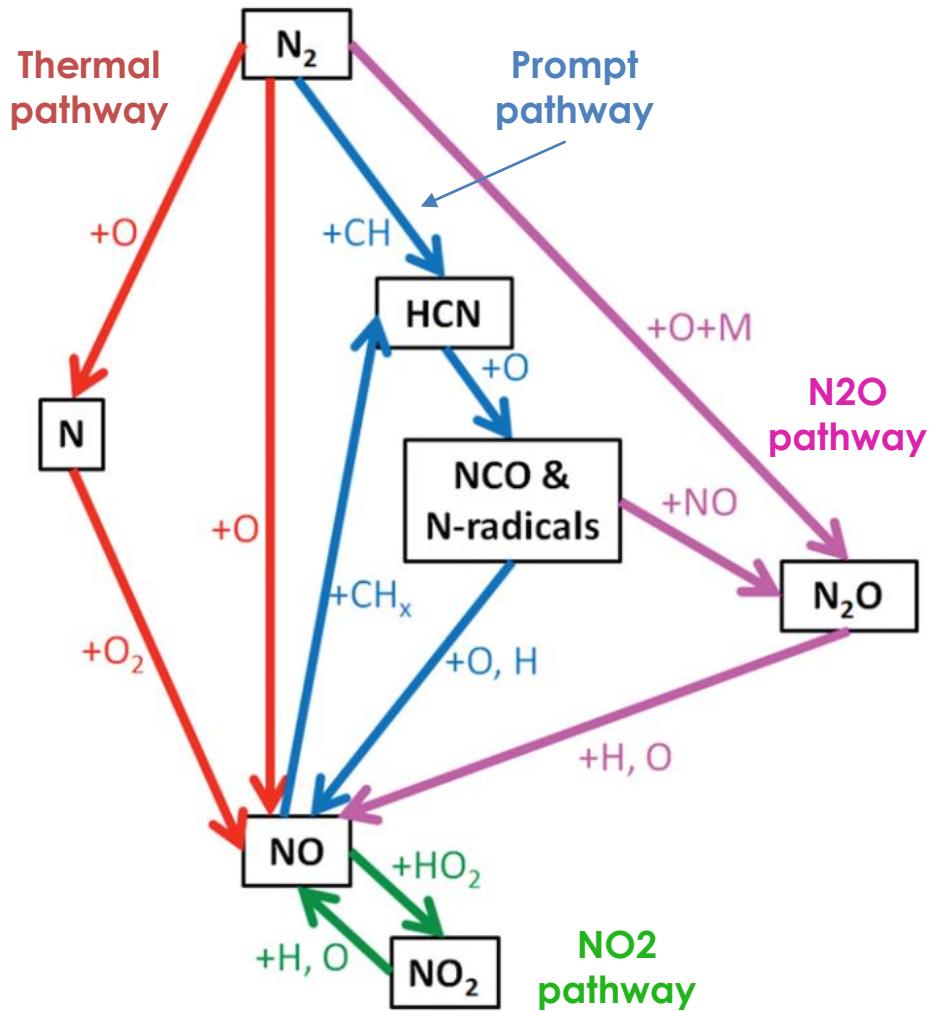
- Fuel NOx



- NO formation from N-containing fuel fragments (CN, NH).
 - Relevant if fuel contains chemically-bound nitrogen.

NOx Pathway Analysis

57

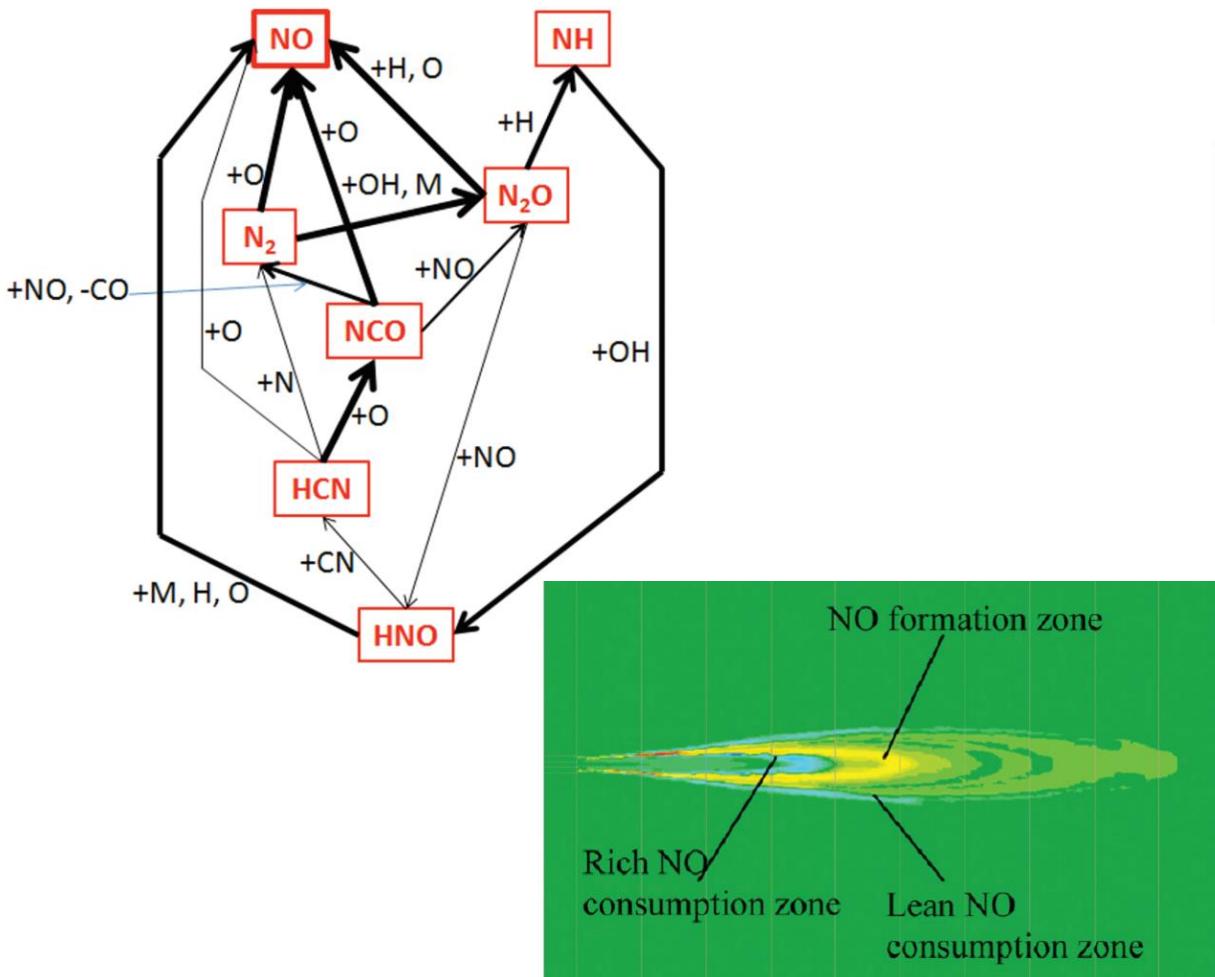


Of the total NO_x produced by the Sandia D flame, 47% is due to the prompt pathway, 32% is due to the N₂O pathway, and 21% is due to the thermal pathway.

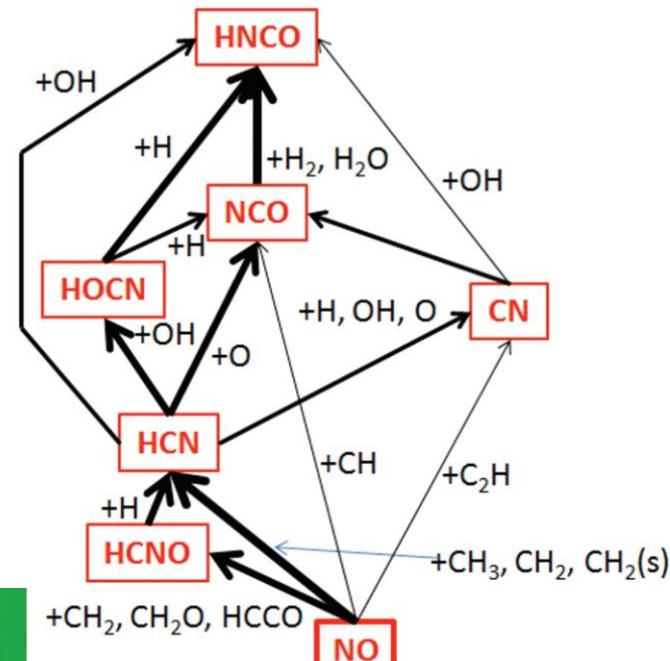
Reaction channels

58

Important reaction channels for NO production
in the high-temperature flame brush.



Important reaction channels for NO consumption in the fuel-rich region.



Rates of
production of NO

Validation: Sandia Syngas Flames

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CO / H₂ / N₂ Jet Flames¹

¹ Barlow, R.S., et al., *Sandia/ETH-Zurich CO/H₂/N₂ Flame Data - Release 1.1*. www.ca.sandia.gov/TNF, Sandia National Laboratories, 2002

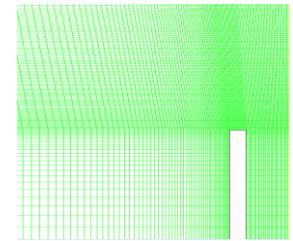
Unconfined turbulent jet flame in low-velocity coflow

Fuel composition:

40% CO, 30% H₂, 30% N₂

Fuel inlet velocity: ~ 45-76 m/s

Computational domain



Non uniform, structured mesh

About 42,000 cells (320x130)

High resolution in the region close to the inlets

CFD Simulation details

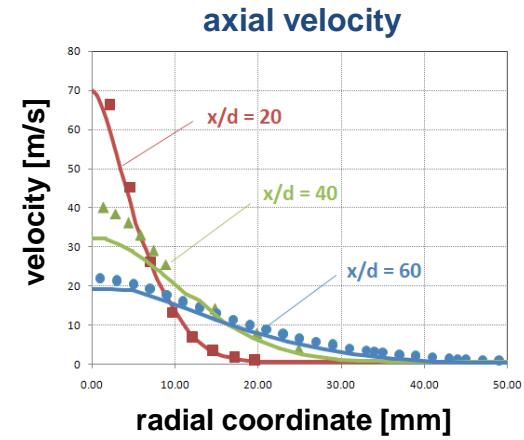
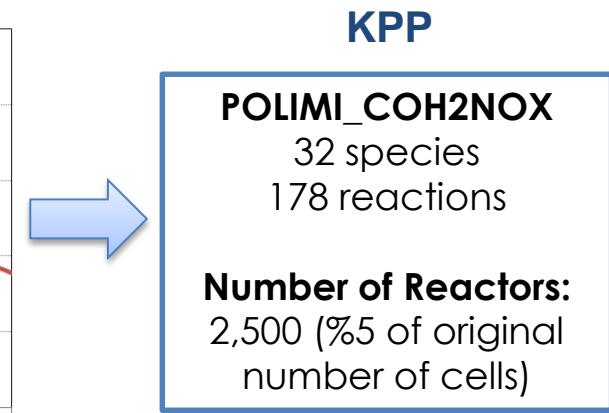
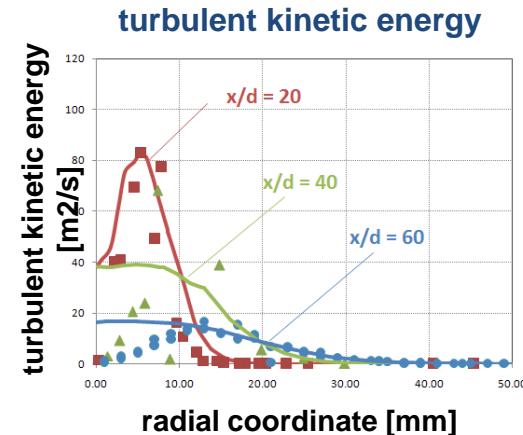
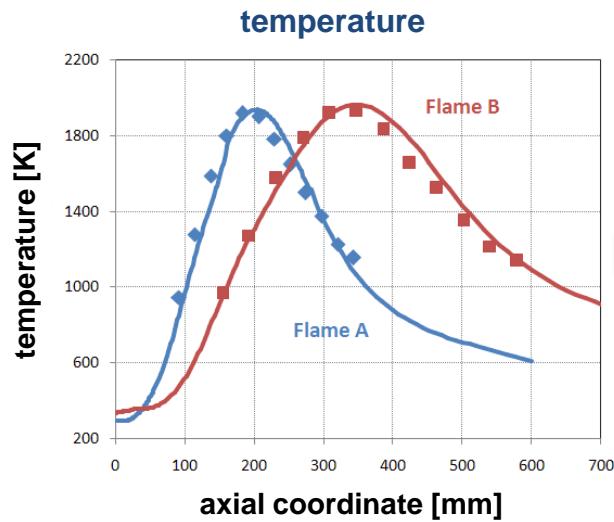
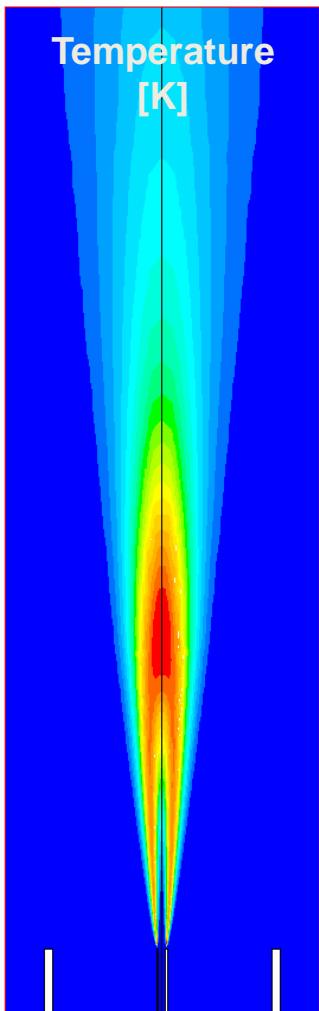
CFD Code	FLUENT 6.3.2
Space	2D Axial-Symmetric
Time	Steady
Turbulence modeling	Standard κ - ϵ turbulence model
Wall treatment	Standard wall functions
Radiation	Discrete Ordinate Model
Solver	Segregated implicit solver

Spatial resolution	Second-Order Upwind scheme
Pressure Interpolation	PRESTO!
Combustion model	Eddy Dissipation Concept (EDC)

POLIMI_COH2 kinetic scheme
13 species
37 reactions

Validation: Sandia Syngas Flames

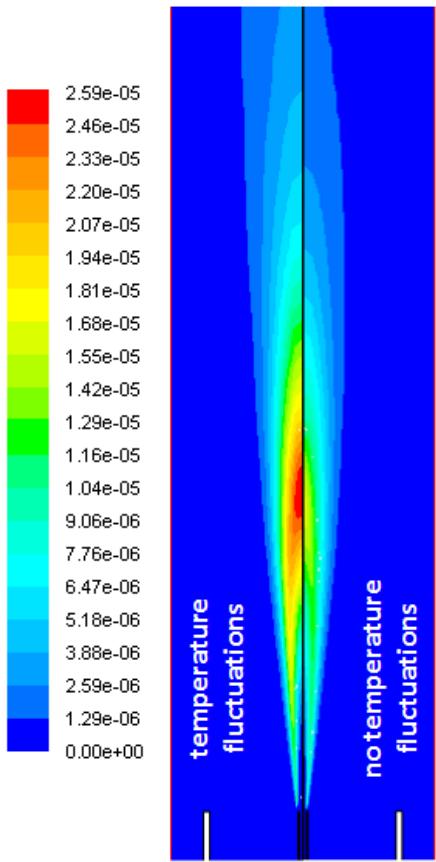
60



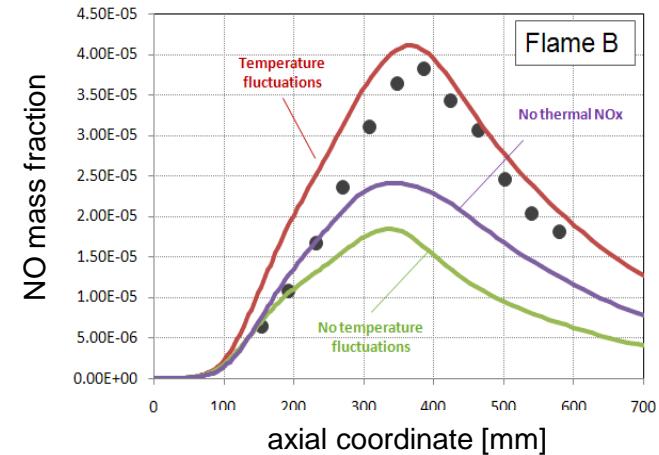
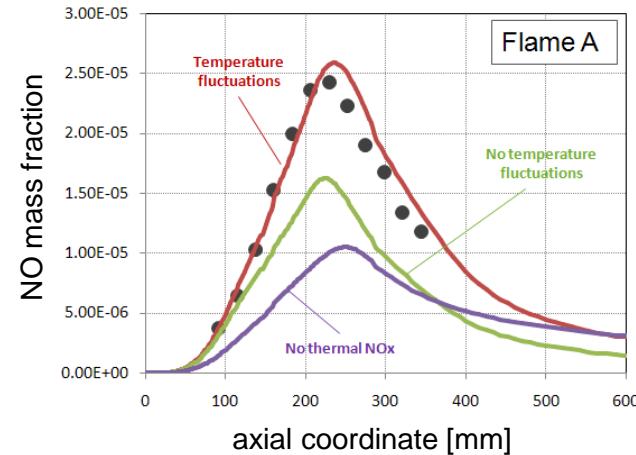
Validation: Sandia Syngas Flames

61

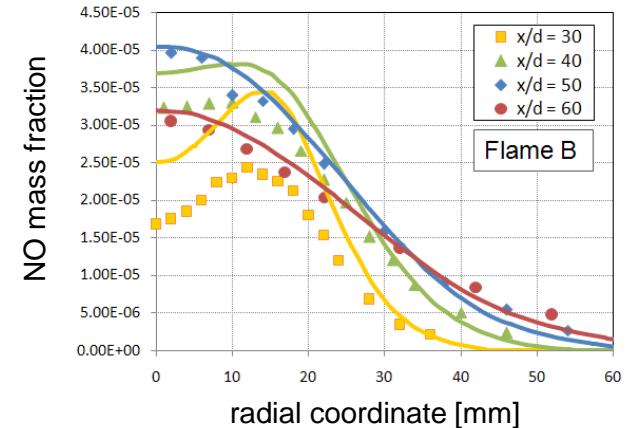
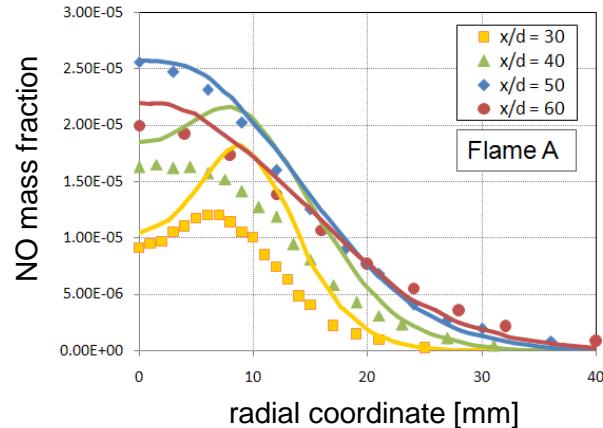
NO mass fraction



Axial profiles



Radial profiles



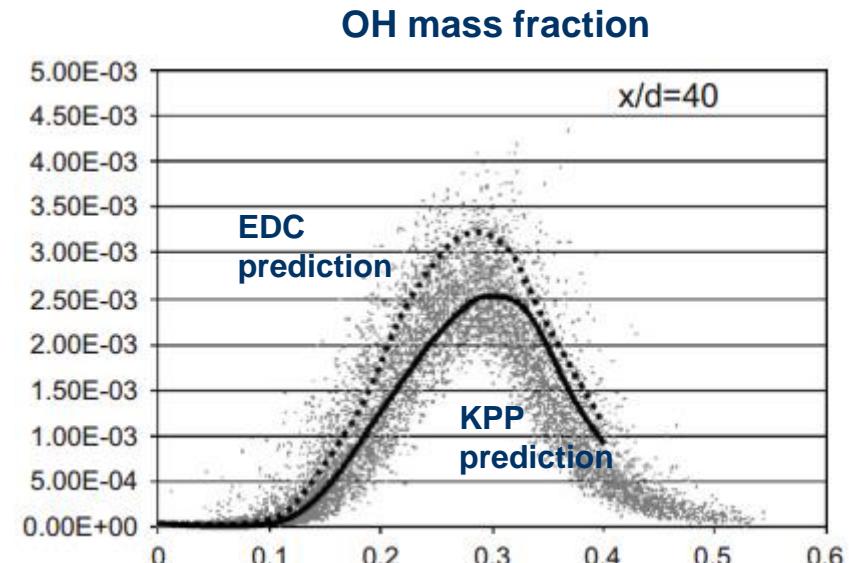
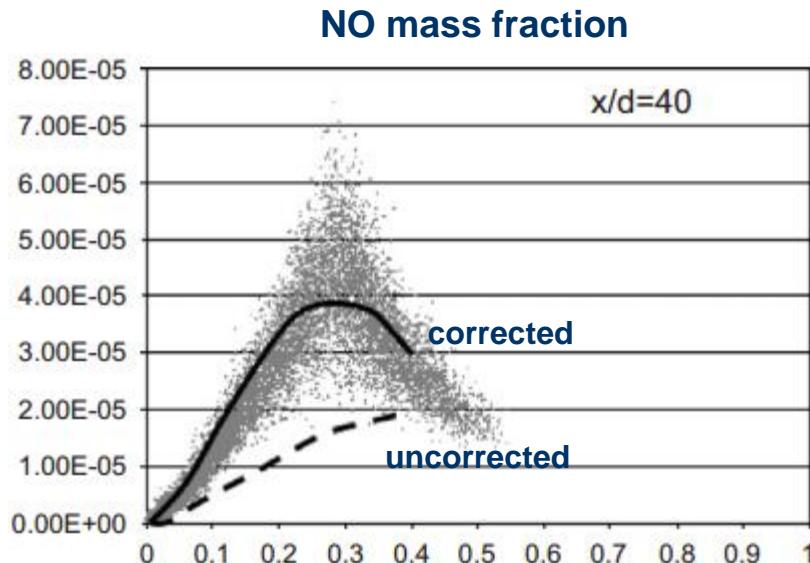
Barlow, R.S., et al., Sandia/ETH-Zurich CO/H₂/N₂ Flame Data - Release 1.1. www.ca.sandia.gov/TNF, Sandia National Laboratories, 2002

Validation: Sandia Syngas Flames

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NO and OH mass fraction for Flame B

Comparison between single shot measurements (symbols) and numerical simulations (lines)



Validation: NH₃-Doped Jet Flame

63

CO / H₂ / N₂ Jet Flame

Drake, M.C., et al., *Nitric oxide formation from thermal and fuel-bound nitrogen sources in a turbulent nonpremixed syngas flame*.

Twentieth Symposium (International) on Combustion - The Combustion Institute, 1984: p. 1983-1990.

Unconfined turbulent jet flame in low-velocity coflow

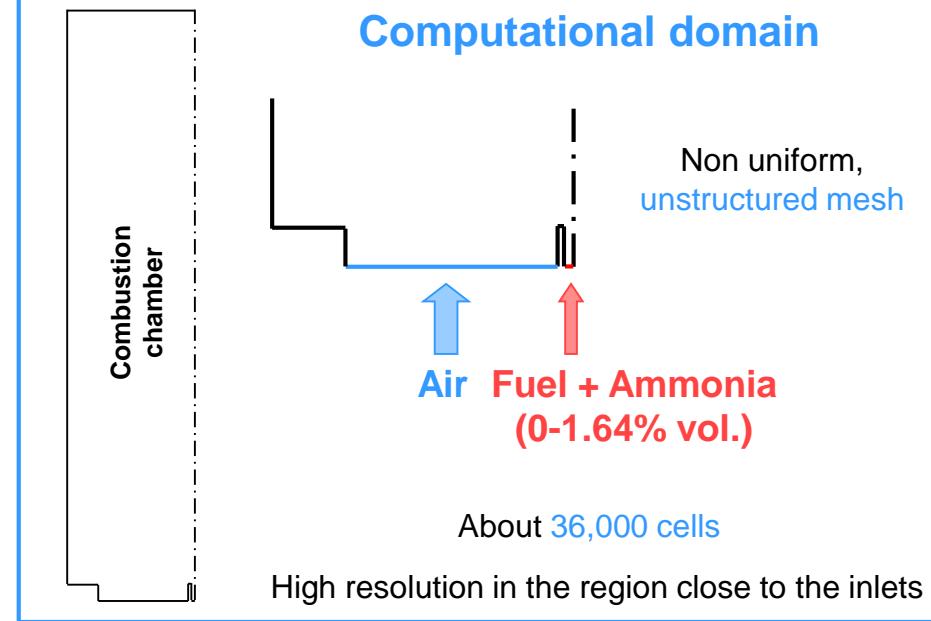
Fuel composition:

40% CO, 30% H₂, 30% N₂

Fuel inlet velocity: ~ 54 m/s

Small amounts of **ammonia** added to the fuel

Computational domain



CFD Simulation details

CFD Code	FLUENT 6.2
Space	2D Axial-Symmetric
Time	Steady
Turbulence modeling	Standard $\kappa-\epsilon$ turbulence model
Wall treatment	Standard wall functions
Radiation	Discrete Ordinate Model
Solver	Segregated implicit solver

Spatial resolution	Second-Order Upwind scheme
Pressure Interpolation	PRESTO!
Combustion Model	Eddy Dissipation Concept

POLIMI_COH2 kinetic scheme
13 species
37 reactions

Validation: NH₃-Doped Jet Flame

64

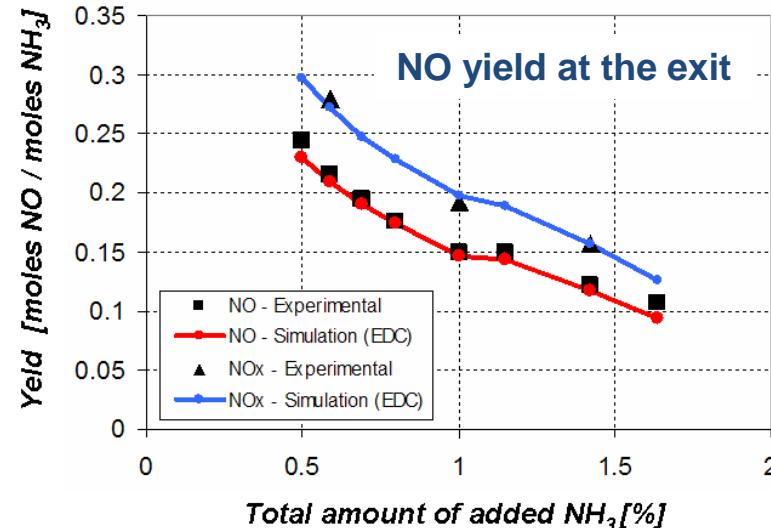
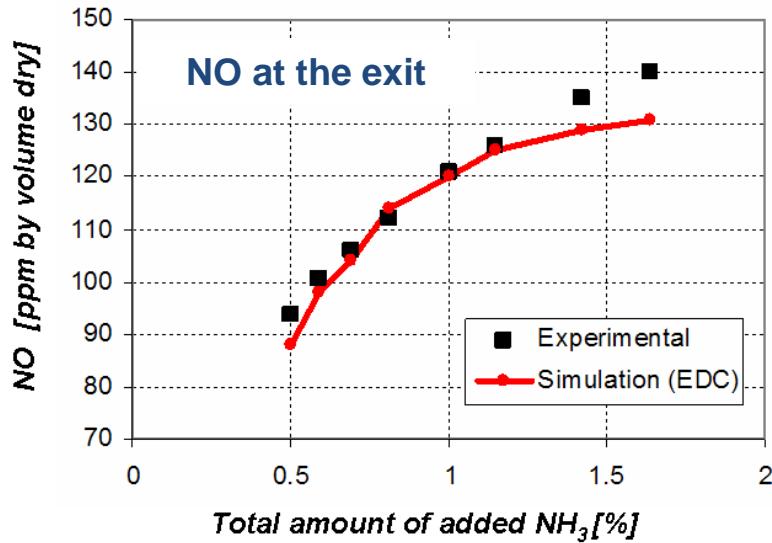
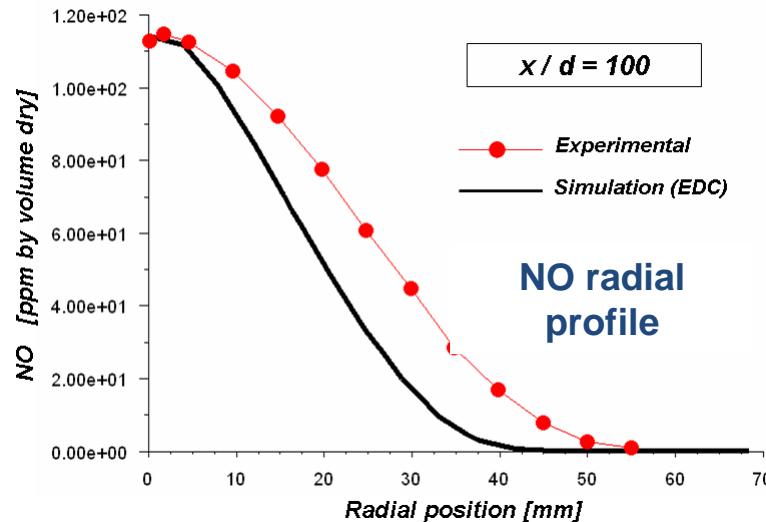
KPP

POLIMI_COH2NOX

32 species

178 reactions

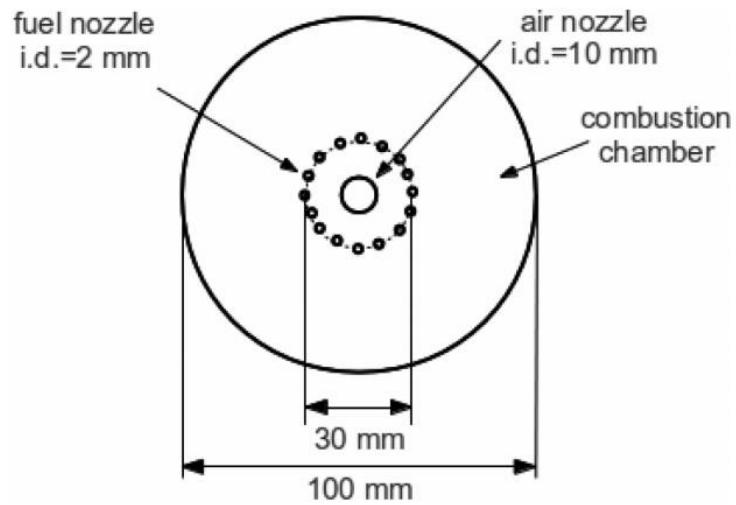
Number of Reactors:
2,000 (%5 of original
number of cells)



Small-scale MILD Combustor

65

Verissimo, A.; Rocha, A.; Costa, M. *Operational, combustion, and emission characteristics of a small-scale combustor*, Energy Fuels 2011, 25(6), 2469–2480.



Combustion chamber
quartz glass cylinder
internal diameter of 100 mm and length of 340 mm.

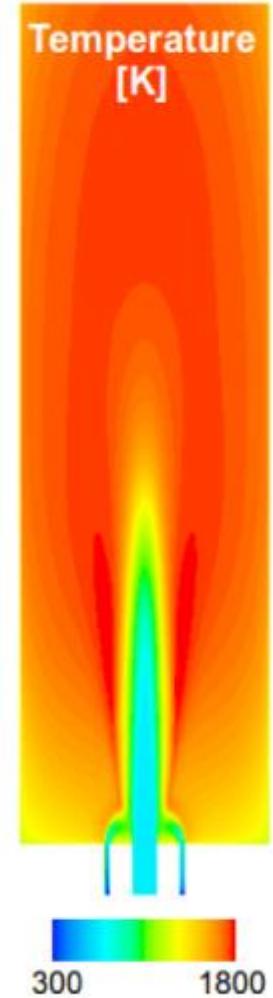
Fuel: CH₄ @ 300K supplied from 16 small orifices ($\Phi=2\text{mm}$)

Oxidizer: air @ 673K supplied from a central nozzle ($\Phi=10\text{mm}$)

3D Computational Mesh
100,000 cells

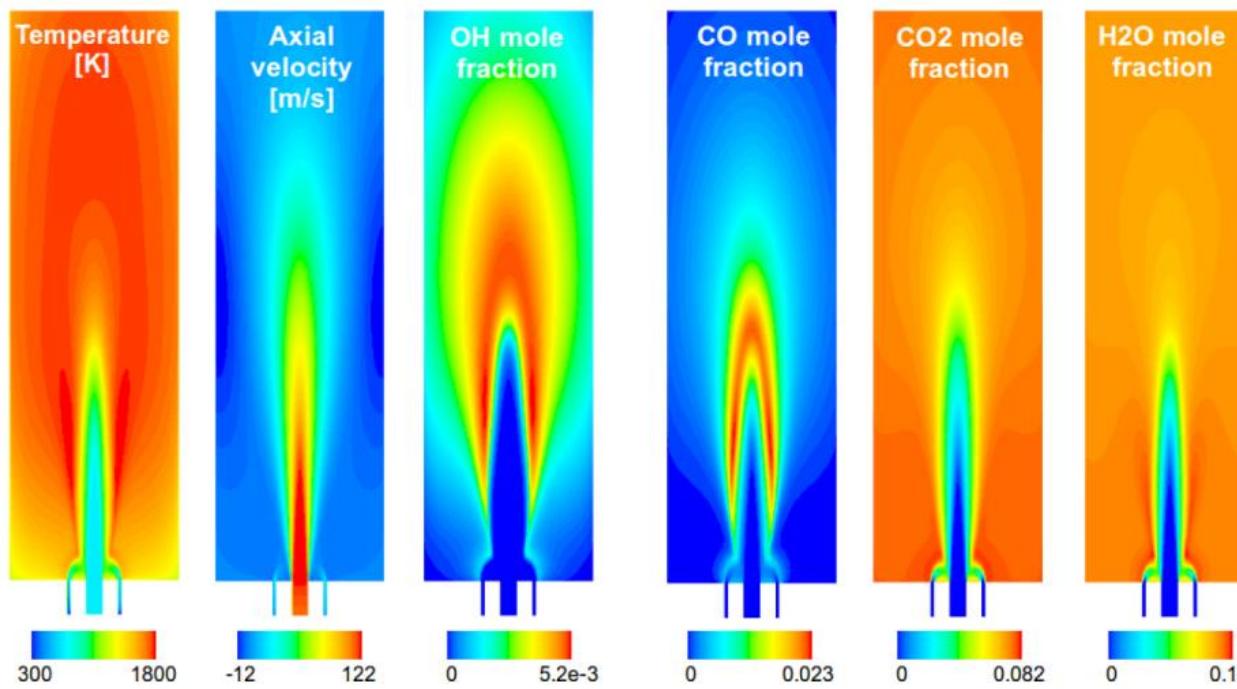
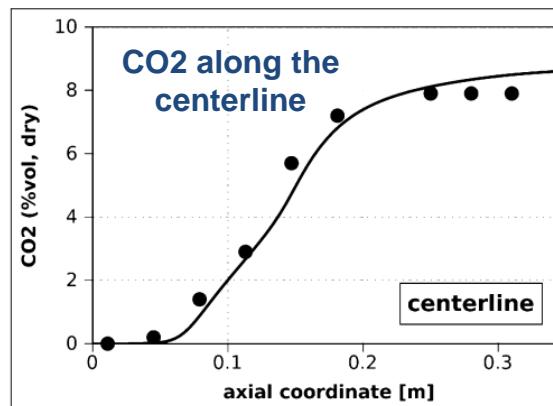
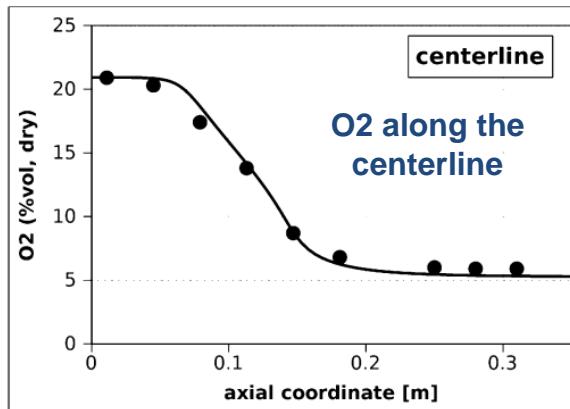
RANS Simulation
K-e turbulent model
Eddy Dissipation Model

Kinetic Scheme
DRM22 (22 species, 111 reactions)

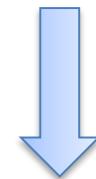


Small-scale MILD Combustor

66



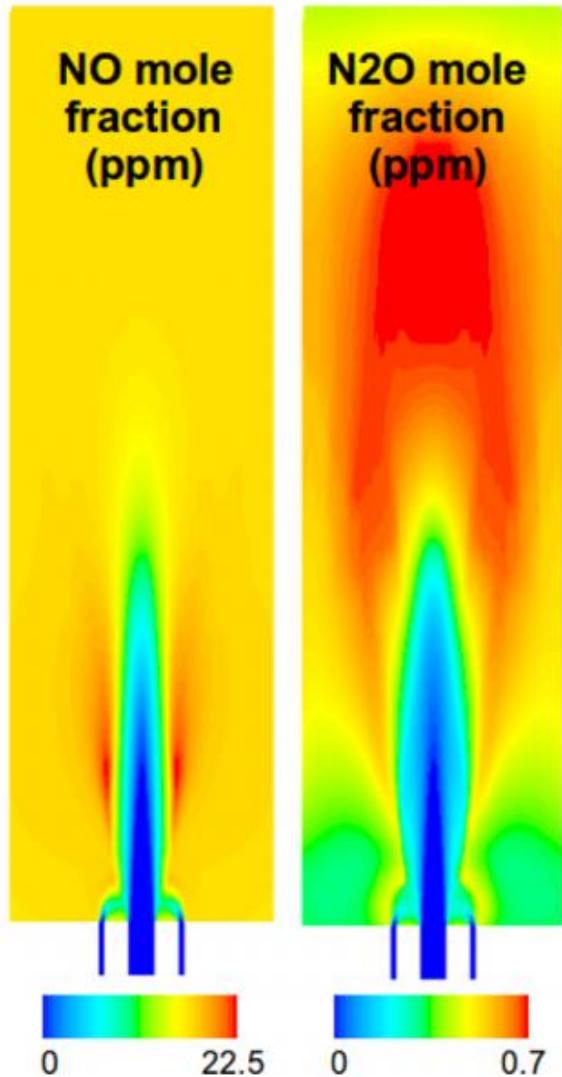
Kinetic Post Processing



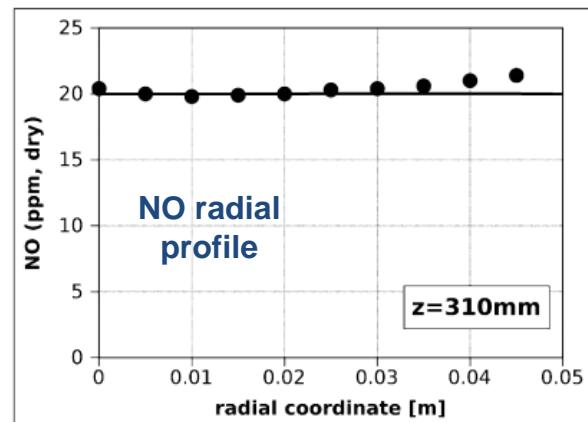
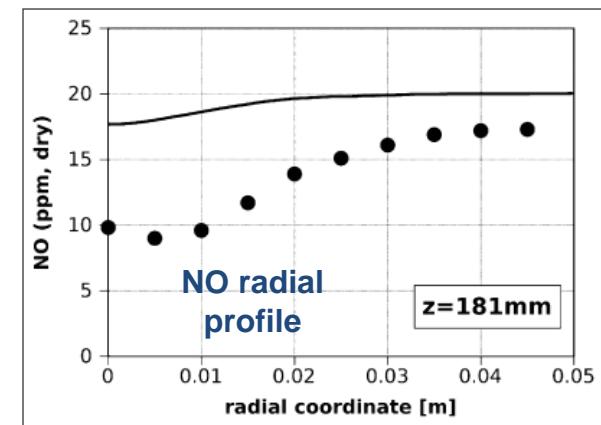
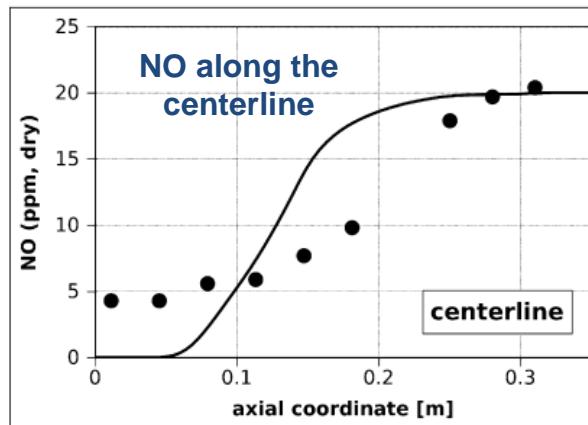
POLIMI_COH2NOX
114 species
2105 reactions

Small-scale MILD Combustor

67



Comparison between experiments and KPP predictions



Reactor Network:
5,000 reactors
(%5 of original number of cells)

1. The CRECK Modeling Group @ Politecnico di Milano
2. Introduction
3. The Kinetic Post Processing (KPP) Technique for NOx
 - ✓ Kinetic mechanisms for CFD applications
 - ✓ Reactor networks from CFD
 - ✓ Effects of temperature fluctuations on NOx formation
 - ✓ Solution of reactor networks
4. Applications to lab-scale and industrial flames
 - ✓ Lab-scale flames
 - ✓ **Industrial cases**
5. Extension to other pollutants
6. Conclusions

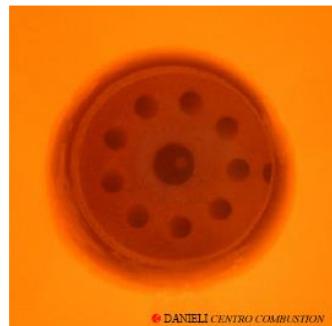


Danieli Centro Combustion
Curno, Italy



Test Furnace: up to 3 MW thermal power

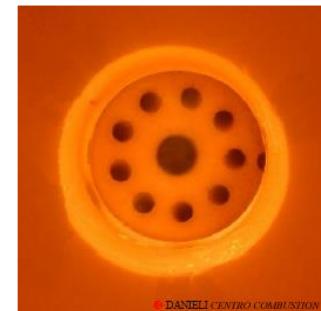
Fuel: gas mixtures with low calorific value
or natural gas



Gas mixture with
low calorific value

30% H₂
15% CO
10% CH₄
45% N₂

Burner region



Natural Gas

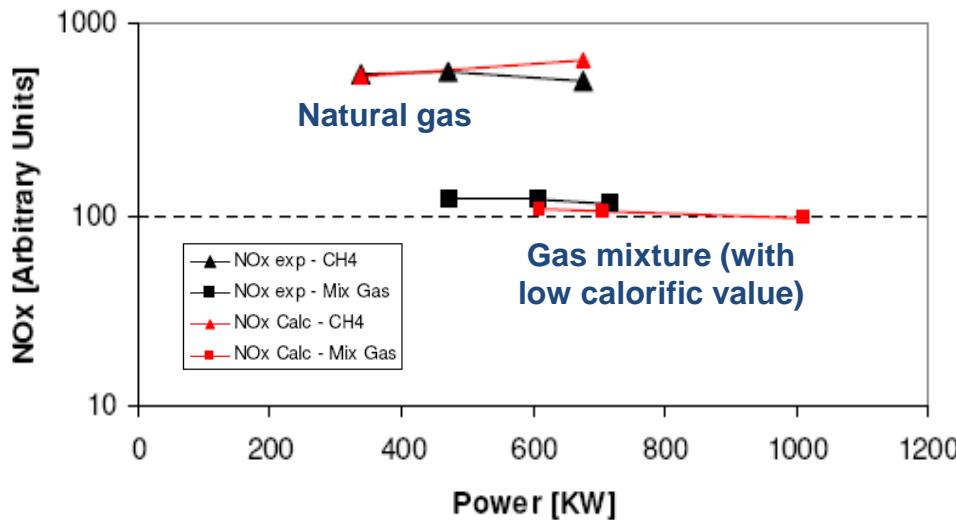
95% CH₄
3% C₂H₆
1% N₂
1% other

Burner region

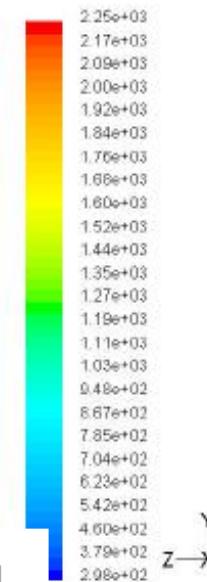
Corus I-70: NOx predictions

70

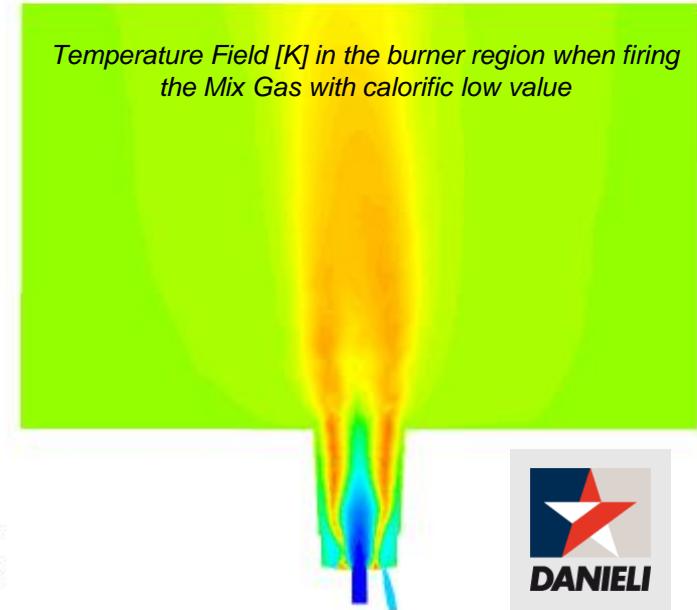
CFD Code	FLUENT 6.2
Space	3D
Grid	Structured (4,000,000 cells)
Time	Steady
Turbulence modeling	Standard κ - ϵ turbulence model
Wall treatment	Standard wall functions
Radiation	Discrete Ordinate Model
Spatial resolution	Second-order Upwind scheme
Pressure Interpolation	PRESTO!
Combustion model	EDC



NOx emissions @3%O₂ in waste gases – Air temperature: 490°C



Temperature Field [K] in the burner region when firing the Mix Gas with calorific low value

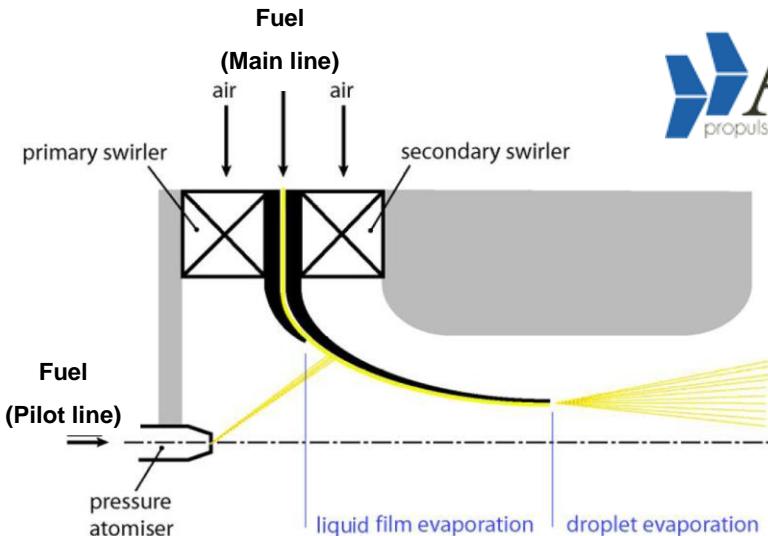
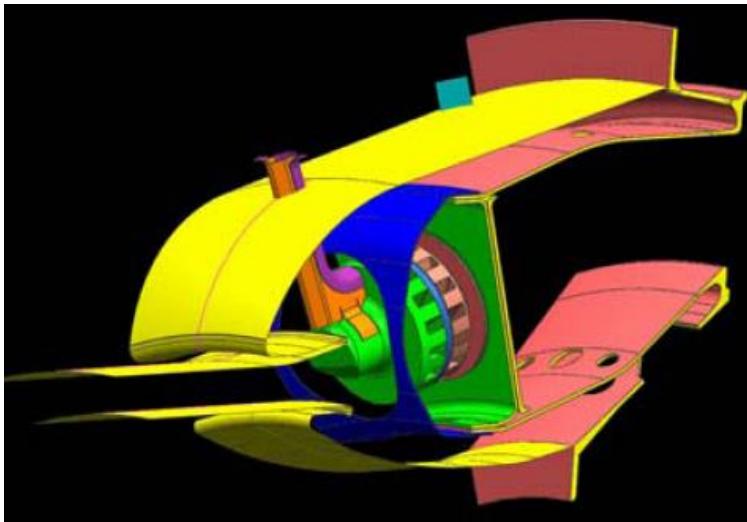


Kinetic Schemes

CFD Simulation
- 7 chemical species
- 3 reactions

KPP
- 100 chemical species
- 1527 reactions

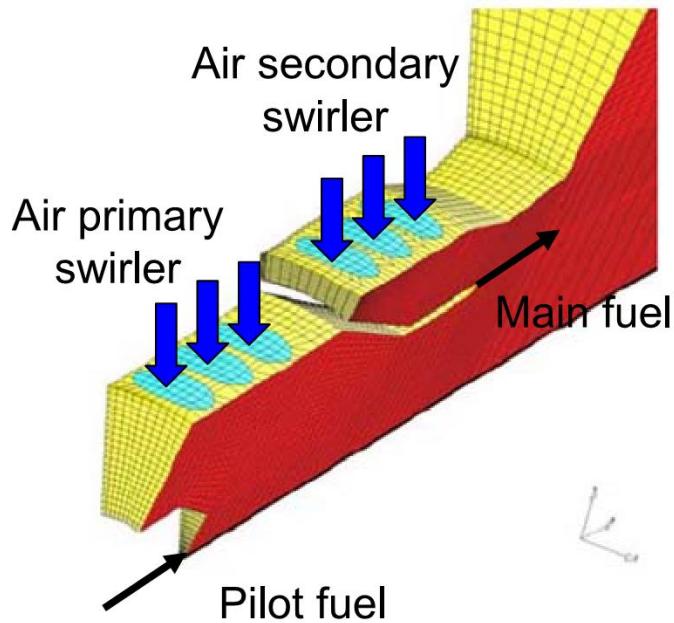
A. Frassoldati, T. Faravelli,
E. Ranzi (2003)



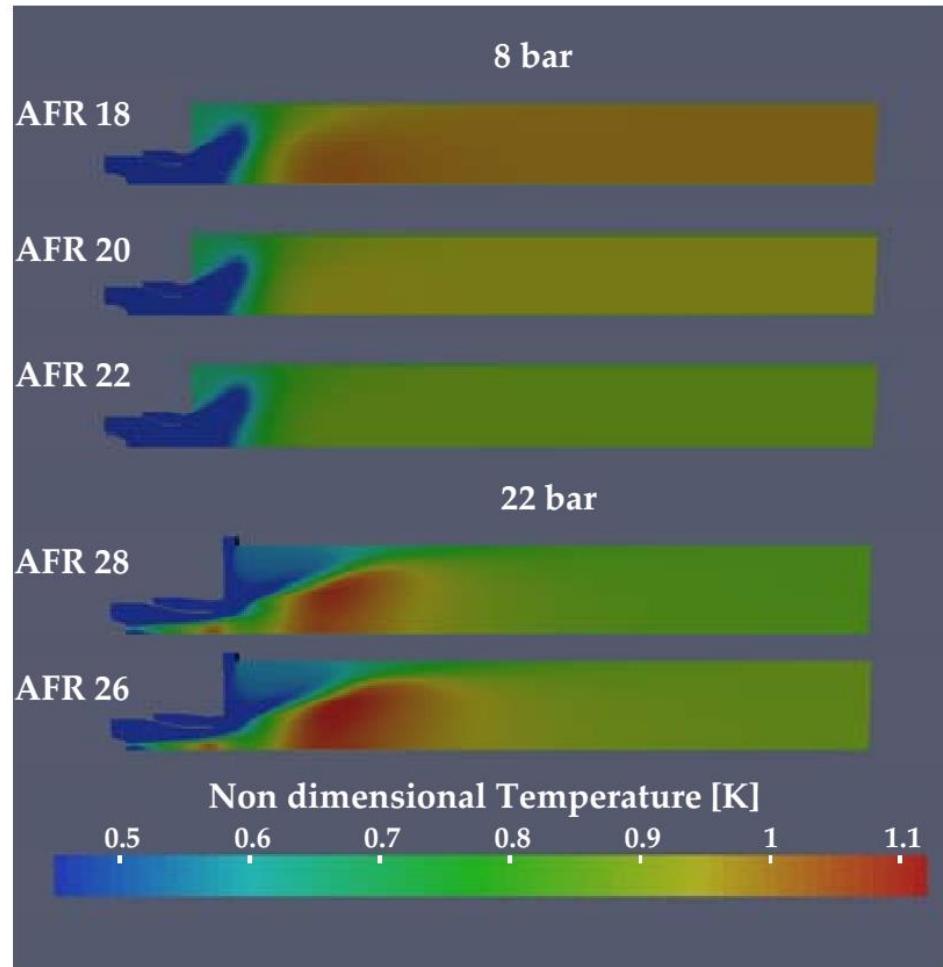
Avio
propulsione aerospaziale

Studied the performance of the PERM (Partial Evaporation & Rapid Mixing) injection system in a **simple tubular combustor**

Experimental Data From	Karlsruhe University	ONERA
	Low P	High P
Inlet Pressure [bar]	8	22
Inlet Temperature [K]	506-522	811
Air/Fuel Ratio (AFR)	18-32	25.7-28.1
Pilot/Total Fuel Ratio	15%	15%

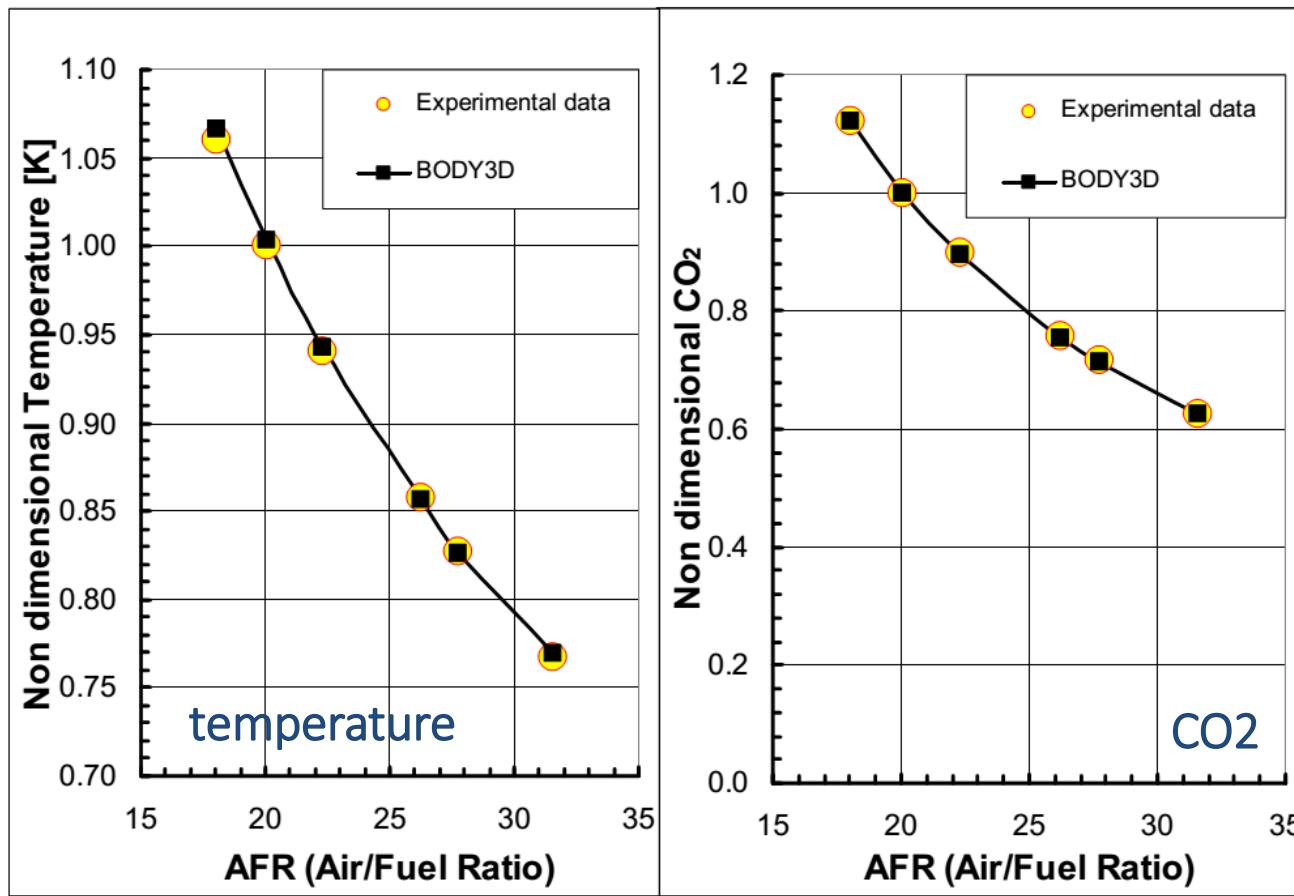


BODY3D CFD Code
K-e turbulence model
ED-FR Combustion model
Global 3-step kinetic mechanism
Mesh with 80,000 cells



AFR id the air/fuel ratio

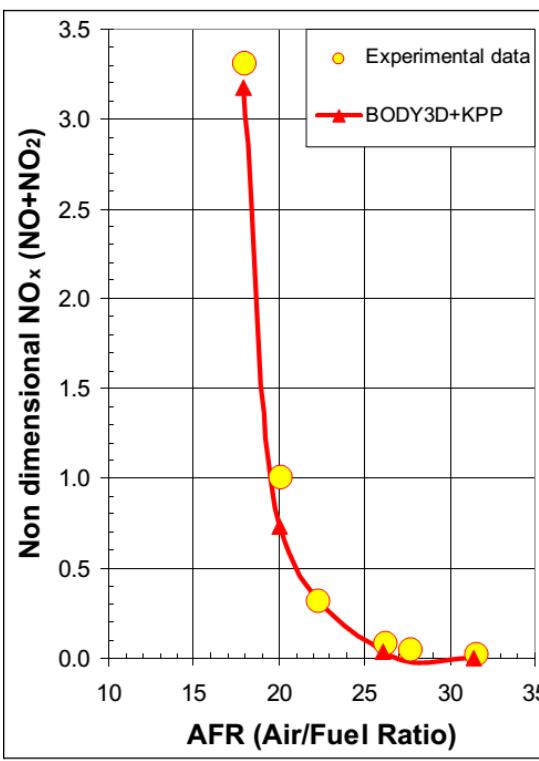
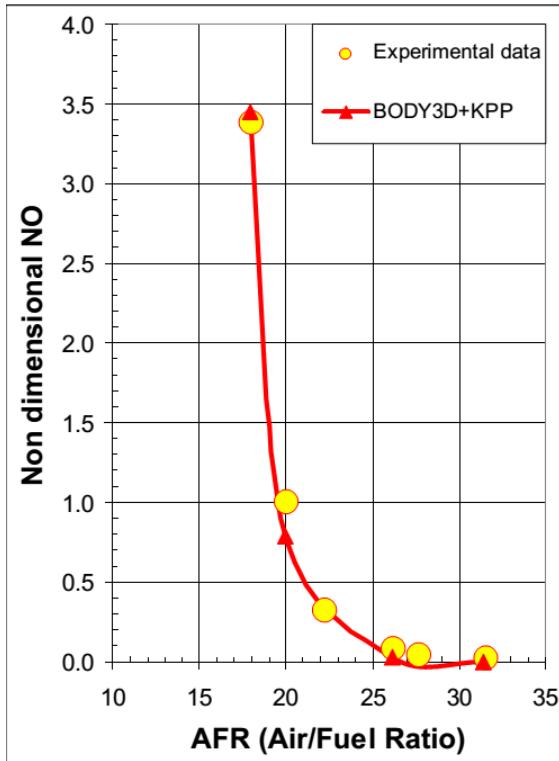
Comparison with measurements at the outlet



Low P (8 bar)

Kinetic post-processing (I)

Comparison with measurements at the outlet



Low P (8 bar)

Kinetic Post
Processing

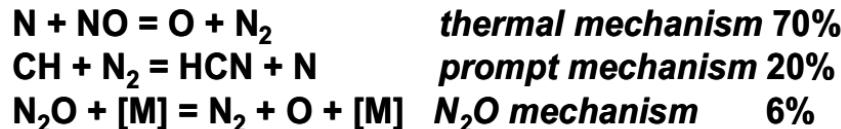


POLIMI_NC7
103 species
1500 reactions

Kinetic post-processing (II)

Low P (8 bar), AFR=18

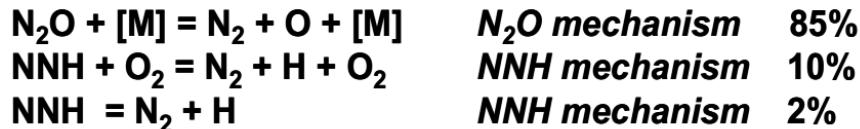
Relative contribution to NO formation [%]



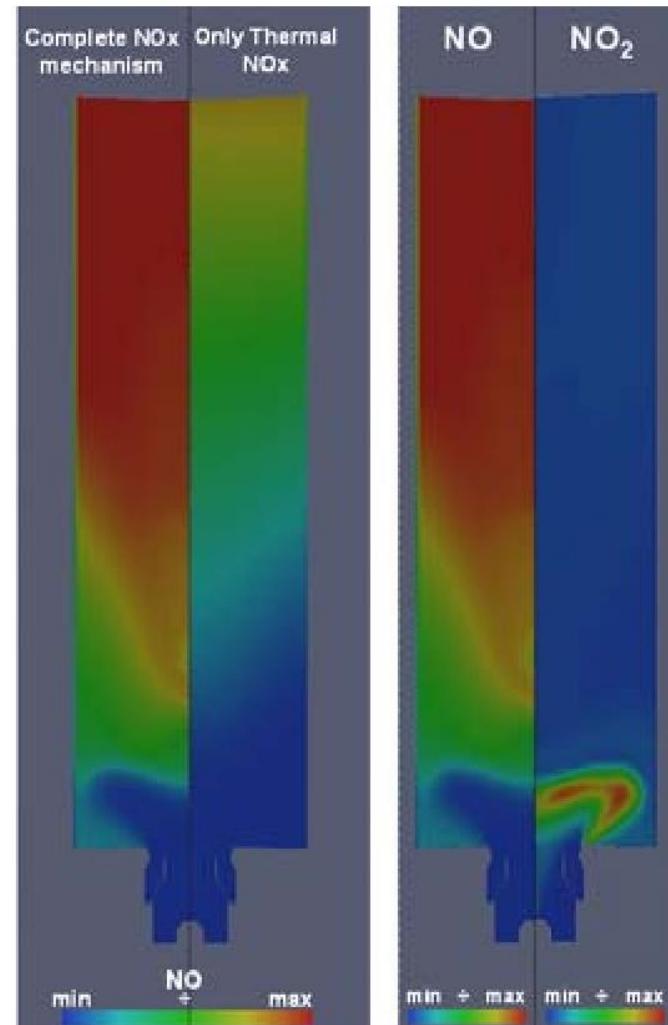
High temperature

Low P (8 bar), AFR=31

Relative contribution to NO formation [%]



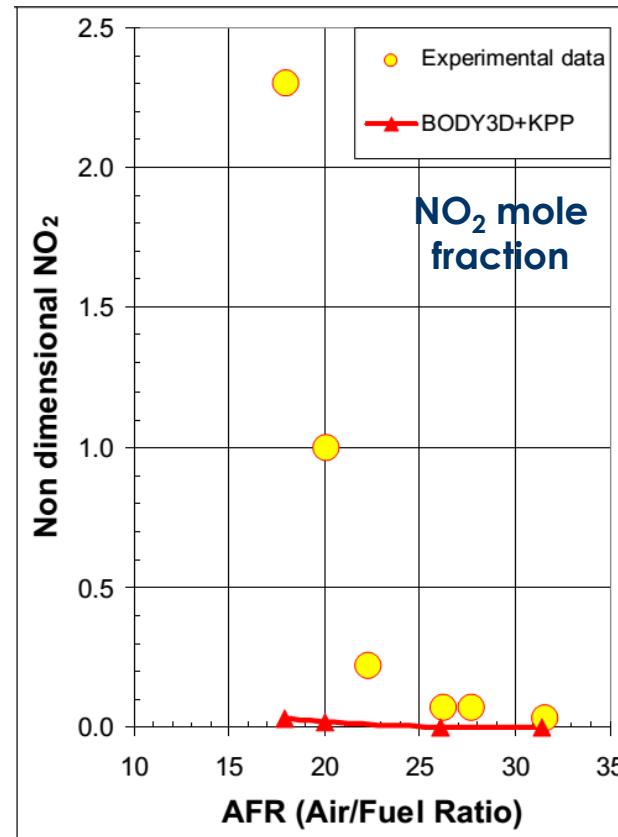
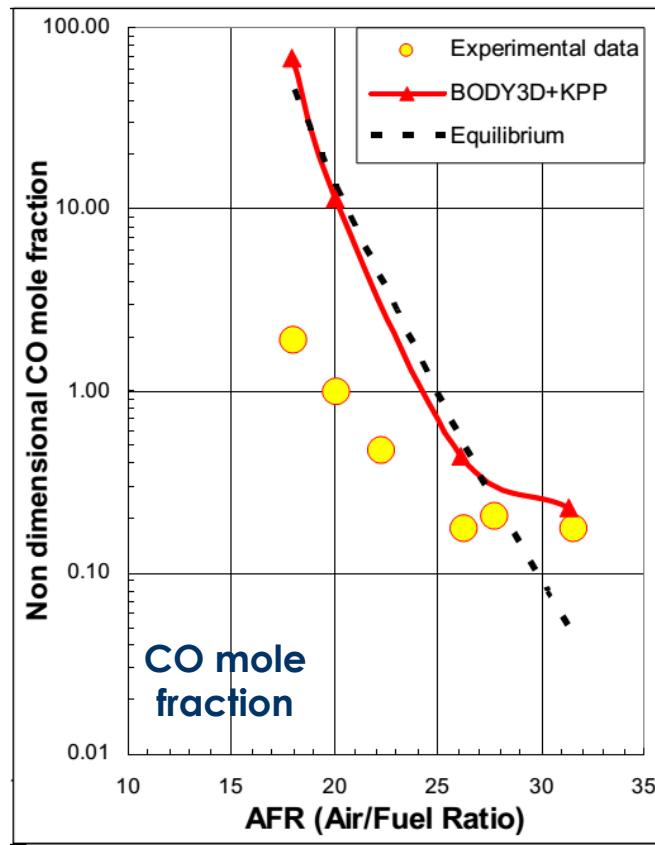
Low temperature



Low P (8 bar), AFR=21.16

The “probe effect” (I)

The model is able to capture the trends but tends to overestimate the CO emissions, especially at high temperatures. On the other hand, CO emissions predicted by the KPP are very close to the equilibrium value at high temperatures, while the effect of finite rate kinetics is evident at lower temperatures.



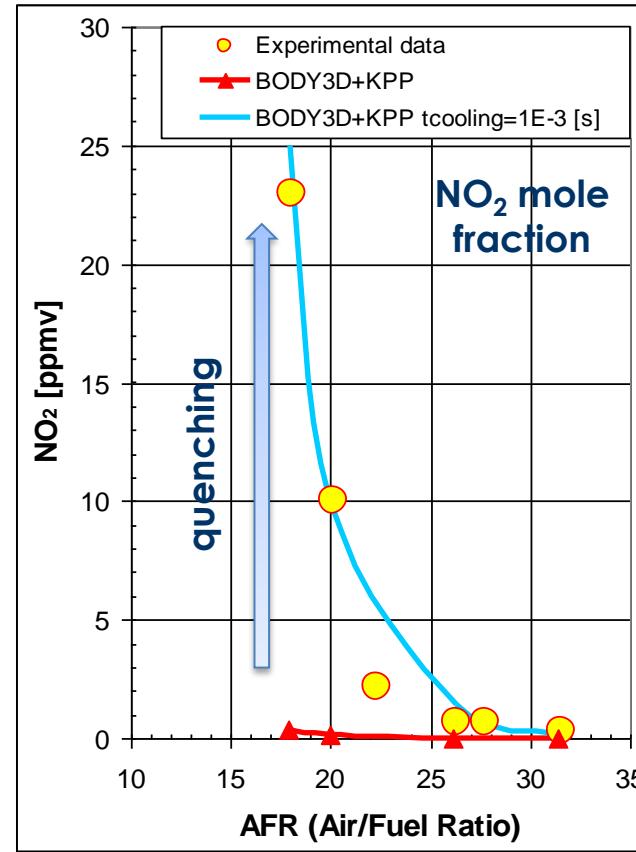
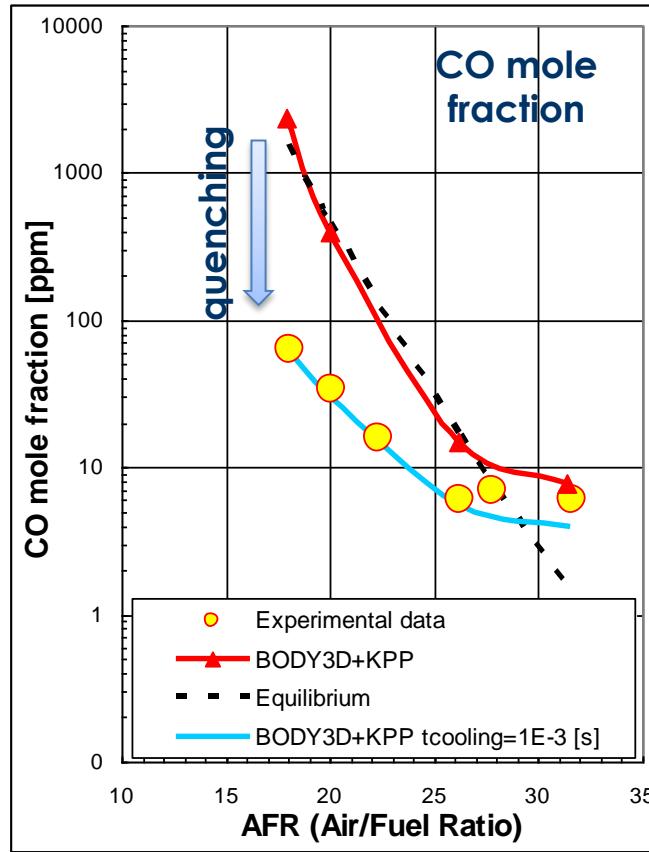
The “probe effect” (II)

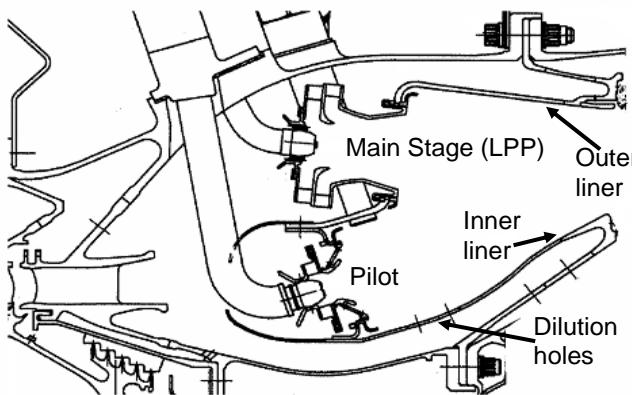
77

Deviation on CO and NO₂ predictions can be explained as a possible effect of the measurement technique. This problem is known in the literature.

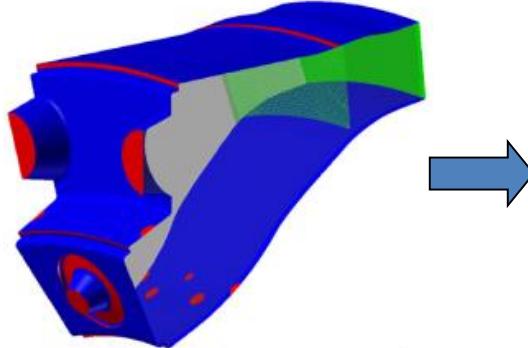
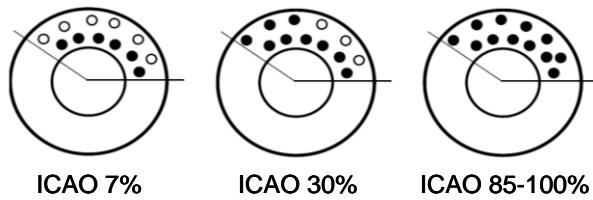
The cooling rate of the flue gases inside the sampling probe is not fast enough to “quench” the reactivity.

Conversion of CO to CO₂ and NO to NO₂ occurs in the probe.





Pilot Run Stage Burning Full Running

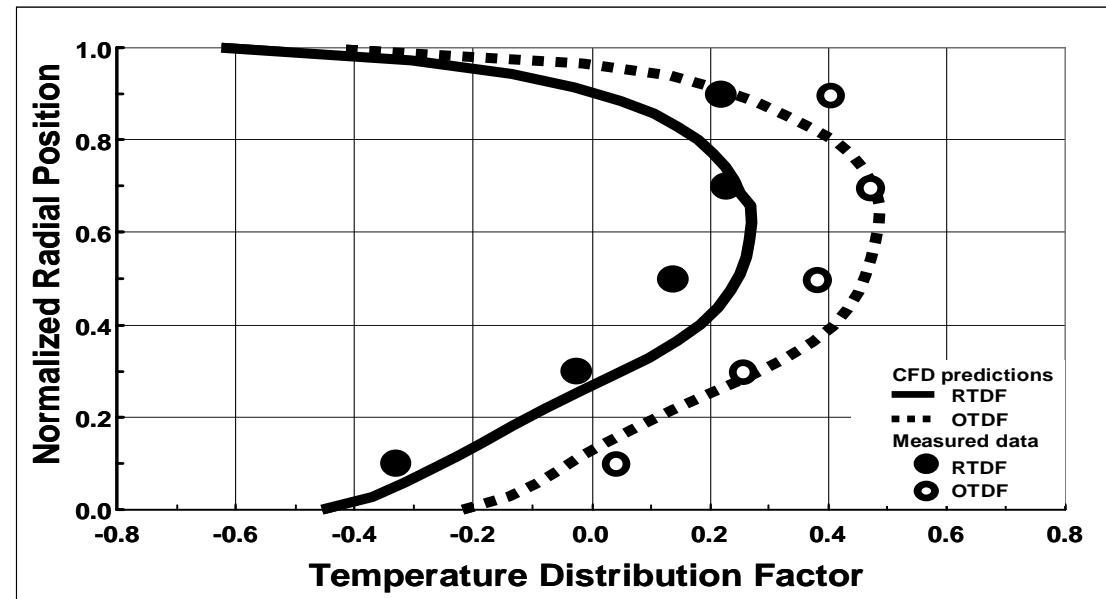


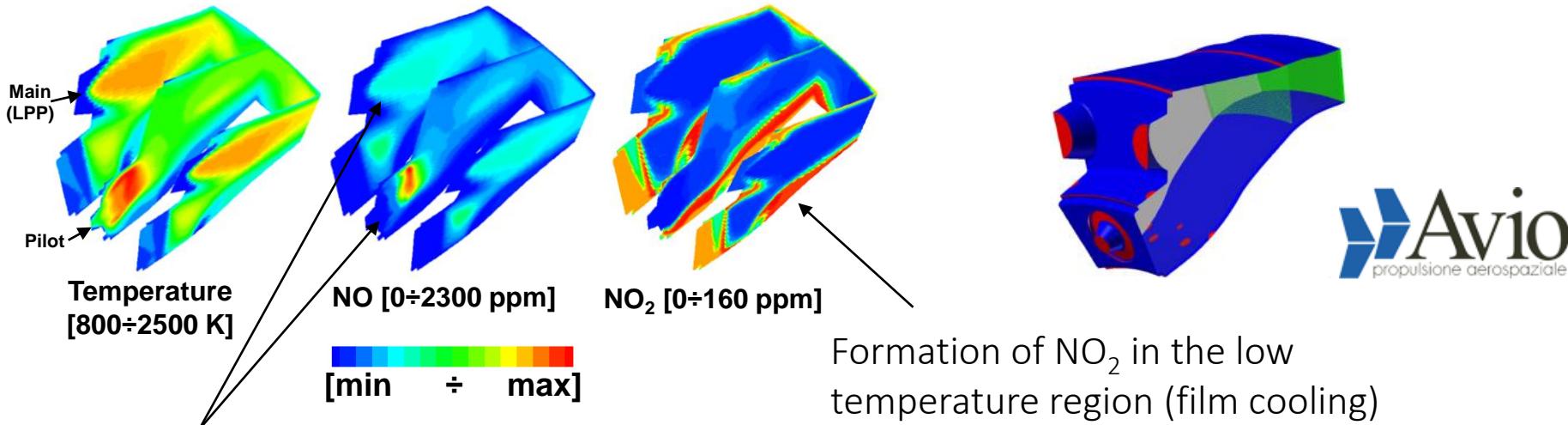
CLEAN is an axially staged combustor equipped with:

- **18 LPP injectors** (Lean Premixed Prevaporized technology)
- **18 conventional pilot injectors**



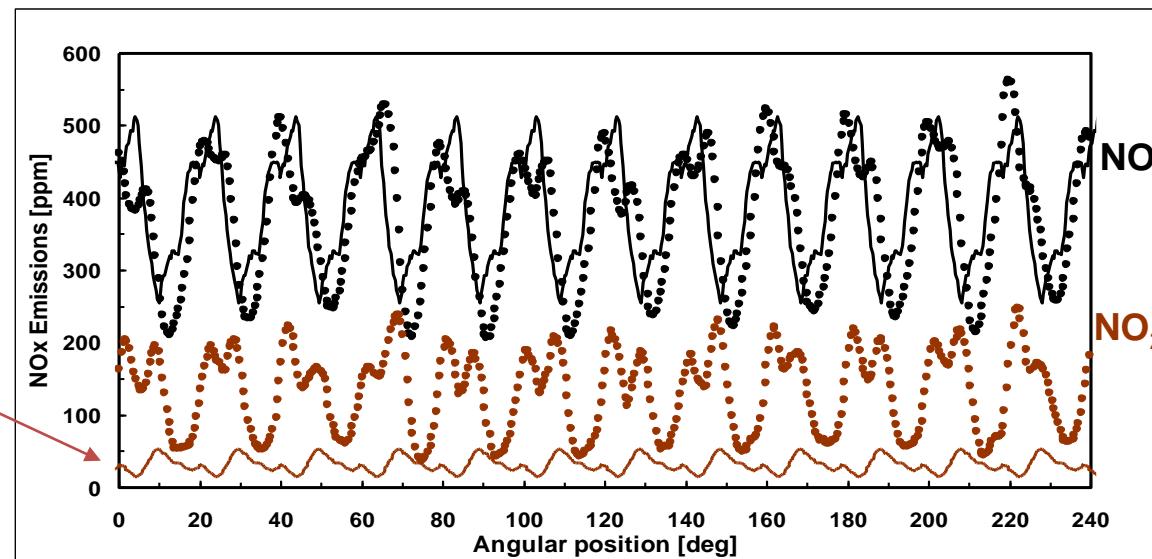
Good agreement with experimental measurements of Radial and Overall Temperature Distribution Factors at the outlet.



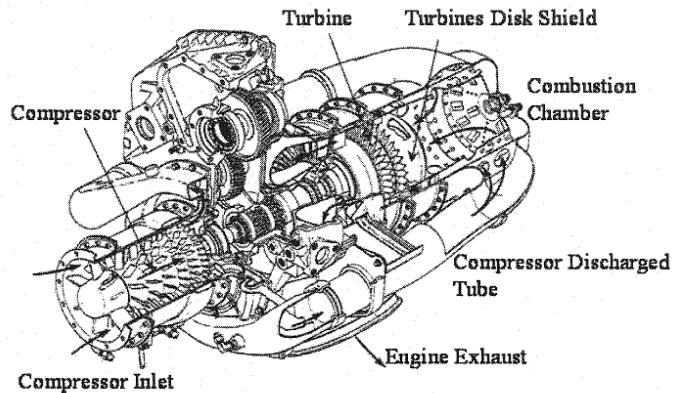


Different NOx formation in the conventional (pilot) and LPP injectors

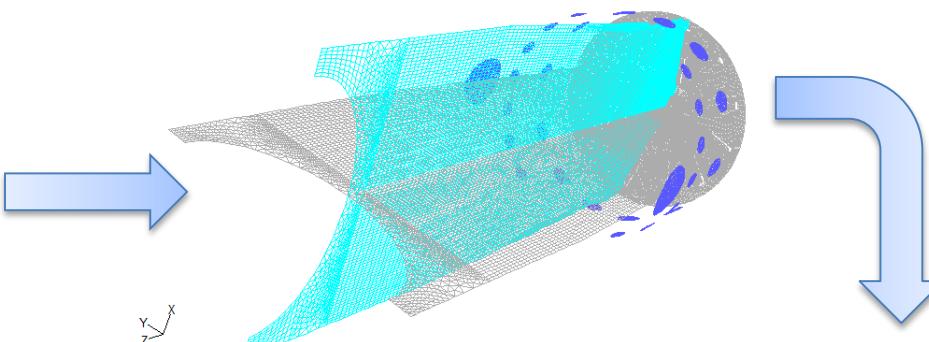
Possible NO->NO₂ conversion in the probe



ROLL-ROYCE ALLISON 250 ENGINE

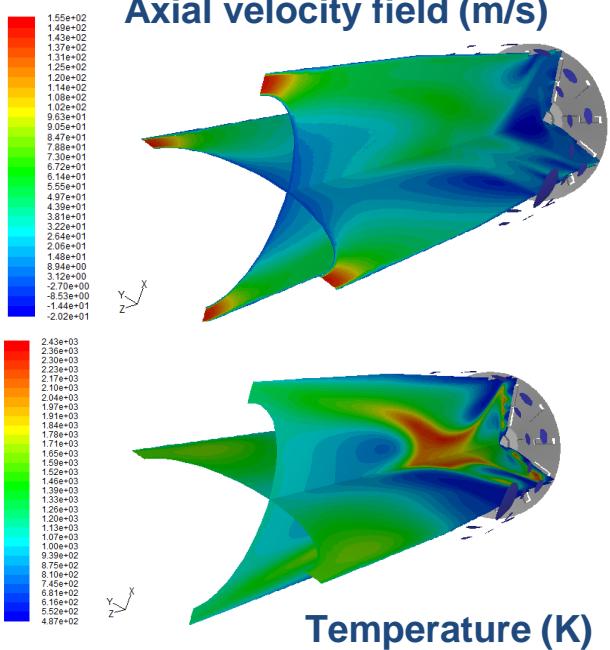
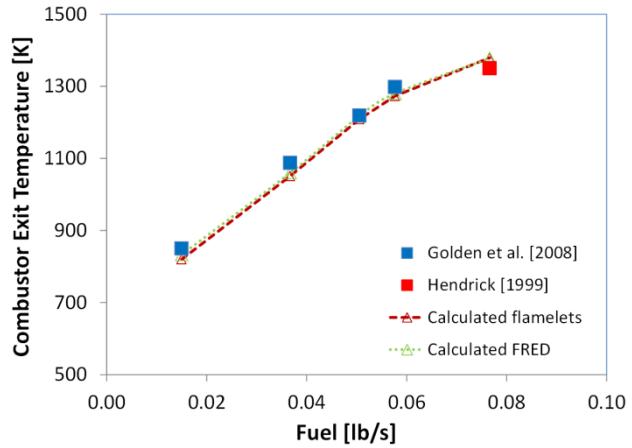


MESH (~1,000,000 cells)



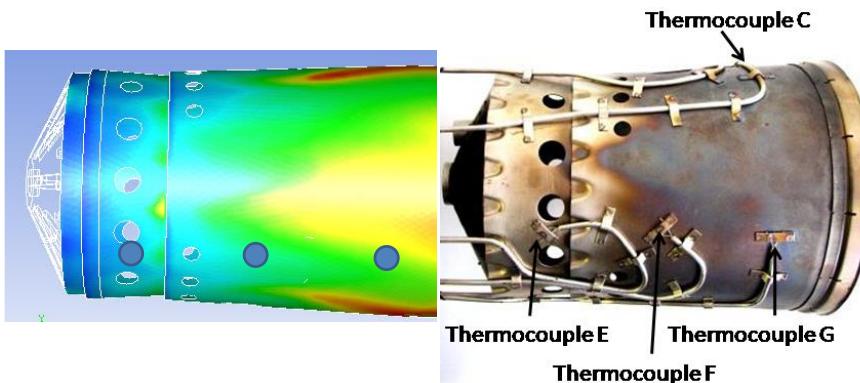
Axial velocity field (m/s)

Comparison with experimental data

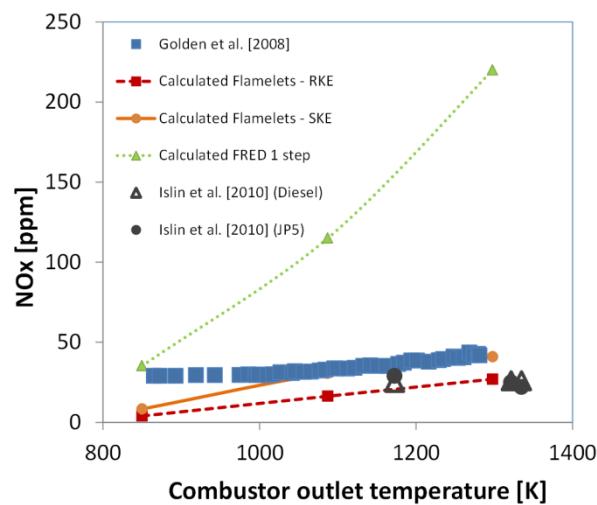


Temperature (K)

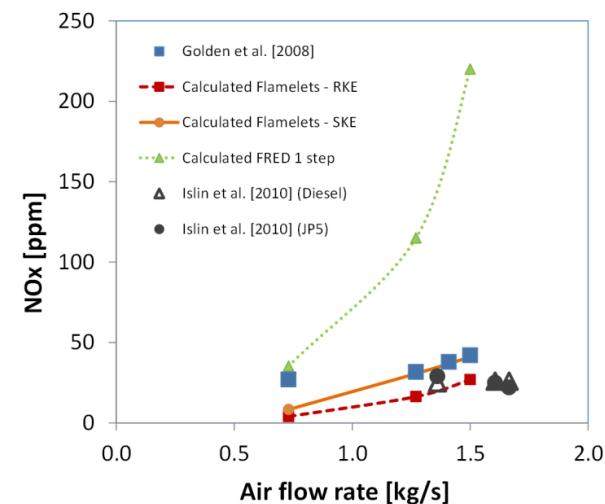
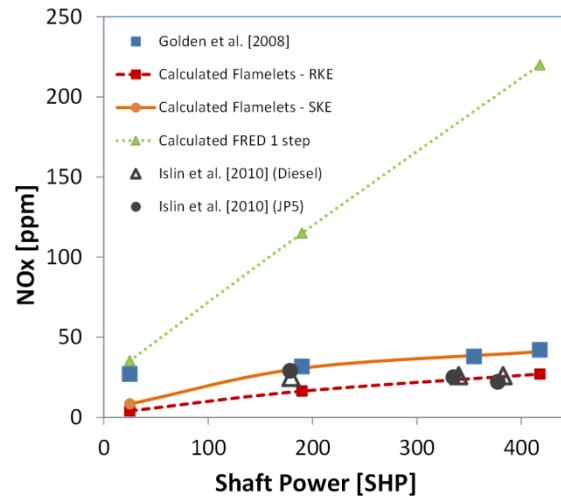
3-RR-Allison 250C engine



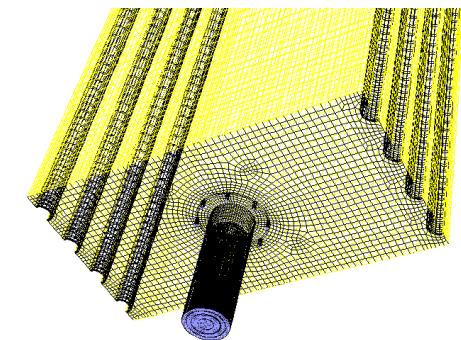
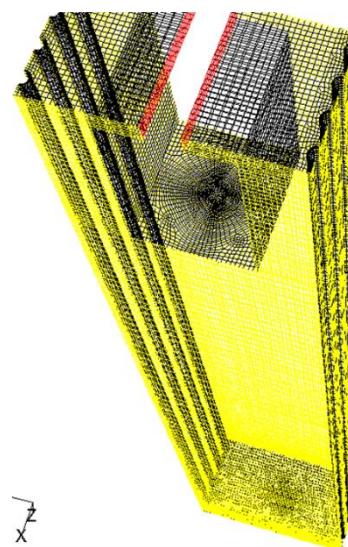
Bester et al., Proceedings of ASME Turbo Expo 2009: Power for Land, Sea and Air, GT2009-60333, June 8-12, 2009, Orlando, Florida, USA.



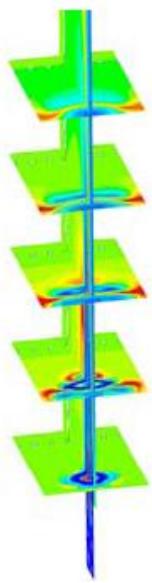
Golden et al., paper AIAA 2008-4902, 44th AIAA/ASME/SAE/ASEE Joint Propulsion Conference & Exhibit 21 - 23 July 2008, Hartford, CT.



Islin et al., Proceedings of ASME Turbo Expo 2010: Power for Land, Sea and Air GT2010, paper 22436.



3D Computational mesh
with 500,000 cells



KPP used to evaluate effect on
NOx of **different burner design,**
possible burner-burner
interaction etc



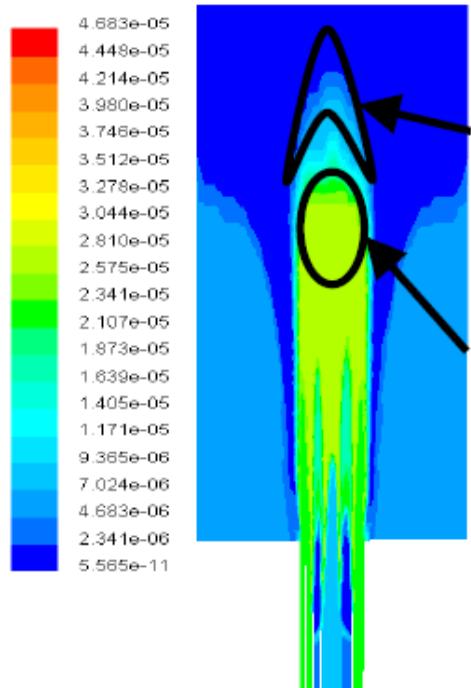
0 NOx Max



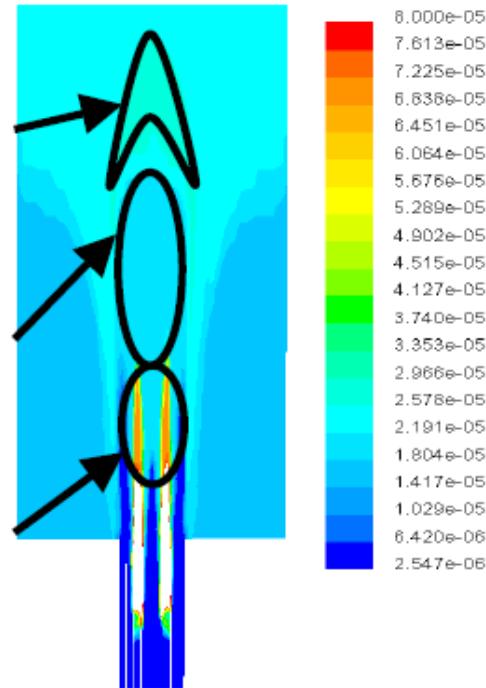
Technip

Technip developed a
parallel version of the KPP
code based on MPI

NO_2 mass fraction



NO mass fraction



Global Kinetic scheme

6 species
3 reactions

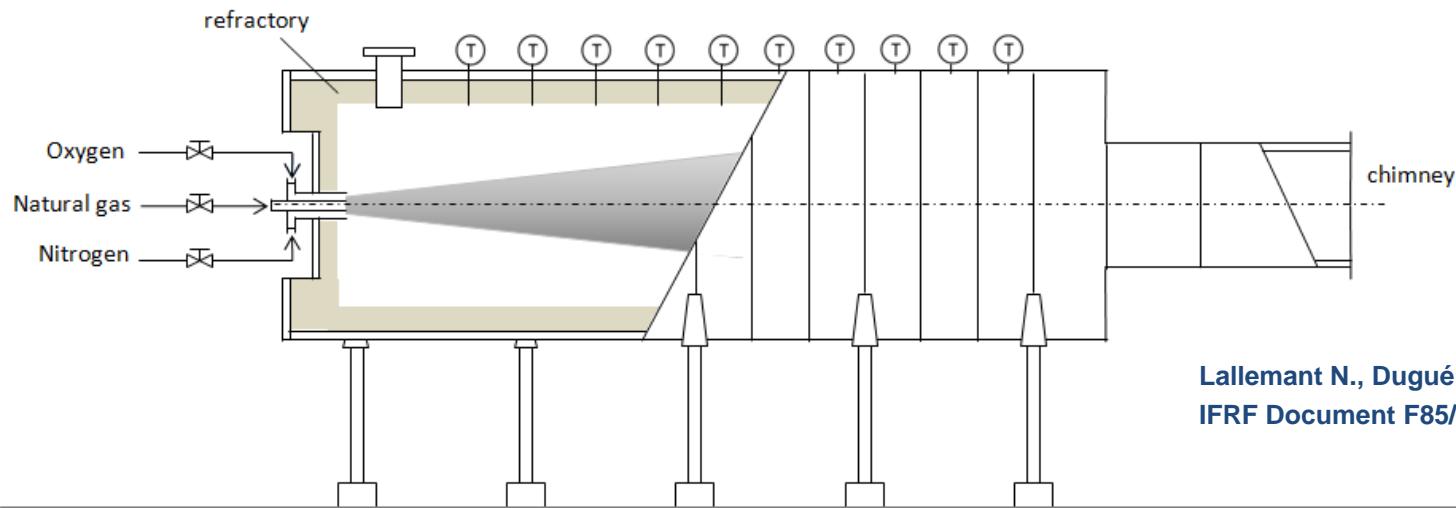
Eddy Dissipation Concept Model

POLIMI_C1C3HTNOX

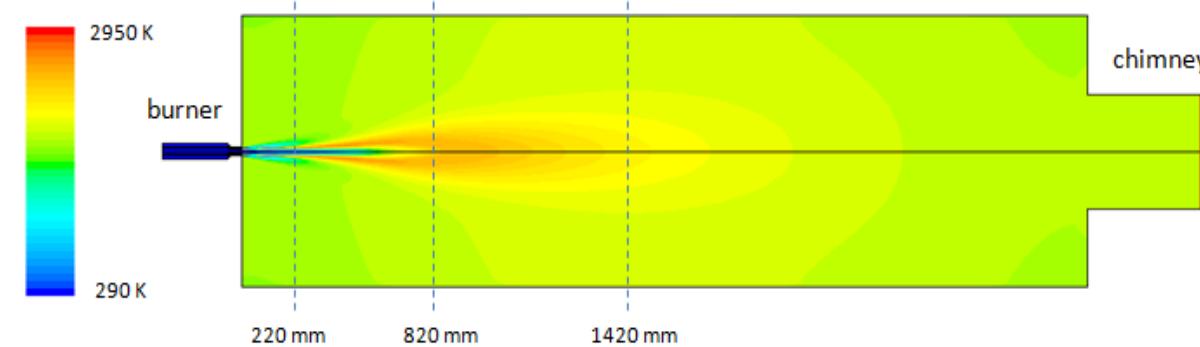
100 species
1527 reactions

Number of Reactors:

500,000
(%100 of original number of cells)



Lallemand N., Dugué J., Weber R.
IFRF Document F85/y/4 (1996)



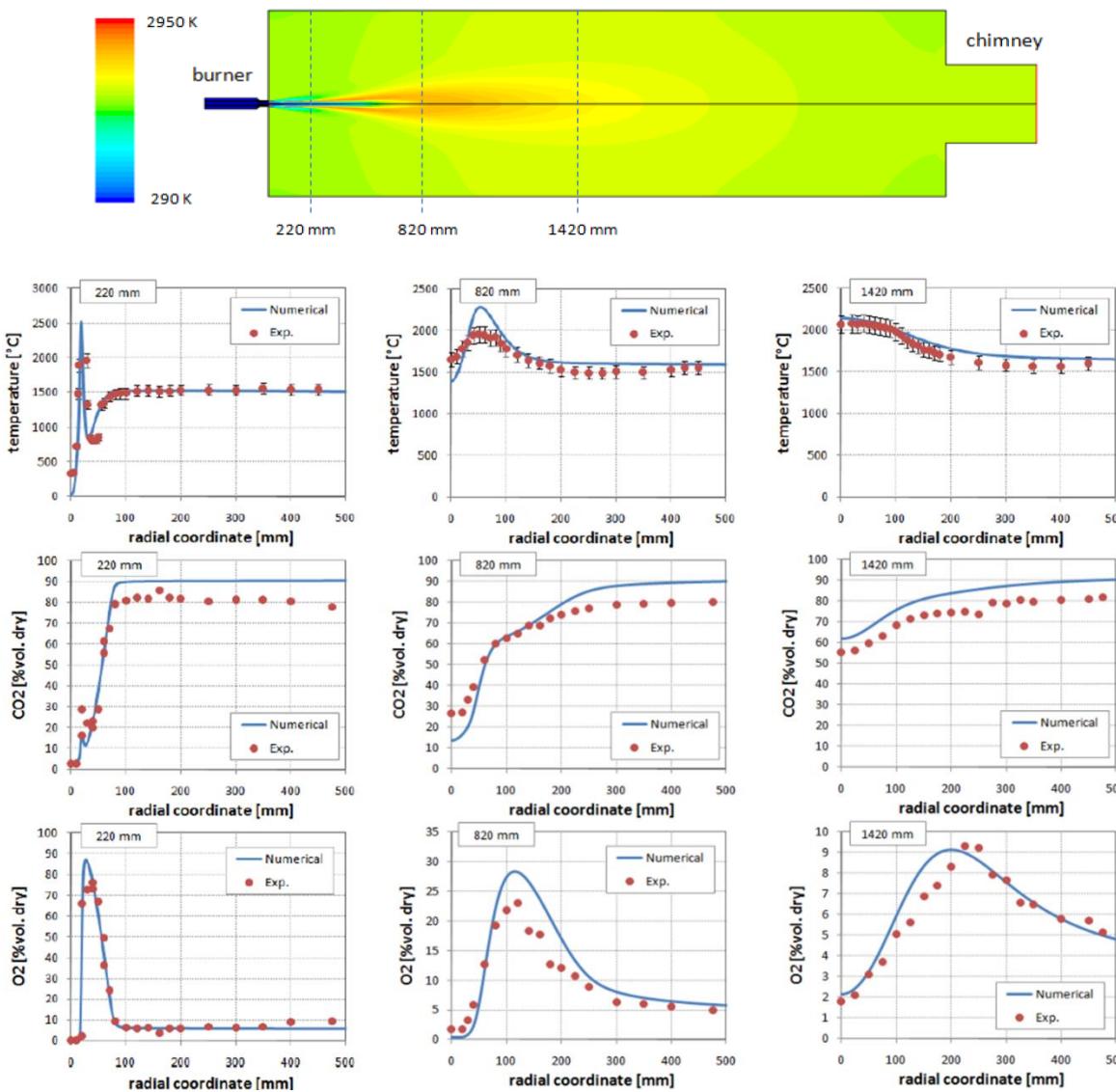
Experimental data

velocity, main species and temperature profiles
inside the furnace at several axial locations

Furnace dimensions: 3750 x 1050 x 1050 mm

Thermal power: 0.78 MW

IFRF Furnace (OxyFLAM2)



CFD

Skeletal Kinetic Scheme
33 species
152 reactions

Eddy Dissipation Concept Model

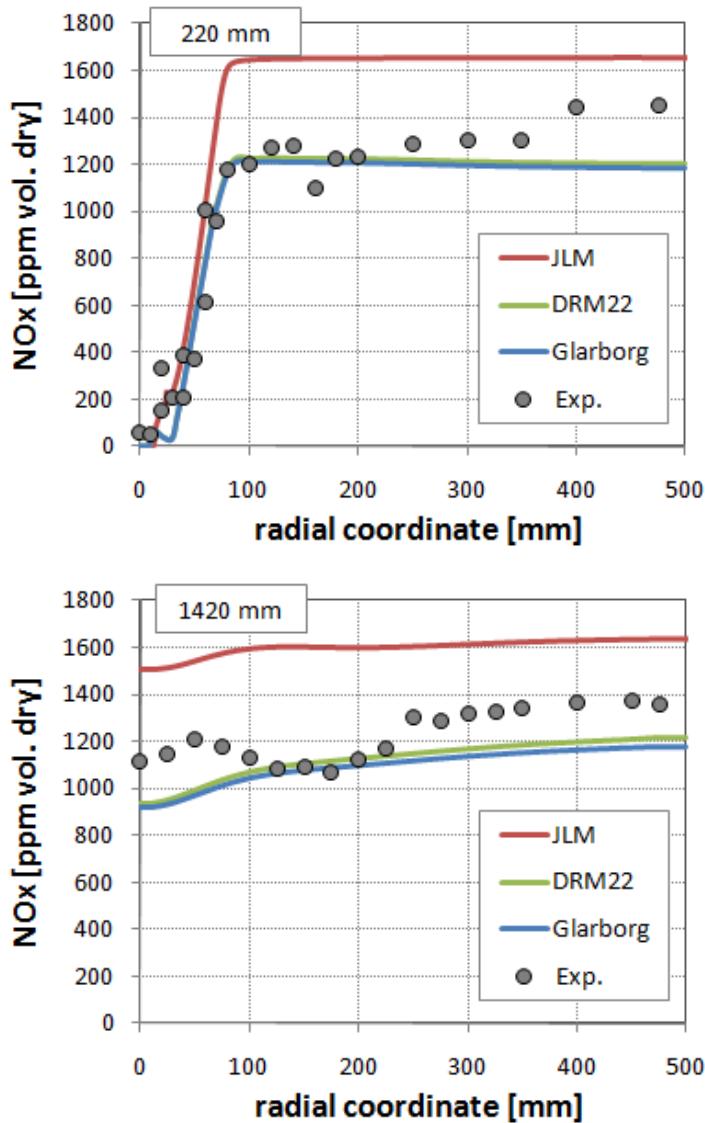


POLIMI_C1C3HTNOX
100 species
1527 reactions

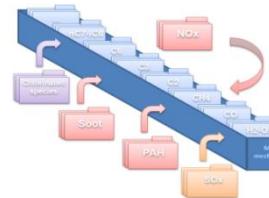
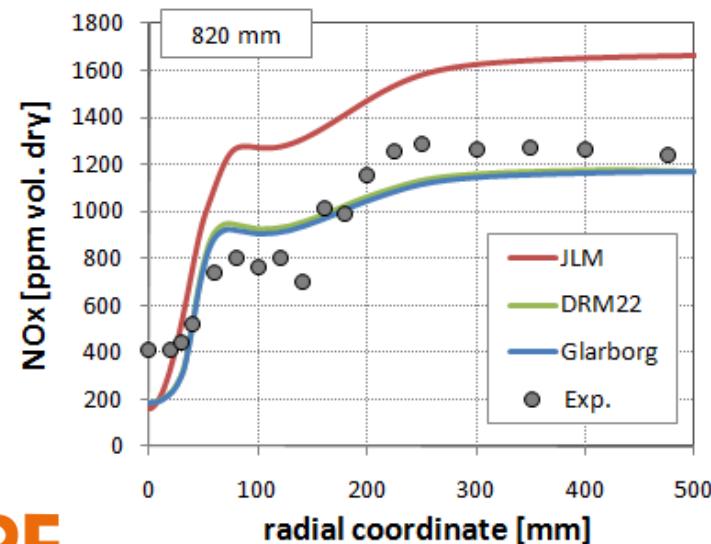
Number of Reactors:
5,000
(%10 of original number of cells)

KPP

MORE



MORE

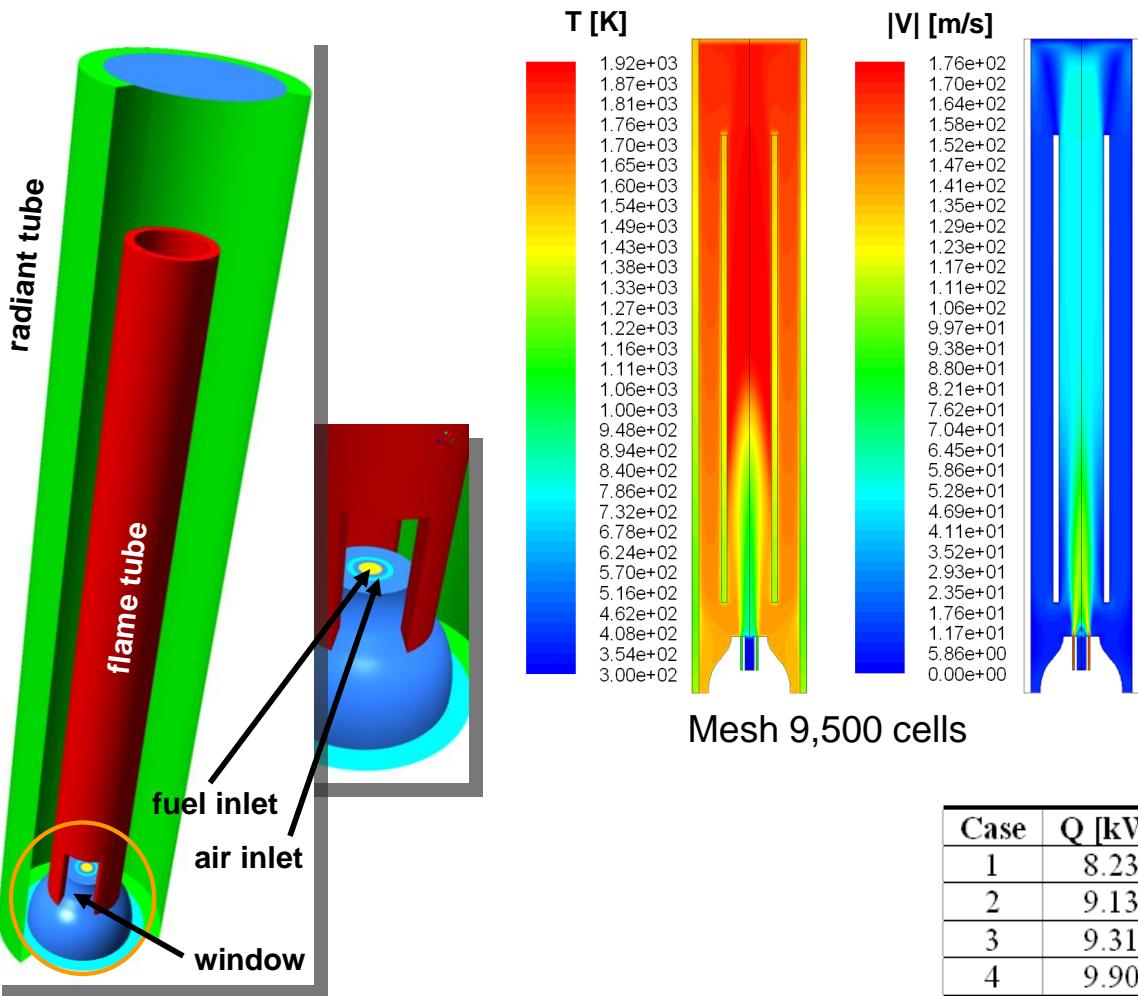


PolimiC1C3HT + NOX

100 species, 1530 reactions

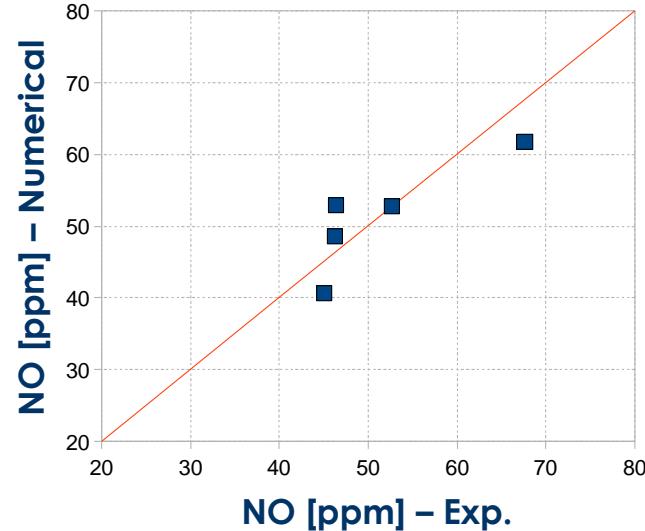
<http://creckmodeling.chem.polimi.it>

Ranzi E., Faravelli T., Frassoldati A., Granata S., Industrial and Engineering Chemistry Research, 44 (44), 5170-5183 (2005).



A. Parente, A. Cuoci, C. Galletti, A. Frassoldati, T. Faravelli, L. Tognotti, NO formation in flameless combustion: comparison of different modeling approaches, European Combustion Meeting 2009 14-17 April 2009 - Vienna, Austria

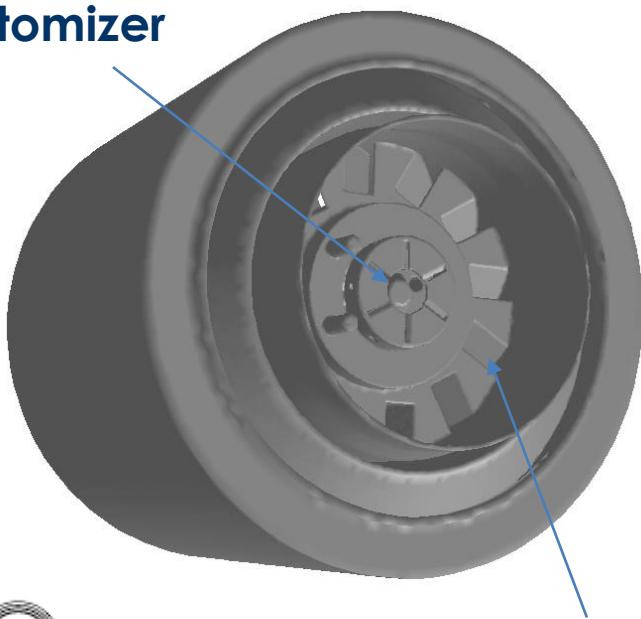
Comparison between experiments and simulation



Case	Q [kW]	T exhaust [K]	T max [K]	NO exp [ppm]
1	8.23	1479	1815	5.8
2	9.13	1535	1920	18.9
3	9.31	1651	2034	40.7
4	9.90	1687	2065	52.9
5	10.53	1710	2066	52.8
6	10.70	1722	2096	61.8
7	10.42	1702	2049	48.6



Atomizer

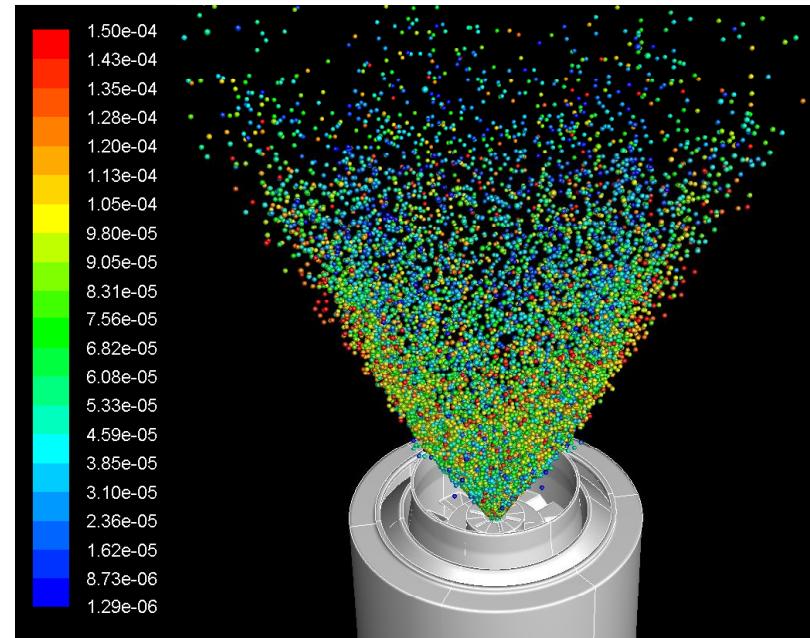


Swirler

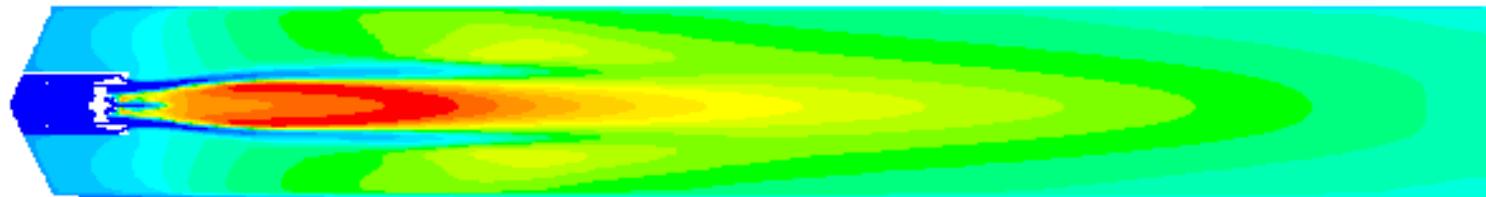


le nuove energie per il clima

Particle diameter [m]



Typical hollow-cone structure obtained using a pressure-swirl atomizer



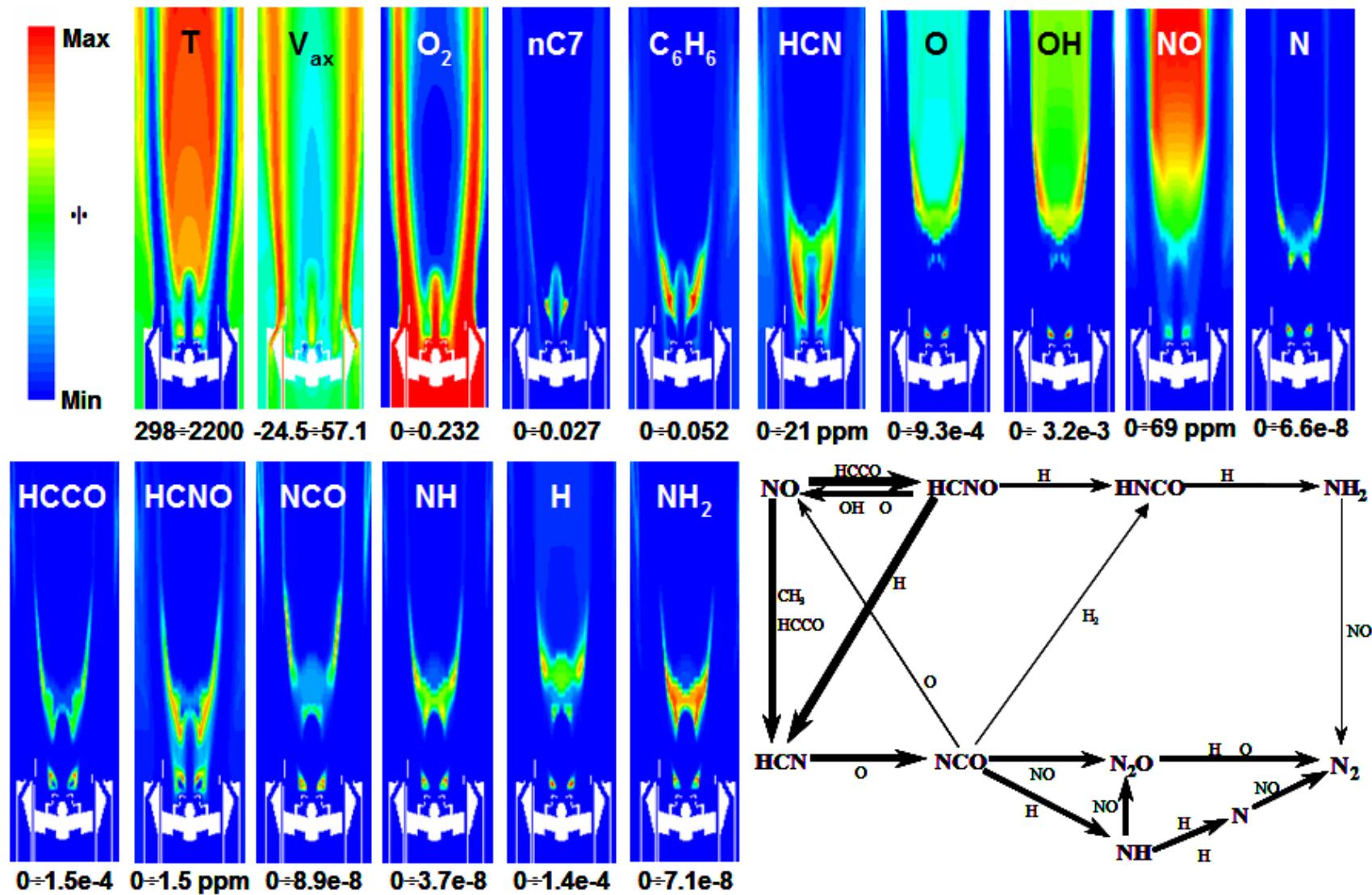
Temperature Field [K]

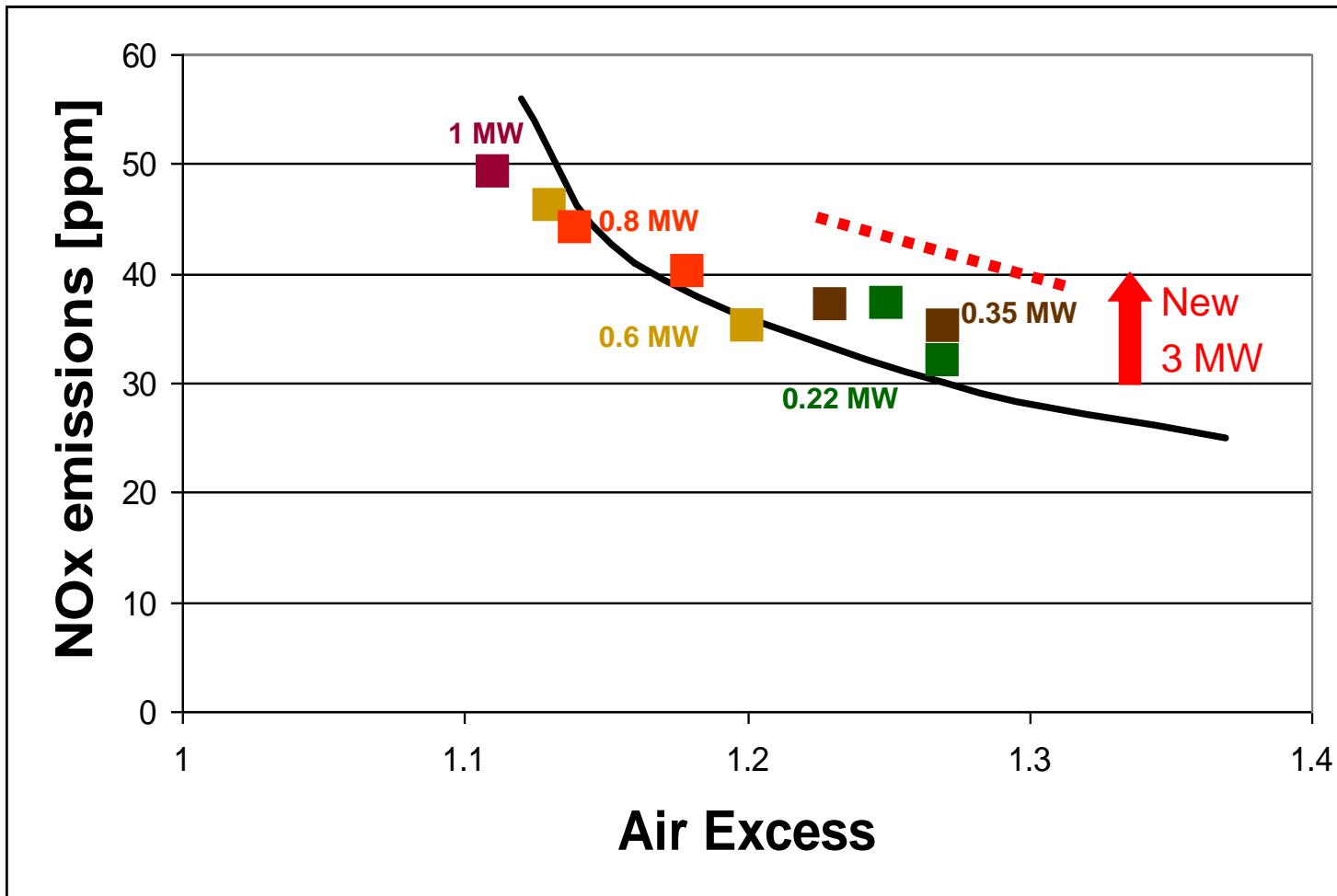
300

2270

Riello Gasoil Burner

89



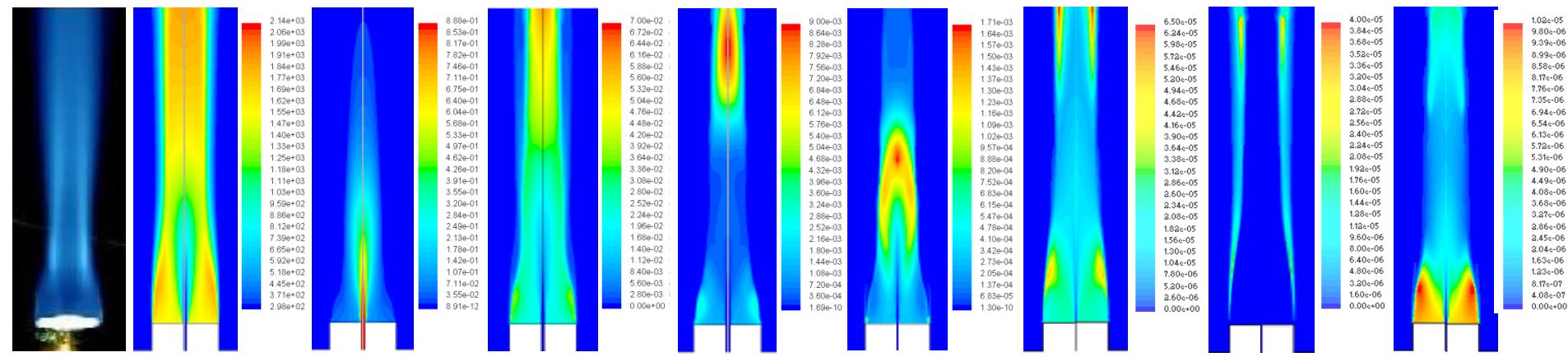


Comparison with measurements is satisfactory
Only measurements at the outlet

1. The CRECK Modeling Group @ Politecnico di Milano
2. Introduction
3. The Kinetic Post Processing (KPP) Technique for NOx
 - ✓ Kinetic mechanisms for CFD applications
 - ✓ Reactor networks from CFD
 - ✓ Effects of temperature fluctuations on NOx formation
 - ✓ Solution of reactor networks
4. Applications to lab-scale and industrial flames
 - ✓ Lab-scale flames
 - ✓ Industrial cases
5. Extension to other pollutants
6. Conclusions

Sandia Bluff-Body Flame

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T[K]

CH_4

CO

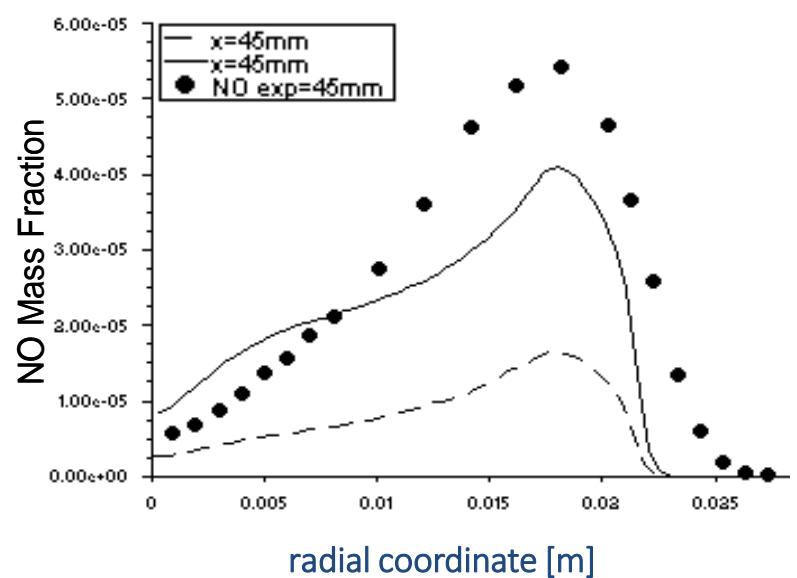
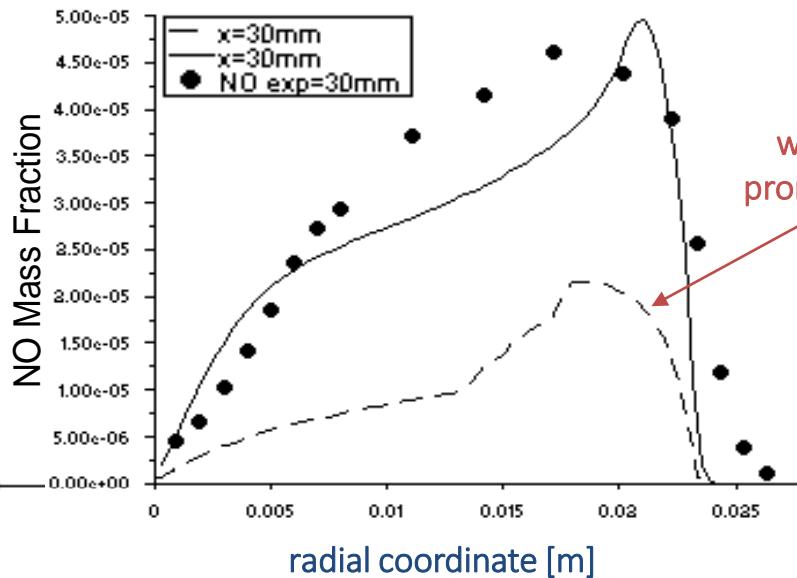
C_2H_2

CH_2O

NO

NO_2

HCN



The weak influence of the minor species on the temperature fields was checked through an energy analysis of the reactor network. For each reactor, energy unbalances were calculated:

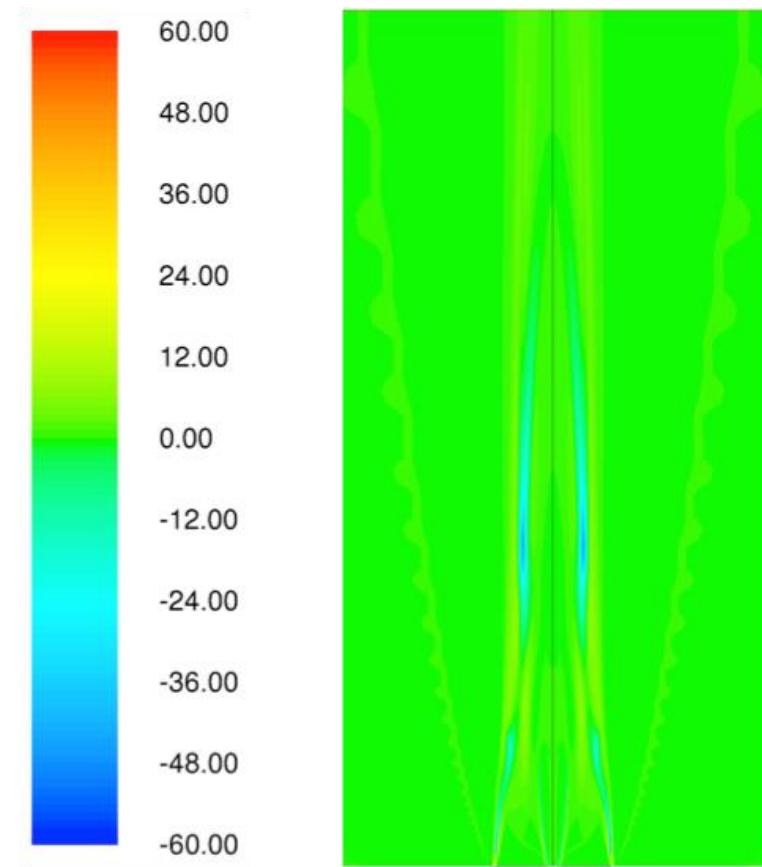
$$\Delta H_{CFD} = (H_{in} - H_{out})_{CFD}$$

$$\Delta H_{KPP} = (H_{in} - H_{out})_{KPP}$$

The overall energy unbalance due to the post-processing was evaluated as the difference. Then, the unbalance in terms of temperature was calculated as:

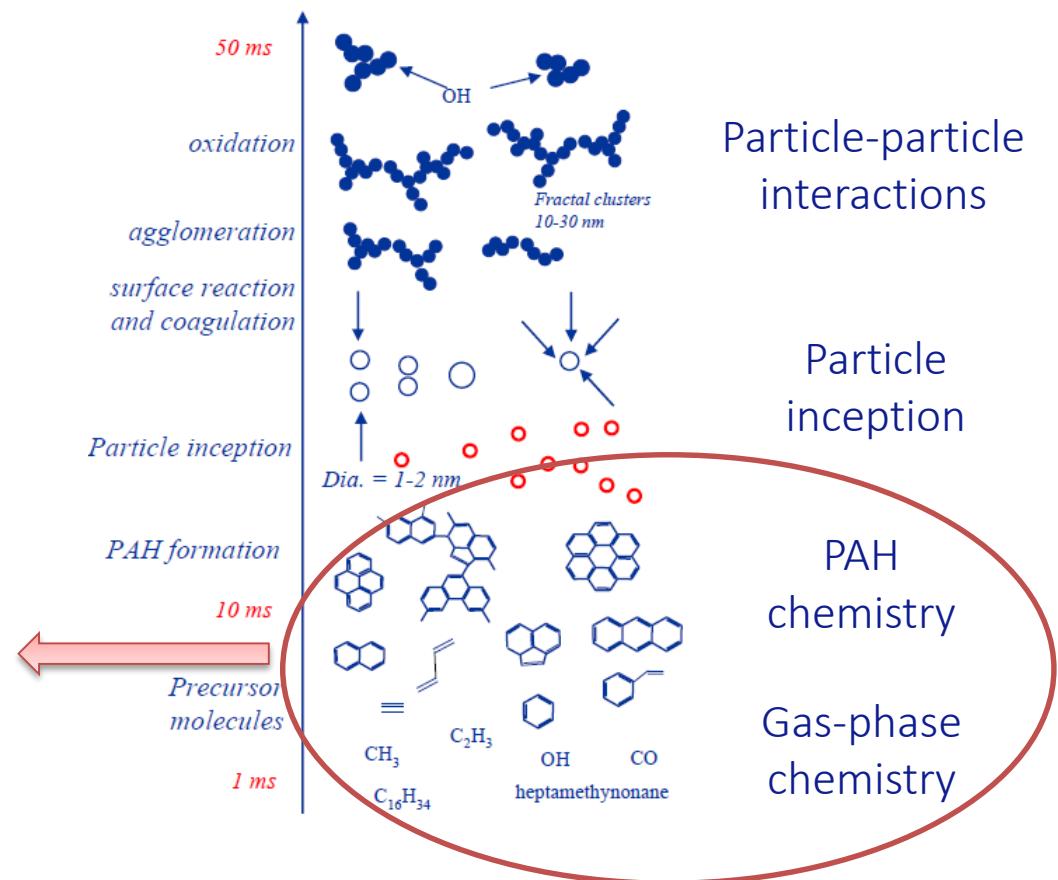
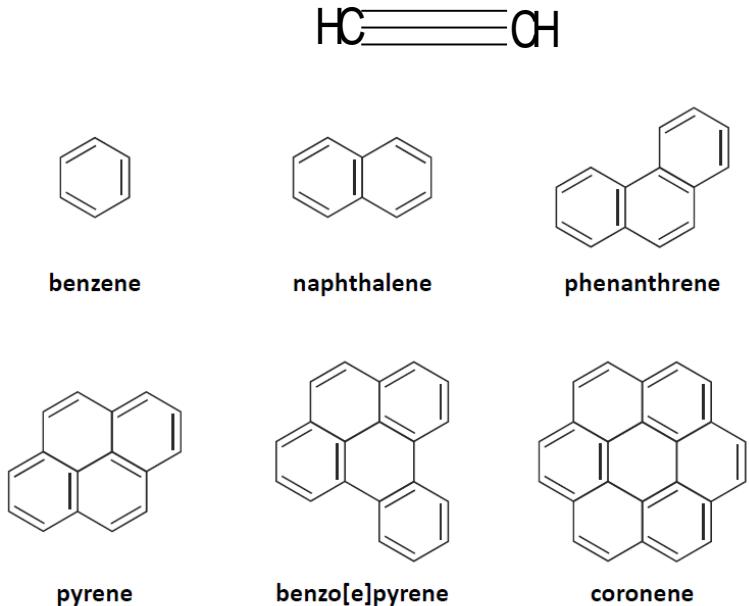
$$\Delta T = \frac{\Delta H_{KPP} - \Delta H_{CFD}}{C_P \dot{m}}$$

Local temperature unbalances in K



The average temperature unbalance is 0.27 K, with a standard deviation of 5.43 K

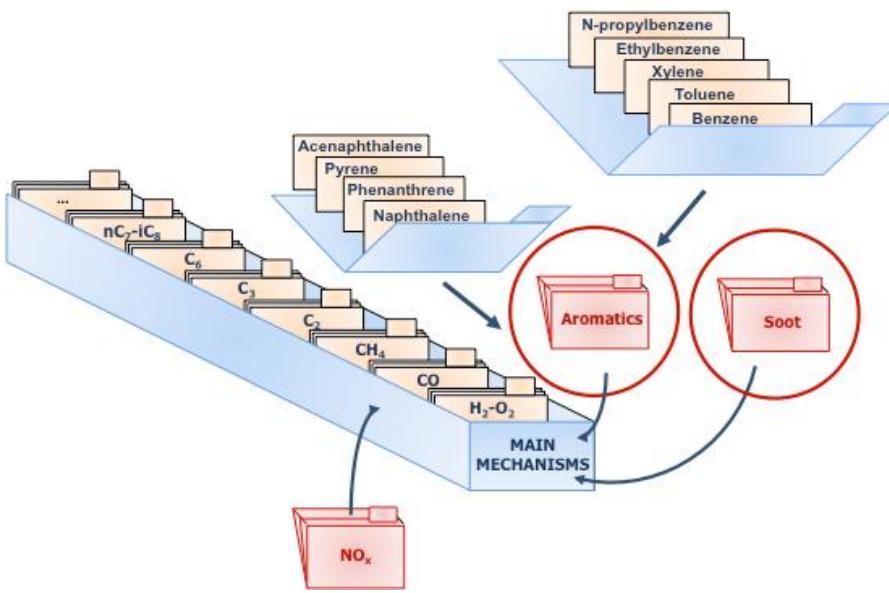
Molecules as key precursor in soot formation



A. D'Anna et al., Combust. Flame 157 (2010) 2106–2115.

The Discrete Sectional Method

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BIN	Mass [amu]	CxHy	Mean Diameter σ [nm]	A	B	C
1	~ 250	$C_{20}H_{16}$ - $C_{20}H_{10}$ - $C_{20}H_6$	0.76	0.8	0.5	0.3
2	~ 500	$C_{40}H_{32}$ - $C_{40}H_{20}$ - $C_{40}H_{12}$	0.96	0.8	0.5	0.3
3	~ 1000	$C_{80}H_{60}$ - $C_{80}H_{36}$ - $C_{80}H_{24}$	1.21	0.75	0.45	0.3
4	~ 2000	$C_{160}H_{112}$ - $C_{160}H_{64}$ - $C_{160}H_{48}$	1.52	0.7	0.4	0.3
5	~ 4000	$C_{320}H_{208}$ - $C_{320}H_{64}$ - $C_{320}H_{64}$	1.91	0.65	0.35	0.20
6	~ 8000	$C_{640}H_{384}$ - $C_{640}H_{224}$ - $C_{640}H_{96}$	2.41	0.6	0.35	0.15
7	~ 15500	$C_{1250}H_{688}$ - $C_{1250}H_{375}$ - $C_{1250}H_{125}$	3.01	0.55	0.3	0.1
8	~ 30000	$C_{2500}H_{1250}$ - $C_{2500}H_{625}$ - $C_{2500}H_{250}$	3.78	0.5	0.25	0.1
9	~ 61000	$C_{5000}H_{2250}$ - $C_{5000}H_{1000}$ - $C_{5000}H_{500}$	4.76	0.45	0.2	0.1
10	~ 121000	$C_{10000}H_{4000}$ - $C_{10000}H_{1500}$ - $C_{10000}H_{1000}$	5.99	0.4	0.15	0.1

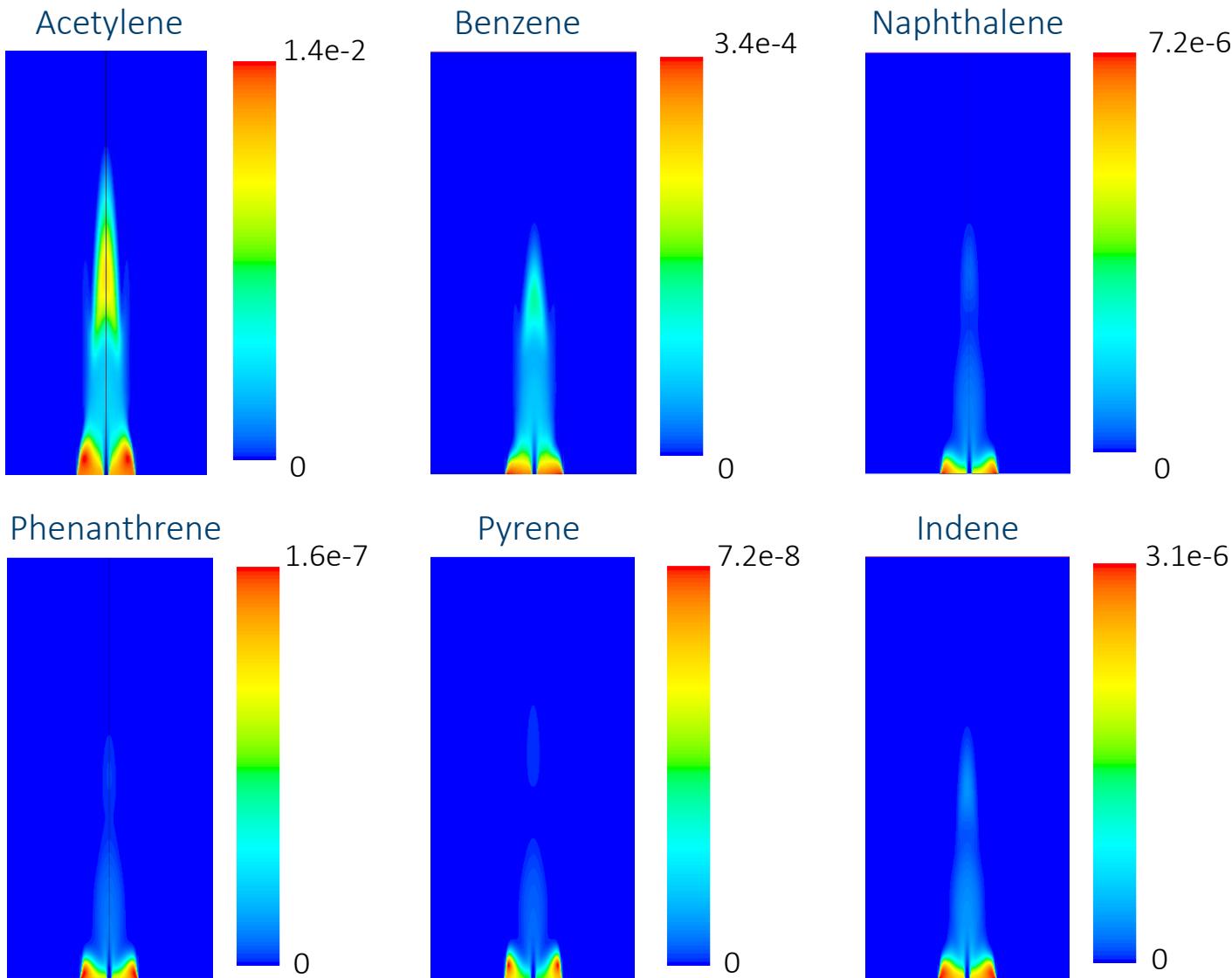
Discrete sectional method: Large PAHs and soot particles with diameters of up to ~60 nm are defined as classes with increasing molecular mass.

Each class is represented by a combination of lumped pseudo-species (BINs), each with an assigned H/C.

The first BIN is the species with **20** carbon atoms and mass of about 250 amu, which is the corannulene. The first particle of soot is considered of about 3000 amu, which is the **BIN5**.

Towards soot: from acetylene to PAHs

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Formation of soot via KPP

Soot particles **do** influence the temperature field through thermal radiation

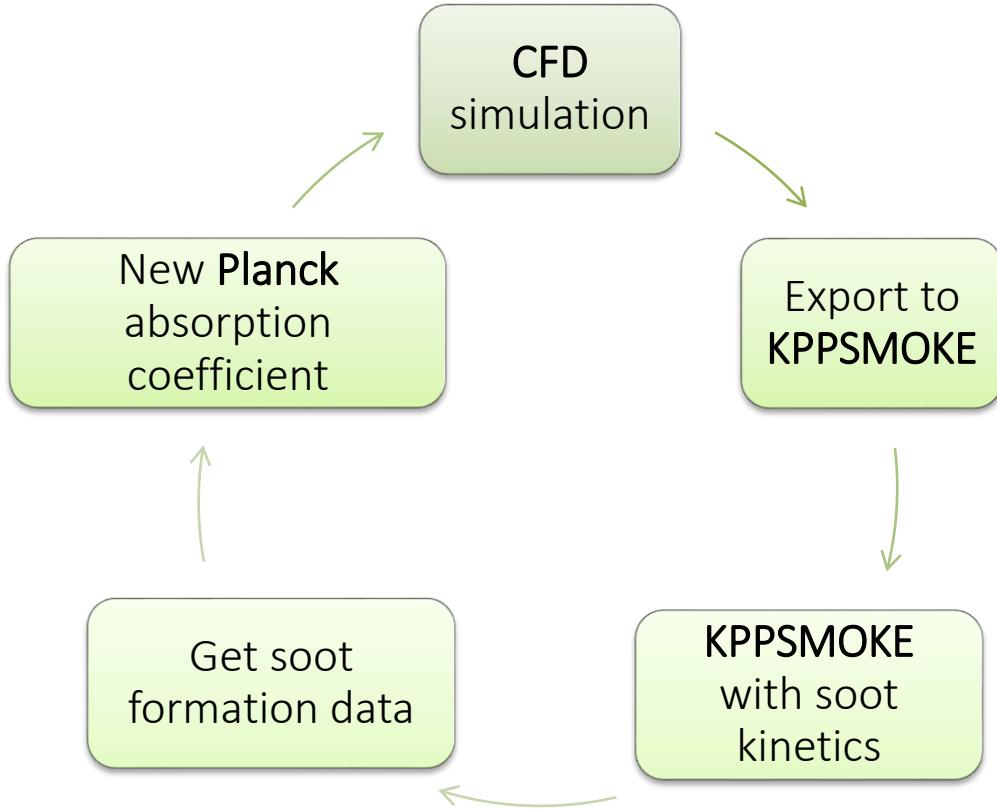
KPPSMOKE **decoupling** between mass and energy balances is no longer valid

BUT

An iterative coupling between mass and energy balances is still possible



Planck absorption coefficient and loop closure





1. The CRECK Modeling Group @ Politecnico di Milano
2. Introduction
3. The Kinetic Post Processing (KPP) Technique for NOx
 - ✓ Kinetic mechanisms for CFD applications
 - ✓ Reactor networks from CFD
 - ✓ Effects of temperature fluctuations on NOx formation
 - ✓ Solution of reactor networks
4. Applications to lab-scale and industrial flames
 - ✓ Lab-scale flames
 - ✓ Industrial cases
5. Extension to other pollutants
6. Conclusions

Papers on Kinetic Post Processing of NOx (I)

Monaghan R., Tahir R., Bourque G., Gordon R., Cuoci A., Faravelli T., Frassoldati A., Curran H., "Detailed emissions prediction for a turbulent swirling non-premixed flame", (2014) Energy & Fuels, 28 (2), pp 1470-1488, DOI: 10.1021/ef402057w

Stagni A., Cuoci A., Frassoldati A., Faravelli T., Ranzi E., "A fully coupled, parallel approach for the post processing of CFD data through reactor network analysis", (2014) Computers & Chemical Engineering, 60, pp 197-212, DOI: <http://dx.doi.org/10.1016/j.compchemeng.2013.09.002>

Cuoci, A., Frassoldati, A., Stagni, A., Faravelli, T., Ranzi, E., Buzzi-Ferraris, G., Numerical modeling of NOx formation in turbulent flames using a kinetic post-processing technique (2013) Energy and Fuels, 27 (2), pp. 1104-1122, DOI: 10.1021/ef3016987

Shabanian, S.R., Medwell, P.R., Rahimi, M., Frassoldati, A., Cuoci, A., Kinetic and fluid dynamic modeling of ethylene jet flames in diluted and heated oxidant stream combustion conditions (2013) Applied Thermal Engineering, 52 (2), pp. 538-554 DOI: 10.1016/j.applthermaleng.2012.12.024

Monaghan, R.F.D., Tahir, R., Cuoci, A., Bourque, G., Furi, M., Gordon, R.L., Faravelli, T., Frassoldati, A., Curran, H.J., Detailed multi-dimensional study of pollutant formation in a methane diffusion flame (2012) Energy and Fuels, 26 (3), pp. 1598-1611, DOI: 10.1021/ef201853k

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Frassoldati, A., Cuoci, A., Faravelli, T., Ranzi, E., Colantuoni, S., Di Martino, P., Cinque, G., Kern, M., Marinov, S., Zarzalis, N., Da Costa, I., Guin, C., Fluid dynamics and detailed kinetic modeling of pollutant emissions from lean combustion systems (2010) Proceedings of the ASME Turbo Expo, 2 (PARTS A AND B), pp. 451-459, DOI: 10.1115/GT2010-22551

Frassoldati, A., Sharma, P., Cuoci, A., Faravelli, T., Ranzi, E., Kinetic and fluid dynamics modeling of methane/hydrogen jet flames in diluted coflow (2010) Applied Thermal Engineering, 30 (4), pp. 376-383, DOI: 10.1016/j.applthermaleng.2009.10.001

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A. CUOCI, A. FRASSOLDATI, BUZZI FERRARIS G, T. FARAVELLI, RANZI E.M. (2007). The ignition, combustion and flame structure of carbon monoxide/hydrogen mixtures. Note 2: Fluid dynamics and kinetic aspects of syngas combustion. INTERNATIONAL JOURNAL OF HYDROGEN ENERGY, vol. 32, p. 3486-3500, ISSN: 0360-3199, doi: 10.1016/j.ijhydene.2007.02.026

Other

Stagni A., Cuoci A., Frassoldati A., Faravelli T., Ranzi E., "Lumping and reduction of detailed kinetic schemes: an effective coupling", Industrial & Engineering Chemistry Research, Accepted, In press (2014), DOI: 10.1021/ie403272f

Ranzi, E., Frassoldati, A., Grana, R., Cuoci, A., Faravelli, T., Kelley, A.P., Law, C.K.. Hierarchical and comparative kinetic modeling of laminar flame speeds of hydrocarbon and oxygenated fuels (2012) Progress in Energy and Combustion Science, 38 (4), pp. 468-501, DOI: 10.1016/j.pecs.2012.03.004

Frassoldati, A., Cuoci, A., Faravelli, T., Niemann, U., Ranzi, E., Seiser, R., Seshadri, K., An experimental and kinetic modeling study of n-propanol and iso-propanol combustion (2010) Combustion and Flame, 157 (1), pp. 2-16, DOI: 10.1016/j.combustflame.2009.09.002